Implementation of Image Registration for Satellite Images using Mutual Information and Particle Swarm Optimization Techniques

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ABSTRACT

The aim of this research is to register satellite images on the DSP processor using probabilistic optimization method named as particle swarm optimization. Satellite image registration is necessary in order to find change detection, to eliminate influence of camera distortion (roll, pitch and yaw), merge satellite imagery and in urban planning. Particle Swarm Optimization is a stochastic search technique with less computation and still very effective as compared to other optimization techniques. It is based on bird flocking, fish schooling and swarm theory. Each particle changes its position and velocity based on its corresponding fitness value. Fitness value can be calculated using joint entropy and mutual information. The algorithm can be used in object recognition, image segmentation, matching and registration. The performance of this algorithm is measured and results are shown using DSK 6713 hardware along with VM32242.

Keywords

Image Registration, Mutual Information, Joint Histogram, Joint Entropy, Particle Swarm Optimization

1. INTRODUCTION

Image registration is a method of aligning two images. First image is called reference image which is fixed and second image is called sensed image which it to be transformed and then registered over reference image. This basic capability is required in various image analysis applications like satellite images used for remote sensing, medical image processing and analysis and in computer vision. The alignment process will find the correspondence between key points in the two images. Image features are unique image properties that can be used to establish correspondence between the images. The most required features are points, because point's coordinates can be directly used to determine the parameters of a transformation function that registers the images.

Correlation based methods registered images directly without finding their features. One image was shifted over another and at each shift position the similarity between the two was determined. The shift position producing the highest similarity was chosen to register the images.

To reduce the computation time sub images can be used and to speed up further multi stage and coarse to fine methods can be used. If the given image has non linear geometric differences, as the scale of the images is reduced, making the image more similar, registration accuracy increases. One can find feature points in low resolution image and map that point in next higher resolution and gradually finding more and more confident points. Image registration will require image transformation, similarity measure and optimizer as shown in fig. 1.



Fig. 1 Basic Image Registration block diagram

Image transformation can be applied over sensed image and transformed sensed image is compared with reference image. Mutual information is used as a similarity measure in this case which is fitness function for particle swarm optimization. If mutual information is less than some predefined value then again transformation is applied over sensed image and procedure repeats until maximum number of iteration is completed. So finally sensed image is registered and quality assessment parameters like RMSE, PSNR, CC and SSIM have been computed.

Image matching and registration is an Optimization problem. Finding the maximum of similarity measure or minimum of dissimilarity measure is a multi-dimensional optimization problem. As number of dimension will increase, degree of freedom will decrease. Therefore it is becoming computationally demanding where exhaustive search over the entire image is required.

There are many optimization techniques available like Simulated Annealing, Genetic algorithm, Memetic algorithm, Ant colony optimization, Differential evolution, Powell's method, Downhill Simplex method, Brent's method and series of one dimensional searches, Levenberg Marquardt optimization, Newton Raphson iteration, Stochastic search methods, Gradient descent methods, Genetic methods, Fuzzy methods, Geometric hashing, Nelder Mead Optimization, Neural Network based methods, Quasi exhaustive search methods, Particle Swarm Optimization (PSO) and many more. Out of these, PSO is suitable for continuous optimization problem because it is highly non linear, non differentiable and non convex.

2. PREVIOUS WORK

Viola and Wells [5] suggested mutual information based image alignment. The method is based on mutual information between the two images. In this, entropy of two images, joint entropy and joint histogram is calculated. This is an intensity based method, it works well where edge and gradient based method fail to register and robust than correlation based method.

Chen et al. [7] proposed medical image registration for multi modal images (CT - MR Brain images) using generalized partial volume estimation (GPVE) technique. Their experimental results show that by properly choosing the kernel functions, the GPVE algorithm significantly reduces the interpolation induced artifacts and thus improving the registration accuracy.

Berthilsson [9] tried to register using cross correlation which is more global search method compared to others like steepest descent based methods. Algorithm is based on certain changes of coordinates in the image and Fast Fourier Transform that makes it faster.

Wolberg and Zokai [14] suggested hierarchical image registration where the affine parameters are computed iteratively using a variation of the Levenberg – Marquadt nonlinear least squares optimization method. In this paper, they are using Sum of Squared Difference (SSD) similarity measure for iterative estimation of perspective deformation. Every time, SSD value is compared with threshold, if SSD is higher than threshold then it is rejected and when SSD is minimum will be the best match. This method is less accurate than NCC but it is faster.

Huttenlocher et al. [15] described new method of similarity measure called Hausdorff Distance (HD). They registered binary images transformed by rotation and translation and compared HD based method with classical CC based method and proved that HD is better than CC.

Mutual information (MI) based image registration can be done for multimodal images. MI which is originating from information theory is a measure of statistical dependency between two data sets. Ritter et al. [16] proposed hierarchical search strategy along with simulated annealing to find maximum mutual information.

Meisen Pan [17] suggested fuzzy based image registration in which Fuzzy C- Means (FCM) clustering is used and divided the coordinates of the pixels in the image into two clusters to fit a straight line, and then derived the slope of the line to compute the rotation angle of the image. Fuzzy method provides good result for mono modal and multi modal (with different sensors) images.

J. Senthilnath [20] suggested multi objective function for fitness calculation. They have used distance condition and angle condition both because only distance condition cannot be effective for multi sensor images. These two conditions give better matching of the corner points between the two images. A set of three points between reference image and sensed image is required in the algorithm. In the past, RANSAC is used to match the points. Based on the results obtained to them, their algorithm is more efficient for multi sensor image registration. Registration accuracy is measured in terms of root mean square error.

Chen Lun Lin [22] described Hybrid particle swarm optimization (HPSO) for medical image registration. HPSO includes two important concept subpopulation and crossover of genetic algorithm and conventional PSO and also provide comparison between HPSO, Genetic algorithm and conventional PSO.

Yong Fang Guo [24] introduced improved PSO for image matching and proved that this method is a simple but effective and reduces computation time. In [25], Yong Fang Guo have modified the method and calculated another objective function using distance transform and PSO and shown that it will again reduce time complexity of the algorithm.

Object detection can also be done using particle swarm optimization proved by Ankit Sharma in [28]. They have determined cross correlation coefficient between the images and applied PSO. Applications are in navigation, guidance, automatic surveillance and robot vision.

Finding point correspondence using Simulated Annealing (SA) explained by Starink and Baker [31] that tries to minimize a dissimilarity measure defined on point pairs. SA is a stochastic optimization algorithm based on the physical analogy of annealing a system of molecules to its ground state.

Thevenaz et al. [32] explained iterative multi scale registration without landmarks in which they have combine Levenberg Marquardt method and sum of squared differences metric. They present an automatic sub pixel registration algorithm which minimizes the mean square difference of intensities between a reference image and sensed image. It uses coarse to fine pyramid strategy and performs minimization using Levenberg Marquardt method. They have used several images from PET and fMRI modalities and concluded that multi resolution refinement strategy is faster and more robust than single scale methods.

We had taken satellite images in which preprocessing is already done otherwise we have to do radiometric correction on raw images which include LUT corrections, stagger correction, correction for block and line losses etc. Some users also expect geometric corrections also to be done on these images. Challenges to register satellite images are mainly because they are linear arrays of CCDs; many such lines together form an image. (The normal images are taken from frame cameras). Here every linear array image is a frame and you can look forth for variations in camera orientations between every frames of such linear arrav giving rise to internal distortion within the image. A corrected satellite image can be free of such distortions.

3. PARTICLE SWARM OPTIMIZATION

There are many methods available for optimization problem. Methods are either deterministic or probabilistic in nature. Deterministic method gives exact solutions and do not use any random technique and rely on the thorough search of the feasible domain. But the disadvantages of deterministic method is it is not robust and can only be applied to restricted class of problems and Often too time consuming or sometimes unable to solve real world problems. Particle Swarm Optimization is an iterative, learning based method introduced by James Kennedy and Eberhart in 1995.

It is population based method and in this context, the population is called swarm and the individuals are called particles. Particles are randomly initialized within the parameter space and each particle is given an initial velocity. Fitness function is computed for each position and if fitness value is less than some threshold then position of particle is updated and a new velocity is calculated in each iteration. Find the best position of the particle and generates social groups, where each particle has different logical neighbors. Each particle will remember its best value and X and Y coordinate of it.

For each iterative process, the particle can update its position (x_i^k) , velocity (v_i^k) and moving based on the particle best (p_{best}) and global best (g_{best}) as following.

$$x_{i}^{k+1} = x_{i}^{k} + v_{i}^{k+1}$$
(1)
$$v_{i}^{k+1} = r_{1} \omega v_{i}^{k} + c_{1} r_{2} (p_{best} - x_{i}^{k})$$

 $\begin{array}{c} v_{i} = r_{1} \otimes v_{i} + c_{1} r_{2} (p_{best} - x_{i}^{k}) \\ + c_{2} r_{3} (g_{best} - x_{i}^{k}) \end{array}$ (2)

Where k is the current iteration, c_1 and c_2 are two positive constants, r_1 , r_2 and r_3 are random number in the range [0, 1]. ω is inertia that will control the influence by the former moving velocity. ω is greater, then global searching performance is better while smaller ω would bring better local search.

4. IMAGE SIMILARITY USING MUTUAL INFORMATION

Fitness function can be calculated using the following equations of mutual information between reference and sensed image and maximum value indicate best match.

Mutual Information (MI) has emerged in recent years as a very effective measure of image comparison. It is intensity based method so it takes into account spatial relationship between pixels.

4.1 Entropy

Entropy is a measure of information. Any image is basically matrix which consists of various intensity values which are random in nature. Shannon entropy probability distribution function is defined by the following equation.

$$H(A) = -\sum_{a} P_A(a) \log_2 P_A(a)$$
(3)

Entropy measures the uncertainty inherent in the distribution of a random variable.

4.2 Joint Entropy

MI is intensity based similarity measure and is closely related with joint entropy of two images which can be calculated from the following equation.

$$H(A,B) = -\sum_{a,b} P_{A,B}(a,b) \log_2 P_{A,B}(a,b)$$
(4)

Joint entropy and conditional entropy are simple extensions that measure the uncertainty in the joint distribution of a pair of random variables, and the uncertainty in the conditional distribution of a pair of random variables. Images are registered when one is transformed relative to the other to minimize the joint entropy.

4.3 Joint Histogram

Individual entropies can be easily calculated from Joint histogram. A joint histogram is a multidimensional histogram created from a set of local pixel features. An entry in a joint histogram counts the number of pixels in the image that are described by a particular combination of feature values. Each entry is the number of times intensity in one image corresponds to an intensity b in the other. Row number is intensity of image 1, i.e. 1st row is the occurrence of intensity 1 in image 1. Column number is intensity of image 2, i.e 1st column is the occurrence of intensity 1 in image 2.

Usually a discrete joint histogram is considered to estimate the joint PDF for the calculation of MI. attempting to compute the overlapping regions; we should maximize the individual entropies and minimize the joint entropy. An image of single amplitude has a less disperse histogram than an image of many grey scales and the lower dispersion implies lower entropy.

4.4 Mutual Information

Mutual information between two images is calculated from individual entropy and Joint entropy as follows.

$$MI(A,B) = H(A) + H(B) - H(A,B)$$
 (5)

Advantage in using mutual information over joint entropy is it includes the individual entropy. Maximizing the mutual info is equivalent to minimizing the joint entropy. After registration joint entropy increases as matching is achieved so the correspondence of pixel to pixel increases, which in terms increase the mutual information.

5. HARDWARE USED

Digital signal processing is now become core in most of the rapidly growing technologies like signal and image processing and in wireless communication. These processors are having capabilities of representing real time analog signals in digital form with fast processing speed. The TMS 320C67X series is a 32 bit floating point processor having implemented VLIW architecture. It requires one computer to create the program, embedded JTAG to load the program from computer to C6713, an AIC23 stereo codec, 4 user accessible LEDs and DIP switches, power supply, 32 bit external memory interface and VM3224K2 display card. The on board power supply provides two voltages, 1.26 V for DSP core and 3.3 V for I/O ports. DSK 6713 operates on 225 MHz. Synchronous dynamic RAM is of 16 MB and Flash of 512 KB [34].

Code composer studio (CCS) provides an IDE to incorporate the software tools. CCS includes tool for code generation (C compiler), debugging tool, assembler and linker. The C compiler will compile the C code with extension .c and generating .asm assembly file. The assembler converts .asm file into machine language object file .obj. the linker links and combines object and library files and generates .out file which can be loaded using CCS into C6713 and run on C6713. The CCS has Graphical User Interface (GUI) using which we can view Time/ Frequency graph, Eye diagram, Constellation diagram and Images.

The DSP VM3224K2 is a TFT LCD video daughter card which support NTSC analog video signal and displays digital video data on TFT LCD display. It used NTSC up to 30 fps as a input and gives output in the form of RGB565 format. The resolution for video / image output is 320 X 240 with 16 bits per pixel. It uses power from DSP board so no additional power is required. This product is a plug in for the Texas instruments C67X starter kit.

The RGB24 is more widely used in different image based applications. In RGB24 format each channel is having 0 - 255 (8 bit) so total $2^{24} = 16$ million different colors. Internally, for memory cache line efficiency this is stored as 4 bytes instead of 3 and thus one bye is lost in exchange of extra access performance. But in embedded systems the memory saving and processing time is the main requirement of any system. The RGB 565 format used 16 bit format to represent color

image. So extra 2 bytes are saved and thus saved time too. In this system 5 bits for red, 6 bits for green and 5 bits for blue color. Human eye is more sensitive to green color so extra 1 bit is added to green component.



Fig. 2 Structure of the TFT LCD Display Unit [33]

The Thin Film Transistor (TFT) LCD uses an RGB565 format and having 320x240 in size. The LCD panel should given pixel information periodically. So VM3224K2 module contains memory which will store 320 X 240 pixel information. LCD controller provides 512 KB DRAM memory data to the LCD panel in synchronization with the horizontal and vertical sync signals. 512 KB DRAM is divided into two parts: 256 KB size in two pages. One part is for display buffer and other is used by DSP. The LCD controller generates signals to drive the LCD, and the 17-bit address generator generates pixel data addresses directed to the LCD.

Pixel locations in TFT-LCD display are shown in fig. 3. The first number in parenthesis represents the horizontal coordinate on the LCD panel, while the second represents the vertical coordinate.

(0,0)	(1,0)	 (318,0)	(319,0)
(0,1)	(1,1)	 (318,1)	(319,1)
		 •••	•••
(0,238)	(1,238)	 (318,238)	(319,238)
(0,239)	(1,239)	 (318,239)	(319,239)

Fig 3 Pixel Locations for the Landscape Panel [33]

6. QUALITY ASSESSMENT PARAMETERS

6.1 Root Mean Square Error

$$RMSE = \sqrt{\frac{1}{MN} \sum_{i=1}^{M} \sum_{j=1}^{N} (x(i,j) - y(i,j))^{2}} \quad (6)$$

It is measure of estimator which suggests the accuracy of registration with respect to reference image. It should be near to zero for best match.

6.2 Peak Signal to Noise Ratio

$$PSNR = 10 \log_{10} \frac{(2^n - 1)^2}{MSE}$$
(7)

It is a ratio of maximum possible power of signal to power of corrupting noise that affects the fidelity of representation. Its range is wide so it is expressed as logarithmic scale. Maximum value of PSNR indicates good match between the two images.

6.3 Cross Correlation

$$= \frac{\sum_{i=1}^{M} \sum_{j=1}^{N} (x(i,j) - \bar{x})(y(i,j) - \bar{y})}{\sqrt{\sum_{i=1}^{M} \sum_{j=1}^{N} (x(i,j) - \bar{x})^2 \sum_{i=1}^{M} \sum_{j=1}^{N} (x(i,j) - \bar{y})^2}}$$
(8)

Range of cross correlation is between -1 to +1. Minimum value indicates the dissimilarity between the images. For maximum matching, its value is 1.

6.4 Structural Similarity Index Matrix

$$=\frac{(2\ \bar{x}\ \bar{y}\ +C1)(2\ \sigma xy\ +C2)}{(\sigma x^{2}\ +\ \sigma y^{2}\ +\ C2)((\bar{x})^{2}\ +\ (\bar{y})^{2}\ +\ C1)} \tag{9}$$

It is a method for comparing the two images using similarity criterion. It is a quality measure of one of the image being compared with another image having perfect quality. It is an improved version of the universal image quality index (UIQI). The mean SSIM is one when two images are same. The difference with RMSE and PSNR is that these approaches estimate perceived errors. Conversely, SSIM considers image degradation as perceived change in structural data which is having strong inter- dependencies (important information about the structure of the object) specifically when they are spatially close.

To compute above quality parameters, the size of two images must be same. x(i,j) is the reference image, y(i,j) is the sensed image, n is the number of bits per pixel, so $(2^n - 1)$ represents maximum gray value, \bar{x} and \bar{y} are the mean values for reference and sensed image respectively, σx^2 and σy^2 are the variance of x and y images, σxy is the covariance of x and y, *M* and *N* are the height and width of the image. C₁ and C₂ are the constants.

$$C_1 = (k_1 * L)^2$$
 and $C_1 = (k_1 * L)^2$ (10)

Where $k_1 = 0.01$ and $k_2 = 0.03$ (default) and $L = (2^n - 1)$

7. ALGORITHM

We have used the following algorithm.

- 1. The first step is to read two satellite images one reference image and another sensed image using DSK 6713. To read the images we have to convert them into .dat file format using MATLAB.
- 2. Open code composer studio 3.1 and connect DSP 6713 kit and then create new project using .pjt extension.
- 3. Open editor window and write C code. Create population of agents called particles which is uniformly distributed and save the details of the particles into two swarm matrixes (one for x and other for y coordinate) which include initial position of the particles, velocity of each particles, updated position, and fitness values / objective function.
- 4. If current position of particle is better than previous one then update it and also update its velocity using equation (1) and (2).
- 5. Calculate fitness value (using equation (5)) and place it at the fourth column and evaluate particle best (pbest) and global best (gbest).

- 6. Repeat the procedure until stopping criterion is satisfied.
- 7. Save the program using .c extension and then add in the current project and build the program. Then load the .out file and run the program.

8. RESULT AND DISCUSSION

The images we have used are taken from Bhuvan website -a Geoportal of ISRO. First set of image is of Vallabh Vidyanagar and we are trying to register Shastri medan area. Second set of image is of New Vallabh Vidyanagar and we had registered academic institutions of CVM including A. D. Patel Institute of Technology.



Fig. 4 - Set 1: Reference and Sensed Image of Vallabh Vidyanagar



Fig. 5 Registered Image



Fig. 6 - Set 2: Reference and Sensed Image of New Vallabh Vidyanagar



Fig. 7 Registered Image

Initially particles are given random values and coordinates of each particle are stored in swarm matrix. For each iteration, fitness function is calculated and accordingly particle's position and velocity is updated. This procedure is repeated until stopping criterion is satisfied. Then RMSE, PSNR, CC and SSIM are calculated using equations (6 -10).



Fig. 8 Set up of image Registration using DSP hardware

The below tables 1 and 2 give parameters of image registration. The result on LCD of VM3224K2 is not seen clearly so results of CCS are shown for better visibility using graph of code composer studio.

Entropy of sensed image H(B): 6.9584									
Entropy of reference image: 26.9634									
No. of	Entropy	Joint	Mutual	X	Y	RMSE	PSNR	CC	SSIM
Itera-	H(A)	Entropy	Inform-	Value	Value				
tion		H(A,B)	ation						
			(MI)						
1.	6.9981	13.2979	1.0495	201	125	65.9734	27.0402	0.0074	0.0362
2.	6.9812	13.2849	1.0493	158	118	66.37	26.9204	-0.0031	0.0288
3.	6.8926	13.2057	1.0489	12	70	64.677	27.4372	-0.0197	0.0303
4.	6.9628	13.2725	1.0489	201	188	65.7641	27.1038	0.0145	0.0256
5.	7.0033	13.3002	1.0497	201	86	65.4868	27.1883	0.0055	0.0310
6.	7.0089	13.3082	1.0495	201	100	65.6392	27.1418	-0.0006	0.0190
7.	6.9586	13.2637	1.0492	201	38	64.3596	27.5356	0.0014	0.0413
8.	6.9728	13.2745	1.0495	170	136	65.4552	27.1980	0.0266	0.0311
9.	6.96	13.2580	1.0498	147	140	65.666	27.1336	0.0215	0.0395
10.	6.9578	13.2208	1.0526	140	128	48.2687	33.2896	0.4687	0.2300

Table 1 Ten fold validation result of set 1

Table 2 Ten fold validation result of set 2

Entropy of sensed image H(B): 8.5811									
Entropy of Reference image: 25.0684									
No. of	Entropy	Joint	Mutual	Х	Y	RMSE	PSNR	CC	SSIM
Itera-	H(A)	Entropy	Inform-	Value	Value				
tion		H(A,B)	ation						
			(MI)						
1.	8.2461	16.6650	1.0097	101	66	60.3954	28.8070	-0.0183	0.1240
2.	8.2253	16.6548	1.0091	101	63	60.8512	28.6566	-0.0336	0.1138
3.	8.6428	17.0092	1.0126	63	158	58.6427	29.3960	0.0624	0.0942
4.	8.6344	17.0033	1.0125	46	195	58.0842	29.5874	0.0499	0.0992
5.	8.4949	16.8591	1.0129	82	123	60.3960	28.8068	-0.0278	0.1135
6.	8.6224	16.9843	1.0129	79	158	59.0153	29.2693	0.0414	0.1090
7.	8.6246	16.9725	1.0137	86	176	57.1590	29.9085	0.0848	0.1019
8.	8.5737	16.7298	1.0254	95	209	46.5916	33.9969	0.3702	0.1514
9.	8.5868	16.5764	1.0357	99	195	42.2731	35.9422	0.4879	0.1378
10.	8.5858	16.5282	1.0386	100	195	40.7711	36.6658	0.5235	0.1835







9. CONCLUSION

In this paper, Particle swarm optimization based satellite image registration is done. This method is iterative learning based method where particles will remember its position and depending on fitness function value, algorithm will update particle's position and velocity. To calculate accuracy of this registration, we have compute quality assessment parameters. The algorithm will be ended when error becomes zero or minimum. Ten fold validation method is used to check the performance of PSO in which the process is repeated for 10 times and parameters are measured. Moreover, the parameters like number of particles, inertia, positive coefficients, number of iterations, size of two images and fitness function will affect the registration time and registration result.

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