

# SC-FDMA based Systems to Reduce PAPR by using a Modified Commanding Scheme

Sajjan Singh<sup>1</sup>

<sup>2</sup>Ph.D Research Scholar  
Department of Electronics &  
Communication Engineering  
Lingaya's University Faridabad,  
India

Pardeep<sup>2</sup>

<sup>1</sup>M.Tech Research Scholar  
Department of Electronics &  
Communication Engineering  
BRCM CET, Bahal  
Bhiwani, India

S. V. A. V. Prasad<sup>3</sup>

<sup>3</sup>Professor  
Department of Electronics &  
Communication Engineering  
Lingaya's University  
Faridabad, India

## ABSTRACT

The 3rd generation partnership project (3GPP) long term evolution (LTE) standard uses single carrier frequency division multiple access (SCFDMA), scheme for the uplink transmissions and orthogonal frequency division multiplexing access (OFDMA) in downlink. SCFDMA makes use of single carrier modulation and frequency domain equalization, it is a technique that has similar performance and essentially the same overall complexity as those of OFDM, But in OFDMA high peak-to-average power ratio (PAPR) is a major drawback. An outstanding advantage of SC-FDMA is its lower PAPR due to its single carrier structure. In this paper, we analyze the PAPR of SC-FDMA signals with pulse shaping. We analytically derive the time domain SC-FDMA signals and numerically compare PAPR characteristics using the complementary cumulative distribution function (CCDF) of PAPR. The results show that SC-FDMA signals indeed have lower PAPR compared to those of OFDMA. Comparing the two forms of SC-FDMA, we find that localized FDMA (LFDMA) has higher PAPR than interleaved FDMA (IFDMA) but somewhat lower PAPR than OFDMA. Also noticeable is the fact that pulse shaping increases PAPR. To reduce the PAPR, we propose an efficient Kalman filter based PAPR reduction algorithm.

## Keywords

OFDMA, SC-FDMA, IFDMA, LFDMA, PAPR, Kalman Filter

## 1. INTRODUCTION

Today demands for media-rich wireless data services have brought much attention to high speed broadband mobile wireless techniques in recent years. Orthogonal frequency division multiplexing (OFDM), which is a multicarrier communication technique, has become widely accepted primarily because of its robustness against frequency selective fading channels which are common in broadband mobile wireless communications. Orthogonal frequency division multiple access (OFDMA) is a multiple access scheme which is an extension of OFDM to accommodate multiple simultaneous users. Furthermore, by adding the cyclic prefix in an OFDM symbol as the guard interval, it can reduce the inter-channel interference (ICI) and inter-symbol interference (ISI).

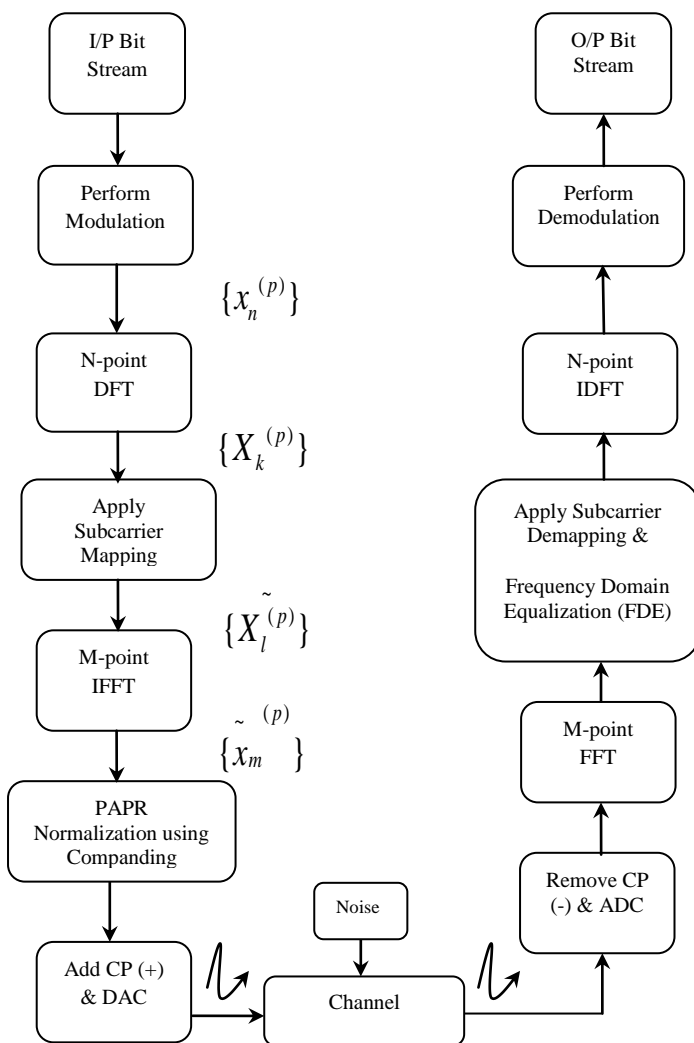
Long term evolution (LTE) is standardized by the third generation partnership project (3GPP) and is an evolution to existing 3G technologies in order to meet projected customer needs over the next decades. 3GPP LTE uses orthogonal

frequency division multiplexing access (OFDMA) for downlink transmission and single carrier frequency division multiple access (SCFDMA) for uplink. SCFDMA is a promising technique for high data rate transmission that utilizes single carrier modulation and frequency domain equalization. Single carrier transmitter structure leads to keep the peak to average power ratio (PAPR) as low as possible that will reduce the energy consumption. SCFDMA has similar throughput performance and essentially the same overall complexity as OFDMA [1]. A highly efficient way to cope with the frequency selectivity of wideband channel is OFDMA. OFDMA is an effective technique for combating multipath fading and for high bit rate transmission over mobile wireless channels. In OFDMA system, the entire channel is divided into many narrow sub channels, which are transmitted in parallel, thereby increasing the symbol duration and reducing the inter-symbol-interference (ISI). OFDMA is highly suitable for broadband wireless access networks (particularly the downlink) since it combines scalability, multipath robustness, and multiple-input multiple-output (MIMO) compatibility [2]. OFDMA is sensitive to frequency offset and phase noise, and thus requires accurate frequency and phase synchronization. LTE has selected orthogonal frequency division multiple access (OFDMA) in the downlink and single-carrier frequency-division multiple access (SC-FDMA) in the uplink [4]. However, other standards, such as Worldwide Interoperability for Microwave Access (WiMAX), use OFDMA in both links, given the benefits of having the same access scheme in terms of reciprocity, allocation flexibility, and bandwidth efficiency [4]. SC-FDMA can be regarded as a DFT-spread OFDMA, where time domain data symbols are transformed to frequency domain by the DFT before going through the OFDMA modulation. In the SC-FDMA systems, a set of orthogonal subcarriers is allocated for each user as in the OFDMA system. There are two popular subcarriers mapping techniques in the SC-FDMA systems; the localized technique and the interleaved technique. In the Localized SC-FDMA or simply LFDMA, the band of each user occupies a dedicated part of the usable spectrum. On the other hand, in Interleaved SC-FDMA or simply IFDMA, the bands of the users are interleaved [5, 6]. Though IFDMA is more desirable than LFDMA in terms of PAPR power efficiency, LFDMA is clearly superior in terms of throughput when channel dependent scheduling is utilized. Thus, LFDMA has been widely implemented in LTE [7]. Currently, the PAPR reduction algorithms in the literature can be categorized as the following three classes of algorithms as (1) the pre-distortion algorithms, (2) coding algorithms and (3) statistical algorithms. The statistical algorithms, such as the

PTS algorithm, and the SLM algorithm, have relatively good performance in regards to the out-of-band interferences and information transfer rate, but signal shape degrades [13,14].

## 2. OVERVIEW OF SC-FDMA SYSTEM MODEL

A simplified block diagram of the SC-FDMA transceiver is depicted in Figure 1. Figure 1 illustrates the transmitter and receiver structure of SC-FDMA system. At the transmitter side, a baseband modulator transmits the binary input to multilevel sequences of complex number  $\{x_n^{(p)}\}$  in one of several possible available modulation formats, such as Quadrature Phase Shift Keying (QPSK), and Quadrature Amplitude Modulation (QAM), etc [7]. The transmitter next groups the modulation symbols,  $x_n^{(p)}$  into blocks each containing  $N$  symbols.



**Fig 1: Transmitter and Receiver structure of an SC-FDMA system model.**

The first step in modulating the SC-FDMA subcarriers is to perform an  $N$ -point discrete Fourier transform (DFT), to produce a frequency domain representation  $X_k^{(p)}$  of the input symbols as given by (1). It then maps each of the  $N$

DFT outputs to one of the  $M (> N)$  orthogonal subcarriers that can be transmitted. Typically,  $N = M/Q$  is an integer sub multiple of  $M$ .  $M$  represents the total number of available subcarriers, where  $M = Q.N$ .  $Q$  is the bandwidth expansion factor of the symbol sequence. For example, if all terminals transmit  $N$  symbols per block, the system can handle  $Q$  simultaneous transmissions without co-channel interference. We further assume that each user occupies the same number of subcarriers, so in this case  $Q$  also represents the number of users. Each user  $p$ ,  $p = 0, 1, \dots, Q-1$  generates a block of  $N$  complex-valued symbols  $x_n^{(p)}$  where  $n = 0, 1, \dots, N-1$ . By applying an  $N$ -point DFT to  $x_n^{(p)}$ , the frequency domain symbols  $X_k^{(p)}$  can be described as:

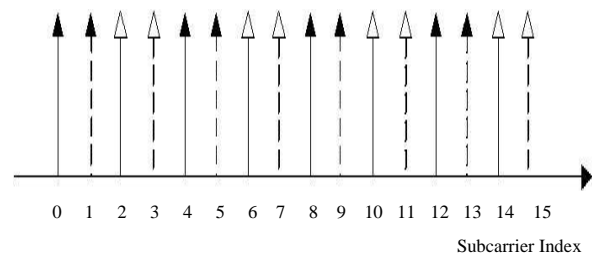
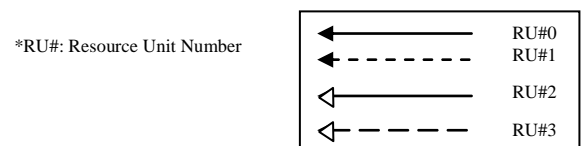
$$X_k^{(p)} = \sum_{n=0}^{N-1} x_n^{(p)} e^{-j\frac{2\pi}{N}kn} \quad \dots (1)$$

The frequency domain symbols are then mapped onto a set of user-dependent subcarriers [10]. The result of the subcarrier mapping is the set of complex subcarrier amplitudes, where  $N$  of the amplitudes are non-zero. As in OFDMA, an  $M$ -point inverse FFT (IFFT) transforms the subcarrier amplitudes to a complex time domain signal. Each then modulates a single frequency carrier and all the modulated symbols are transmitted sequentially [8].

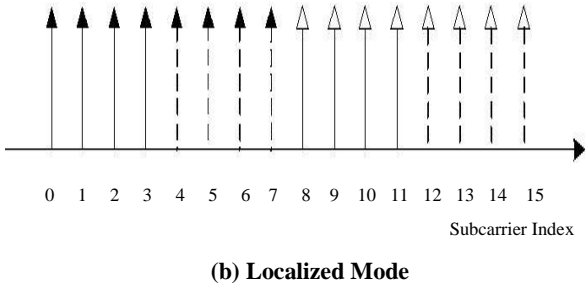
The transmitter performs two other signal processing operations prior to transmission. It inserts a set of symbols referred to as a cyclic prefix (CP) in order to provide a guard time to prevent inter-block interference (IBI) due to multipath propagation. The transmitter also performs a linear filtering operation referred to as pulse shaping in order to reduce out-of-band signal energy [9].

There are  $M$  subcarriers, among which  $N (< M)$  subcarriers are occupied by the input data. In the time domain, the input data symbol has symbol duration of  $T$  seconds and the symbol

duration is compressed to  $\tilde{T} = (N/M)T$  after going through SC-FDMA modulation [11]. There are two methods to choose the subcarriers for transmission as shown in Fig. 2.

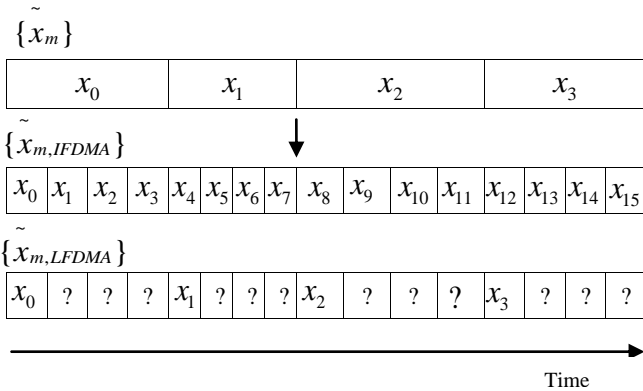


**(a) Distributed Mode**



**Fig. 2: Frequency Domain Representation of SC-FDMA system: Distributed mode, (b) Localized mode. An example of  $M=16$ ,  $Q=4$  and  $N=4$**

Figure 2 shows an example of a frequency division multiple access schemes with distributed and localized subcarrier mapping. There are 16 ( $M=16$ ) available subcarriers shared by 4 ( $Q=4$ ) users and each user occupies 4 ( $N=4$ ) subcarriers. Each user must map its frequency domain symbols onto the assigned resource unit (RU) and zeros are inserted for the remaining subcarriers. In DFDMA, the RU for each user is a set of interleaved subcarriers across the available transmission band. DFDMA is robust against frequency selective fading since it better exploits the available frequency diversity [10]. In LFDMA, the RU for each user is a set of adjacent subcarriers. LFDMA can potentially achieve multiuser diversity if for each user the localized section of allocated bandwidth experiences high channel gain. This form of multiuser diversity requires independent frequency selective fading per user combined with intelligent radio resource unit allocation [10]. In the distributed subcarrier mapping mode, DFT outputs of the input data are allocated over the entire bandwidth with zeros occupying in unused subcarriers, whereas consecutive subcarriers are occupied by the DFT outputs of the input data in the localized subcarrier mapping mode. We will refer to the localized subcarrier mapping mode of SC-FDMA as localized FDMA (LFDMA). The case of  $M = Q$ .  $N$  for the distributed mode with equidistance between occupied subcarriers is called Interleaved FDMA (IFDMA) [11].



**Fig. 3 An example of SC-FDMA transmit symbols in the time domain for  $N = 4$ ,  $Q = 4$  and  $M = 16$ .**

An example of SC-FDMA transmit symbols in the time domain for  $N = 4$ ,  $Q = 4$  and  $M = 16$  is illustrated in figure 3. After subcarrier mapping, the frequency data is transformed back to the time domain by applying inverse FFT (IFFT).

The frequency domain samples  $\{\tilde{X}_l^{(p)}\}$  after the subcarrier mapping process (Distributed and Localized) are represented by equations (2) and (3) respectively:

$$\tilde{X}_l^{(p)} = \begin{cases} X_k^{(p)} = X_{(l-p)/Q}^{(p)}, l = Qk + p \\ 0, \text{ otherwise} \end{cases} \dots\dots (2)$$

$$\tilde{X}_l^{(p)} = \begin{cases} X_k^{(p)} = X_{(l-Np)}^{(p)}, l = k + Np \\ 0, \text{ otherwise} \end{cases} \dots\dots (3)$$

Where  $l$  represents the subcarrier index going into the  $M$ -point IFFT,  $l = 0, 1, \dots, M - 1$  and  $p$  is the resource unit number (RU#). It should be noted that  $p$  can also denote the user index, i.e.  $p = 0, 1, \dots, Q - 1$ . After subcarrier mapping,

the sampling period  $\tilde{T}$  is reduced, i.e.  $\tilde{T} = (N/M) \cdot T$ , where  $T$  is user input symbol period. The frequency domain samples  $\{\tilde{X}_l^{(p)}\}$  are transformed back into the time domain by an  $M$ -point IDFT. The output time domain samples of SC-FDMA before the application of pulse shaping can generally be described by equation (4):

$$\tilde{x}_m^{(p)} = \frac{1}{M} \sum_{l=0}^{M-1} \tilde{X}_l^{(p)} e^{(j\frac{2\pi}{M}ml)} \dots\dots (4)$$

### 3. PAPR OF SC-FDMA SIGNALS

In this section, we analyze the PAPR of the SC-FDMA signal for each subcarrier mapping mode. For distributed subcarrier mapping mode, we will consider the case of IFDMA. In the subsequent derivations, we will assume  $M = Q$ .  $N$ .

Let  $\{x_n : n = 0, 1, \dots, N - 1\}$  be data symbols to be modulated. Then,  $\{X_k : k = 0, 1, \dots, N - 1\}$  are frequency domain samples after DFT of  $\{x_n : n = 0, 1, \dots, N - 1\}$ ,

$\{\tilde{X}_l^{(p)} : l = 0, 1, \dots, M - 1\}$  are frequency domain samples after subcarrier mapping, and  $\{\tilde{x}_m : m = 0, 1, \dots, M - 1\}$  are time symbols after IFFT of  $\{\tilde{X}_l^{(p)} : l = 0, 1, \dots, M - 1\}$ . The complex pass band

transmit signal of SC-FDMA  $x(t)$  for a block of data is represented as:

$$x(t) = e^{j\omega_c t} \sum_{m=0}^{M-1} \tilde{x}_m r(t - m\tilde{T}) \dots\dots (5)$$

Where  $\omega_c$  is the carrier frequency of the system and  $r(t)$  is the baseband pulse. In our research, we use a raised-cosine pulse, which is a widely used pulse shape in wireless communications, defined as follows in the time domain [11, 12].

$$r(t) = \sin c \left( \pi \frac{t}{\tilde{T}} \right) \frac{\cos \left( \frac{\pi \alpha t}{\tilde{T}} \right)}{1 - \frac{4\alpha^2 t^2}{\tilde{T}^2}} \quad \dots (6)$$

Where  $\alpha$  is the roll off factor which ranges between 0 and 1.

The PAPR is defined as the ratio of peak power of  $x(t)$  to the average power of  $x(t)$ , follows for transmit signal  $x(t)$  :

$$PAPR = \frac{\max_{0 \leq t \leq M\tilde{T}} |x(t)|^2}{\frac{1}{M\tilde{T}} \int_0^{M\tilde{T}} |x(t)|^2 dt} \quad \dots (7)$$

Without pulse shaping, that is, using rectangular pulse shaping, symbol rate sampling will give the same PAPR as the continuous case since SC-FDMA signal is modulated over a single carrier [11]. Thus, PAPR without pulse shaping with symbol rate sampling can be expressed as follows:

$$PAPR = \frac{\max_{m=0,1,\dots,M-1} |\tilde{x}_m|^2}{\frac{1}{M} \sum_{m=0}^{M-1} |\tilde{x}_m|^2} \quad \dots (8)$$

#### A. Time domain symbols of IFDMA

For IFDMA, the frequency samples after subcarrier mapping  $\{\tilde{X}_l\}$  can be described as follows.

$$\tilde{X}_l = \begin{cases} X_{l/Q}, l = Q.k & (0 \leq k \leq N-1) \\ 0, \text{ otherwise} & \dots (9) \end{cases}$$

After subcarrier mapping, we derive the time symbols  $\{\tilde{x}_m\}$

which are obtained by taking inverse FFT of  $\{\tilde{X}_l\}$ .

Let,  $m = N.q + n$  where  $0 \leq q \leq Q-1$  and  $0 \leq n \leq N-1$

Then,

$$\begin{aligned} \tilde{x}_m (= \tilde{x}_{Nq+n}) &= \frac{1}{M} \sum_{l=0}^{M-1} \tilde{X}_l e^{j2\pi \frac{m}{M} l} = \frac{1}{Q} \cdot \frac{1}{N} \sum_{k=0}^{N-1} X_k e^{j2\pi \frac{m}{N} k} \\ &= \frac{1}{Q} \cdot \frac{1}{N} \sum_{k=0}^{N-1} X_k e^{j2\pi \frac{Nq+n}{N} k} \end{aligned}$$

If  $q=0$ , then

$$\begin{aligned} &= \frac{1}{Q} \cdot \left( \frac{1}{N} \sum_{k=0}^{N-1} X_k e^{j2\pi \frac{n}{N} k} \right) \quad \dots (10) \\ &= \frac{1}{Q} x_n \end{aligned}$$

The resulting time symbols  $\{\tilde{x}_m\}$  are simply a repetition of the original input symbols  $\{x_n\}$  in the time domain. Therefore, the PAPR of IFDMA signal is the same as in the case of conventional single carrier signal. An example of an IFDMA signal is shown in Fig. 3.

#### B. Time domain symbols of LFDMA

For LFDMA, the frequency samples  $\{\tilde{X}_l\}$  after subcarrier mapping can be described as follows:

$$\tilde{X}_l = \begin{cases} X_l, 0 \leq l \leq N-1 \\ 0, N \leq l \leq M-1 \end{cases} \quad \dots (11)$$

Let  $m = Q.n + q$ , where  $0 \leq n \leq N-1$ , and  $0 \leq q \leq Q-1$ .

Then,

$$\begin{aligned} \tilde{x}_m (= \tilde{x}_{Qn+q}) &= \frac{1}{M} \sum_{l=0}^{M-1} \tilde{X}_l e^{j2\pi \frac{m}{M} l} \\ &= \frac{1}{Q} \cdot \frac{1}{N} \sum_{l=0}^{N-1} X_l e^{j2\pi \frac{Qn+q}{QN} l} \quad \dots (12) \end{aligned}$$

If  $q=0$ , then above equation becomes

$$\begin{aligned} \tilde{x}_m &= \frac{1}{Q} \cdot \left( \frac{1}{N} \sum_{l=0}^{N-1} X_l e^{j2\pi \frac{n}{N} l} \right) \quad \dots (13) \\ &= \frac{1}{Q} x_n \end{aligned}$$

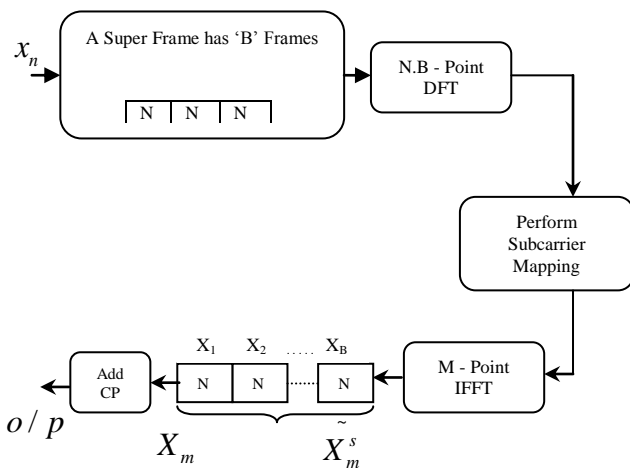
If  $q \neq 0$ , since  $X_l = \sum_{p=0}^{N-1} x_p e^{-j2\pi \frac{p}{N} l}$ , equation (12) can be simplified after derivation, as follows:

$$\tilde{x}_m = \tilde{x}_{Qn+q} = \frac{1}{Q} \left( 1 - e^{j2\pi \frac{q}{Q}} \right) \cdot \frac{1}{N} \sum_{p=0}^{N-1} \frac{x_p}{1 - e^{j2\pi \left\{ \frac{(n-p)}{N} + \frac{q}{Qn} \right\}}} \quad \dots (14)$$

As can be seen from equations (12) and (14), in the time domain, LFDMA signal has exact copies of input time symbols in the  $N$ -multiple sample positions. In-between values are sum of all the time input symbols in the input block with different complex-weighting, which would increase the PAPR. An example of an LFDMA signal is shown in Fig. 3.

**C. Super Frame Scheme with IFDMA**

The figure 4 shows the block diagram of Super frame technique used in SC-FDMA based systems. This technique also reduces PAPR of SC-FDMA signals.



**Fig 4: Structure of the transmitter using SC-OFDM with super frame scheme**

In this scheme B frames with N subcarriers will be combined into one super frame. It reduces the PAPR compared the normal IFDMA. The super frame with lowered PAPR will finally be divided into B OFDM frames for the transmission. The super frame technique (SF-IFDMA) is most suitable for the IFDMA systems with small number of subcarriers N, for example  $N \leq 512$ . This scheme is very effective in reducing the PAPR in IFDMA systems, especially when N is small. It can achieve significant reduction of PAPR without requirement of and side information.

**D. Companding Transform with Kalman Filter (Proposed Scheme)**

A Companding using Kalman filter is an algorithm to reduce the dynamic range of a signal by increasing the amplitudes of the smaller signals. The average signal power is increased with this technique. PAPR is reduced to an extent if dynamic range is reduced. Fig. 1 shows the block diagram of OFDM system with companding scheme to reduce PAPR in OFDM systems.

**a) Companding Transform**

Our aim in this work involves applying  $u$ -law companding at the transmitter to reduce the PAPR of the transmitted waveform so as to reduce distortion through the transmit amplifier and allow operation closer to amplifier saturation. Values of  $u$  ranging between 0.125 and 64 were used in the study since the optimal performance was found to reside within this range of operation.

$$x_c(n) = K(u) x_{\max} \frac{\ln[1 + u \frac{|x_{dat}(n)|}{x_{\max}}]}{\ln[1 + u]} \text{sign}[x_{dat}(n)] \quad \dots (16)$$

Where

$$x_{\max} = \max_n(x_{dat}(n)) \quad \dots (17)$$

And where  $K(u)$  is a normalization constant such that the average power of the companded signal is equal to the average power of the uncompanded signal. A proposed approximation for  $K(u)$  is as follows:

$$K(u) \approx \frac{\ln(1+u)}{u} \quad \dots (18)$$

However, this approximation is not highly accurate, and in practice, would lead to unnecessary degradation in the demodulation performance. To mitigate errors introduced by normalization inaccuracies, numerically-determined values of  $K(u)$  were computed and employed instead, where long-term power averages of both uncompanded and companded OFDM symbols were numerically estimated to find  $K(u)$ .

To reduce the PAPR of an OFDM system a new technique based on companding with Kalman Filter is proposed in this paper. This technique gives the opportunity to keep the PAPR to an adequate level by doing the task of multiple companding which is illustrated by below given steps.

The key signal processing steps are described as follows:

*Step 1:* Binary data is generated and modulation is performed in order to create symbols or vectors  $X_m$ .

*Step 2:* IFFT is performed on vector  $X_m$ , and the output of IFFT is represented in the form as given by equation (19).

$$x = [x(1), x(2), \dots, x(N)]^T \quad \dots (19)$$

*Step 3:* A threshold value of PAPR based on application requirement is set for comparison i.e. for level 4 the value of the threshold is set at

$$PAPR_{th} = 4db$$

*Step 4:* Calculate  $PAPR_1$  and it is compared with  $PAPR_{th}$

Step 5: If,  $PAPR_1 \leq PAPR_{th}$  then the original signal is transmitted i.e.

Transmitted signal,  $t_r(n) = x(n)$

Step 6: A counter is initialized (i.e. a=0) to indicate how many times Companding is performed when,

Transmitted signal,  $t_r(n) = x(n)$

Step 7: If, A Companding transform is then applied to  $x(n)$  by using Kalman Filter i.e.

$$x_1(n) = C\{x(n)\} \quad \dots (20)$$

Step 8: Step 2 & step 4 are repeated for  $x_1(n)$ . Here the calculated PAPR for  $x_1(n)$  is  $PAPR_2$ .

Step 9: If  $PAPR_2 \leq PAPR_{th}$  then,  $t_r(n) = x_1(n)$  and a=1.

Step 10: If,  $PAPR_2 > PAPR_{th}$  Another companding transform is applied to  $x_1(n)$ .

Step 11: This whole procedure is repeated unless  $PAPR_m \leq PAPR_{th}$  Where m=1, 2, 3, . .

#### a) Introduction to Kalman Filter

The Kalman filter is a mathematical tool which consists of a set of mathematical equations; these equations provide an efficient computational means in order to estimate the state of a process, in a way such that the mean of the squared error is minimized. The filter can be used to estimate past, present and even future states. In order to estimate the state  $x \in \mathfrak{R}^n$  of a discrete-time controlled process which is given by the linear stochastic difference equation (21) below:

$$x_k = Ax_{k-1} + Bu_{k-1} + w_{k-1} \quad \dots (21)$$

With a measurement  $z \in \mathfrak{R}^m$  that is given by Eqn. (22)

$$z_k = Hx_k + v_k \quad \dots (22)$$

In practice  $H$  might change with each time step, but here we assume it is constant. The Kalman filter estimates a process with the help of feedback control: the filter estimates the process state at some time and then obtains feedback in the form of measurements.

The equations of Kalman filter are divided into two groups viz: (1) *Time Update* equations and (2) *Measurement Update* equations. The time update equations can also be thought of as *predictor* equations, [16] while the measurement update equations can also be thought of as *corrector* equations. The equations for the time update and measurements update are given below. Kalman filter Time Update Equations as follows:

$$\hat{x}_k = A\hat{x}_{k-1} + Bu_{k-1} \quad \dots (23)$$

$$P_k^- = AP_{k-1}A^T + Q \quad \dots (24)$$

Kalman filter Measurement Update Equations as follows:

$$K_k = P_k^- H^T (HP_k^- H^T + R)^{-1} \quad \dots (25)$$

$$\hat{x}_k = \hat{x}_k + K_k \left( z_k - H \hat{x}_k \right) \quad \dots (26)$$

$$P_k = (I - K_k H) P_k^- \quad \dots (27)$$

## 4. SIMULATION RESULTS

In this section, we present the results of computer simulations used to evaluate PAPR reduction capability. In the simulation, an OFDM system with a sub-carrier of  $N = 128,512$  and QAM modulation was considered. We can evaluate the performance of the PAPR reduction scheme using the complementary cumulative distribution (CCDF) of the PAPR of the OFDM signal.

### a. CCDF Performance

We can evaluate the performance of PAPR using the cumulative distribution of PAPR of OFDM signal. The cumulative distribution function (CDF) is one of the most regularly used parameters, which is used to measure the efficiency of and PAPR technique [15]. The CDF of the amplitude of a signal sample is given by equation (28).

$$F(z) = 1 - \exp(-z) \quad \dots (21)$$

However, the complementary CDF (CCDF) is used instead of CDF, which helps us to measure the probability that the PAPR of a certain data block exceeds the given threshold. The CCDF of the PAPR of the data block is desired in our case to compare outputs of various reduction techniques. This is given by equation (22).

$$P(PAPR > z) = 1 - P(PAPR > z) = 1 - (1 - \exp(-z))^N \quad \dots (22)$$

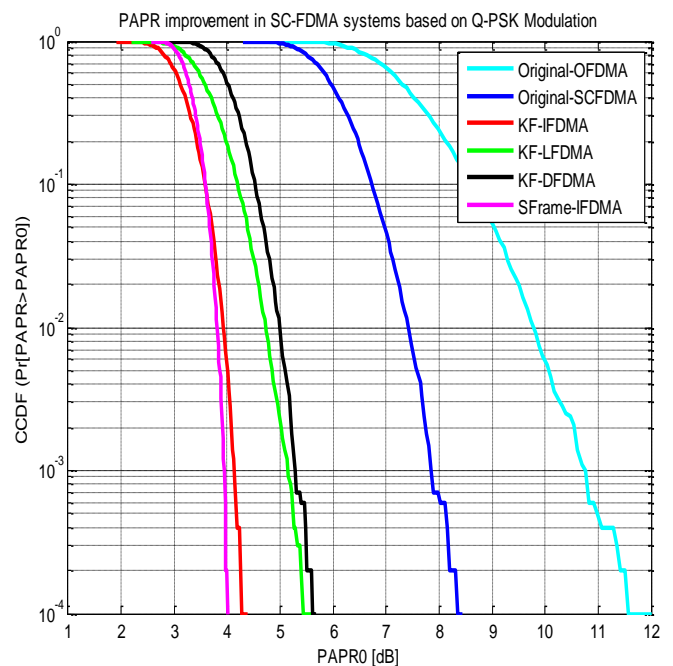
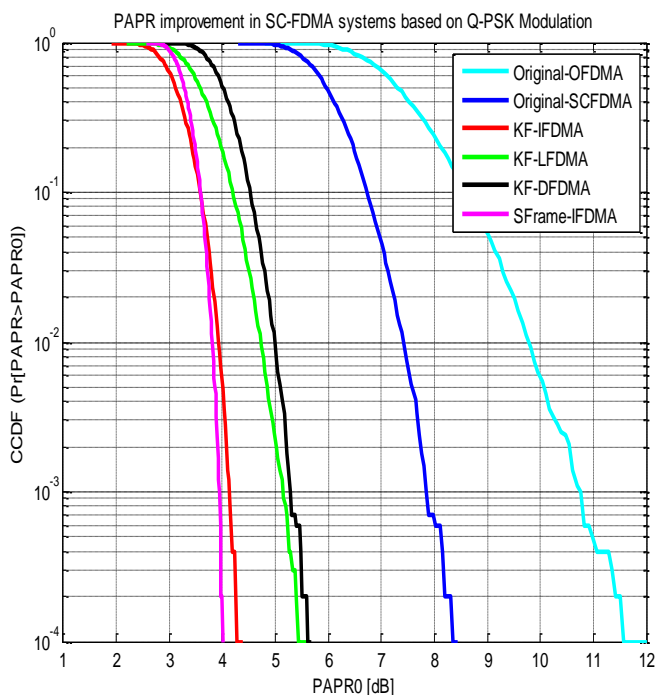
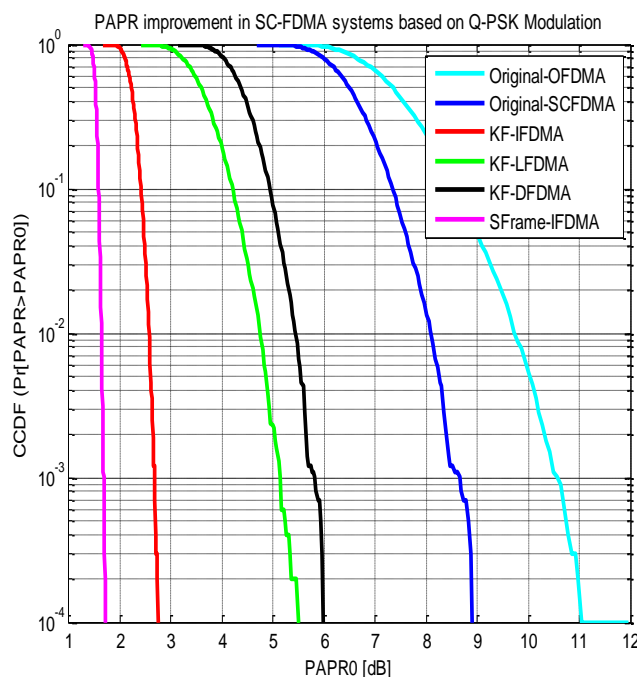


Fig. 5 PAPR PERFORMANCE OF SCFDMA USING Q-PSK AT ROLLOFF FACTOR 0.22



**Fig. 6 PAPR PERFORMANCE OF SCFDMA USING Q-PSK AT ROLLOFF FACTOR 0.42**



**Fig. 7 PAPR PERFORMANCE OF SCFDMA USING Q-PSK AT ROLLOFF FACTOR 0.82**

\*KF-IFDMA- PAPR Reduction in IFDMA systems Using Kalman Filter  
 \*KF-LFDMA- PAPR Reduction in LFDMA systems Using Kalman Filter  
 \*KF-DFDMA- PAPR Reduction in DFDMA systems Using Kalman Filter  
 \*SFrame-IFDMA- PAPR Reduction in Super Frame based IFDMA Using Kalman Filter

The simulation parameters are as follows:

No. of subcarriers: 64, 128 & 512

Modulation scheme: Q-PSK

Channel: AWGN

SNR range: 0 to 20 (in dB)

Total number of Bits transmitted: 64000, 128000 & 512000

Total OFDM symbols: 1000

## 5. CONCLUSION

The proposed scheme introduces an effective implementation of PAPR reduction Single Carrier- Frequency Division Multiple Access based communication systems. Simulation results have shown satisfactory PAPR performance at  $10^{-4}$  CCDF level. The results are shown at different values of roll off factor using Q-PSK modulation scheme. We also analyse behaviour of system under QAM modulation scheme also. Companding based analysis provides some advantages over uncompanding based analysis such as it is more immune to impulse and narrowband noises, also improves spectral efficiency and saving in transmission power. In this paper, a Kalman filter approach is used to improve the PAPR performance of OFDM system. It provides greater efficiency & good BER performance also. From the results shown in figures we observed that there is a very good improvement is found in IFDMA based systems than LFDMA based systems. We also found that Super Frame scheme gives more improved results over normal IFDMA system.

## 6. ACKNOWLEDGMENTS

The authors would like to thank the anonymous reviewers for their constructive comments, which helped improve this paper.

## 7. REFERENCES

- [1] M. M. Rana, Md. Saiful Islam and Abbas Z. Kouzani ,” Peak to Average Power Ratio Analysis for LTE Systems,” 2010 Second International Conference on Communication Software and Networks, pp 516-520.
- [2] Mohamed Noune and Andrew Nix, ” Frequency-Domain Precoding for Single Carrier Frequency-Division Multiple Access,” IEEE Communications Magazine • June 2009, pp 68-74
- [3] Elias Yaacoub and Zaher Dawy ,”A Game Theoretical Formulation for Proportional Fairness in LTE Uplink Scheduling,” IEEE Communications Society subject matter experts for publication in the WCNC 2009.
- [4] GILBERTO BERARDINELLI, LUIS ÁNGEL MAESTRO RUIZ DE TEMIÑO, SIMONE FRATTASI,” OFDMA VS. SC-FDMA: PERFORMANCE COMPARISON IN LOCAL AREA IMT-A SCENARIOS,” IEEE Wireless Communications • October 2008, pp 64-72.
- [5] F. S. Al-kamali · M. I. Dessouky · B. M. Sallam ,” Equalization and Carrier Frequency Offsets Compensation for the SC-FDMA System,” Springer Wireless Pers Commun Sep. 2011.
- [6] F.S. Al-kamali · M.I. Dessouky · B.M. Sallam ,” Impact of the power amplifier on the performance of the single carrier frequency division multiple access system,” Telecommun Syst ,Springer , April 2011.
- [7] Enchang SUN, Pengbo SI, Ruizhe YANG, Yanhua SUN, and Yanhua ZHANG ,” Power function companding

- scheme for peak-to-average power ratio reduction of SC-FDMA signals,” 2011 10th IEEE/ACIS International Conference on Computer and Information Science, 2011.
- [8] Hyung G. Myung, Kyle Jung-Lin Pan, Robert Olesen, and Donald Grieco,” Peak Power Characteristics of Single Carrier FDMA MIMO Precoding System, ©2007 IEEE, pp 477-481.
- [9] Meng Ma, Xiaojing Huang, *Member, IEEE*, Bingli Jiao, *Member, IEEE*, and Y. Jay Guo, *Senior Member, IEEE*,” Optimal Orthogonal Precoding for Power Leakage Suppression in DFT-Based Systems,” IEEE TRANSACTIONS ON COMMUNICATIONS, VOL. 59, NO. 3, MARCH 2011 pp 844-853.
- [10] Gillian Huang, Andrew Nix and Simon Armour,” IMPACT OF RADIO RESOURCE ALLOCATION AND PULSE SHAPING ON PAPR OF SC-FDMA SIGNALS,” The 18th Annual IEEE International Symposium on Personal, Indoor and Mobile Radio Communications (PIMRC'07), ©2007 IEEE.
- [11] Hyung G. Myung Junsung Lim and David J. Goodman,” PEAK-TO-AVERAGE POWER RATIO OF SINGLE CARRIER FDMA SIGNALS WITH PULSE SHAPING,” The 17th Annual IEEE International Symposium on Personal, Indoor and Mobile Radio Communications (PIMRC'06) 2006 IEEE.
- [12] Mohamed Salah , Gamal Abdel-Fadeel, and Zaki B. Nossair ,” Peak to Average Power Ratio Reduction in Single Carrier OFDMA Systems,” ASAT-13 May 2009 pp1-12.
- [13] Md. Mahmudul Hasan “A New PAPR Reduction Technique in OFDM Systems Using Linear Predictive Coding” *Wireless Pers Commun* DOI 10.1007/s11277-013-1387-2, Springer Science+Business Media New York 2013.
- [14] Chunjiang Duanmu · Hongtao Chen ,”Reduction of the PAPR in OFDM Systems by Intelligently Applying Both PTS and SLM Algorithms,” *Wireless Pers Commun*, © Springer Science+Business Media New York 2013.
- [15] Zhongpeng Wang,” Combined DCT and Companding for PAPR Reduction in OFDM Signals,” *Journal of Signal and Information Processing*, 2011 pp 100-104
- [16] Mukunthan Pandurangan and Dananjayan Perumal,” Modified PTS with FECs for PAPR Reduction in MIMO-OFDM System with Different Subblocks and Subcarriers,” *IJCSI International Journal of Computer Science Issues*, Vol. 8, Issue 4, No 2, July 2011 pp 444-452.