

Hybrid Supervised Learning in MLP using Real-coded GA and Back-Propagation

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ABSTRACT

This paper addresses a classification task of pattern recognition by combining effectiveness of evolutionary and gradient descent techniques. We are proposing a hybrid supervised learning approach using real-coded GA and back-propagation to optimize the connection weights of multilayer perceptron. The following learning algorithm overcomes the problems and drawbacks of individual technique by introducing global and local adaptation strategies. The behavior of the proposed algorithm is observed by the experimental results on a couple of popular benchmark datasets. The results of our algorithm are compared with training algorithms based on conventional back-propagation and real-coded genetic algorithm. Finally we realize that proposed hybrid learning algorithm outperforms back-propagation and real-coded genetic algorithm based training the multilayer perceptron.

Keywords: Genetic Algorithms; Multi-layer perceptron; Gradient descent; Generalization

1. INTRODUCTION

Classification is one of the most recurrently encountered decision making tasks of pattern recognition. A classification problem occurs when an object needs to be assigned into a predefined class (group) in decision space based on a number of features (attributes) from feature space [3]. Nowadays, neural networks have recognized by research community as an important tool for classification with immense studies concerning training. Most widely used neural network model for classification is multilayer perceptron (MLP) based on one or more sequentially connected layers of perceptrons. Multilayer perceptron model considered in this paper belongs to the feedforward neural networks. In classification first, the network is trained on a set of paired data to evolve a set of connection weights and second, then the network is ready to test a new set of data [4]. The most popular and widely used training algorithm to estimate the values of the weights is the back-propagation (BP) algorithm [11], follows the principle of gradient descent technique. Because of back-propagation algorithm, multilayer perceptrons are widely employed in many real problems and can approximate any non-linear complex functions with arbitrary accuracy. Despite of its popularity, back-propagation algorithm has drawback of slow error convergence rate and being trapped at local minima. Another technique, global search based optimization algorithms are being used as learning method for feedforward neural networks. Many researchers have introduced evolutionary algorithms to optimize the neural networks weights globally in order to avoid the local minima that so often appear in complex problems. Davis [5] showed how any neural network can be rewritten as a type of genetic algorithm

called a classifier system and vice versa. Whitley [6] attempted successfully to train feedforward neural networks using genetic algorithms. Sexton, Dersey, and Jhonson [7]. Gupta and Sexton [8] compared back-propagation with a genetic algorithm for neural networks training. X. Yao [9] gave new dimension to neural networks. Sankar K. Pal and Dinabandhu Bhandari [10] used binary-coded GA for selection of optimal weights in MLP. Whitley, Darrell, Starkweather, Timothy, and Christopher Bogart [16] hybridized genetic algorithms and neural networks for optimizing connections and connectivity. J. D. Schaffer, Whitley and L. J. Eshelman [19] wrote a survey on combinations of genetic algorithms and neural networks. H. Hasan Örkücü, HasanBal [2] used binary and real coded genetic algorithms for optimization of the connection weights of more than one hidden layers in the MLP. In this paper we have represented all connection weights as real numbers in the genetic algorithms. Genetic algorithms (GAs) based learning is used to find near-optimal solutions globally from search space without computing gradient information. Original genetic algorithms use binary string vector representation similar to the chromosome structure of biology. But binary GA has some disadvantages based learning main objective is to improve accuracy of the network and no consideration is given to the speed of convergence and local error. Here, our focus is to first apply GA leaning and next the gradient descent algorithm in multi-layer perceptron to optimize the best connection weights and minimize local errors with fast convergence. We have found that our approach not only succeeds in its task but it outperforms back-propagation, the standard training algorithm.

The paper is structured as follows: Sections 2 deals an overview of neural networks and genetic algorithms respectively with a special emphasis on their strengths and weaknesses; Section 3 focuses on the detail of proposed algorithm; Section 4 describes empirical evolution of proposed algorithm on 11 real world data sets with their result analysis; Section 5 provides conclusions about our work and suggestions for future work.

2. BACKGROUND STUDY

2.1. Multi-layer perceptron training with back-propagation

Neural networks are used to solve problems in which the complete formulation is unknown i.e. no casual model or mathematical representations exist. It is a massively parallel distributed processor made up of simple processing units, which has a natural propensity for storing experiential knowledge and making it available for use. It is very sophisticated modeling technique capable of modeling extremely complex functions. Neural network are also

referred to in literature as neurocomputers, connectionist networks, parallel distributed processors, etc [12]. Neural networks consist of number of simple processing units called neurons and unidirectional communicational channels called connections (links).

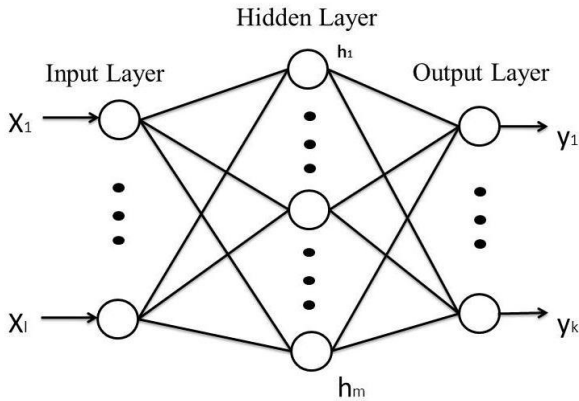


Fig 1: Schematic representation of multilayer perceptron

The figure 1 shows the architecture of feed forward neural network, most common form of it is multi-layer perceptron.

The units are organized in several layers, namely an input layer, one or more hidden layers, and an output layer.

We have used in our experiment, a three layer feedforward neural network with m inputs, k outputs and l hidden neurons. Each neuron of both hidden and output layer uses hyperbolic tangent function $f(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$ as activation function. The output of the hidden node h ($1 \leq h \leq l$) and output node q ($1 \leq q \leq k$) can be expressed as:

$$z_h = f(W^T X) = f(\sum_{i=1}^m (w_i x_i + b_h)), \quad (1)$$

$$o_q = f(V^T Z) = f(\sum_{i=1}^l (v_i z_i + b_q)), \quad (2)$$

respectively, where $W = [w_1, w_2, \dots, w_i, \dots, w_m]^T$ the connection weight vector connects input nodes to hidden node h , $V = [v_1, v_2, \dots, v_i, \dots, v_k]^T$ the connection weight vector connects hidden nodes to output node k , $X = [x_1, x_2, \dots, x_i, \dots, x_m]^T$ the input vector for each hidden node and $Z = [z_1, z_2, \dots, z_i, \dots, z_k]^T$ the input vector for each output node. z_h and o_q are the responses of hidden and output neuron of node h and node q , respectively. b_h and b_q are the biases for hidden node h and output node q respectively. Most commonly used connection weights training algorithm for multi-layer perceptron is back-propagation. The idea of connection weights training in multi-layer perceptron is usually formulated as minimization of an error function, such as mean square error (MSE) between target (d) and actual (o) outputs averaged over all training examples. For a given training set, back-propagation learning may proceed in one of the two basic ways: sequential (on-line or pattern) mode and batch mode. In this paper we used batch learning in the experiment to adjust connection weights after the presentation of all the training examples that constitute an epoch. Thus net mean square error (MSE) function for a given neural network weight vector w is described as $E(w)$; a value which is total sum of error of each neurons of the output layer of all training samples.

$$E(w) = \frac{1}{nk} \sum_{i=1}^n \sum_{j=1}^k (d_{ij} - o_{ij})^2 \quad (3)$$

One method for minimization of error by repeatedly updating the weights of the net in the back propagation algorithm is to apply the principle of gradient descent as:

$$\Delta w_{ji}(n) = -\eta \frac{\partial E(w)}{\partial w_{ji}} = \eta \cdot \delta_j(n) \cdot \text{input}_j(n) \quad (4)$$

where η is a positive number is called learning-rate parameter of the back-propagation algorithm, δ_j the local gradient of a layer j , and n is the number of the iteration in the training. The equation (4) is also called delta rule. The learning-rate η controls the descent. A large value η enables back-propagation to move faster to the target weights by reducing error of the neural network but it may not reach at minimum error of the error curve every time and rather oscillate. To avoid oscillation because of increasing the rate of learning, it is to modify the delta rule the equation (4) by including a momentum term. The following equation is called the generalized delta rule:

$$\Delta w_{ji}(n) = \eta \cdot \delta_j(n) \cdot \text{input}_j(n) + \alpha \cdot \Delta w_{ji}(n-1) \quad (5)$$

Again a term $hdec$ is subtracted from equation (5), $hdec$ is the decay factor $0.01 > hdec > 0$ enables only those weights that help to minimize the error to survive and hence improve the generalization capability of the network.

In addition, another improvement in learning algorithm is stopping rule to control when training ends. It is necessary due to the overfitting (overtraining) phenomenon.

2.2. Real-coded genetic algorithm

Genetic algorithms are randomized search algorithm based on the principle of natural selection and natural genetics. The characteristic of genetic algorithms are population-based evolution, survival of the fittest, directed stochastic, derivative-free. GAs performs the search process in four stages: initialization, selection, crossover, and mutation [13]. GAs has been successfully incorporated in a wide range of applications. GAs are robust, the reasons for this are [14]: 1) GA can solve hard problems quickly and reliably, 2) GAs are easy to interface to existing simulations and models, 3) GAs are extensible and 4) GAs are easy to hybridize. The binary coding representation of chromosomes encounter certain difficulties when dealing with continuous search spaces with large dimensions and a great numerical precision is required [15]. These difficulties are: more computing time for coding and decoding of chromosomes, premature convergence, and hamming cliff problem. Since the performance of binary-coded genetic algorithm for continuous optimization problems are not effective for continuous search space that led towards the use of real-coded genetic algorithm. In real-coded GA the representation of chromosomes are candidate solutions is very close to variables of the problem that means there are no difference between the genotype and the phenotype. The size of chromosome is number of genes that equals to number of variables the objective function have in a problem. In this paper size of chromosome is the total weights of the neural network and the value of genes are same as the value of weights.

2.2.1 Outlines of simple genetic algorithms

A GAs initiates with a population of randomly generated chromosomes. The chromosomes undergo evolution in a form of natural selection, reproduction and mutation. A new population of chromosomes is created using a selection mechanism and particular genetic operators such as crossover and mutation as search mechanism. Using number of

iterations called generations, chromosomes advances toward better solutions by selection of high fitness values in the population and through crossover and mutation. The structure of GAs as follows.

```

Simple_Genetic_Algorithm ()
{
  initialize population;
  evaluate population;
  while (termination_criteria_not_satisfied)
  {
    select parents for mating pool;
    perform crossover;
    perform mutation;
    new generation after crossover and
    mutation;
    Evaluate population;
  }
}

```

Fig 2: Structure of simple genetic algorithms

3. PROPOSED HYBRID SUPERVISED TRAINING ALGORITHM

Traditional back-propagation algorithm adapts gradient information of error function to optimize the connection weights of the neural network but several times it may get stuck to local optimum easily. GAs has good exploration and exploitation characteristics that lead towards near optimal solution in a complex non-linear search space. Hence GA has been extensively used in neural networks weights optimization and is known as successful alternative approach to back-propagation algorithm. Several studies have been used GAs as training algorithm in multilayer perceptron and its performance compared with back-propagation that the former outperforming the latter in most applications. Moreover it is difficult to use binary-coded genetic algorithms for continuous search space with large dimensions and a great numerical precision. To overcome these problems it seems more natural to represent the genes of a chromosome directly as real numbers for applications with variables in continuous domain. Genetic algorithms based on real number representation of chromosomes are called real-coded genetic algorithms. In RGA the size of a chromosome is same as length of the vector which is the solution of the problem but in BGA it is not so [1]. However in RGA proper selection of genetic operators are very important for specific applications. In the present classification problem, the neural networks training using RGA suffers from premature error convergence that is earlier in training using BGA. In this paper an attempt has been taken to propose a hybrid supervised learning algorithm by integrating both real-coded genetic algorithms and back-propagation methods together to alleviate the premature error convergence problem of RGA and to get stuck in local minimum of MLP in the training of multilayer perceptron. In the simulation of the proposed algorithm, it has been observed that hybrid training algorithm outperforms the individual training methods of multilayer perceptron. Figure 2

shows the framework of hybrid real-coded genetic algorithm and back-propagation algorithm.

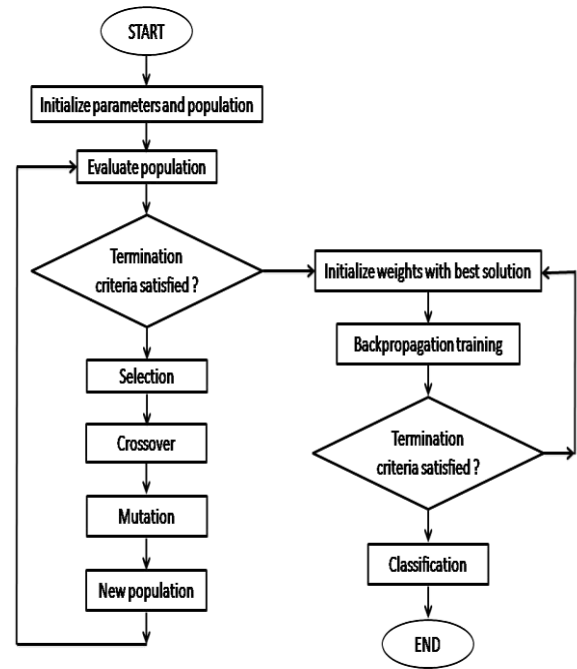


Fig 3: Framework of hybrid algorithm for classification

3.1 Encoding connection weights and initial population

In [1] proposed, number of connection weights in the network are the parameters of a chromosome. For L number of layers, number of parameters is

$$P = \sum_{i=1}^{L-1} p_{i+1}(p_i + 1).$$

Each parameter is represented a real value in a range of (-1, 1). In addition to that more number of chromosomes in the population results in lesser number of generations to be executed for convergence but takes higher processing time for each generation.

3.2 Determine fitness function

Here, the network with more error, the fitness value is less and vice versa, decreasing overall error function F (E) may be represented as increasing function

$$F(E) = \frac{1}{1 + E_{MSE}}$$

Where E_{MSE} is the total mean square error of individual chromosome and a MSE normalization operation applied on that chromosome total MSE, which is its fitness value.

3.3 Fitness scaling or fitness shifting

In order to make GAs work effectively on finite populations, we must modify the way we select individuals for reproduction. The basic idea is to control the number of reproductive opportunities each individual gets, so that it is neither too large, nor too small. One of the ways to control the reproductive opportunity of each individual is fitness scaling or fitness shifting. In this, the maximum number of reproductive trials allocated to an individual is set to a certain value typically 2.0.

3.4 Genetic operators

Genetic operators are the basic search mechanisms of the GA for creating new points based on the existing population. Selection operator performs exploitation of promising candidates in every generation. Reproduction of new points (children) from the selected points (parents) using the two genetic operations: crossover and mutation that leads to exploration of new parts of the search space. Crossover produces two new individuals (children) from two existing individuals (parents), whereas mutation alters one individual to produce a single individual. In this work, arithmetic crossover and non-uniform-mutation function have been used [17] in real-coded genetic algorithms.

3.4.1 Crossover operator

Let us assume that $C_1 = (c_1^1, \dots, c_i^1, \dots, c_n^1)$ and $C_2 = (c_1^2, \dots, c_i^2, \dots, c_n^2)$ are two chromosomes selected for the application of crossover operator. For the arithmetic crossover operator then two offspring, $H_k = (h_1^k, \dots, h_i^k, \dots, h_n^k)$, $k = 1, 2$, are generated, where $h_1^1 = \lambda c_1^1 + (1 - \lambda)c_1^2$ and $h_1^2 = \lambda c_1^2 + (1 - \lambda)c_1^1$. λ is a positive constant and in the experiments, λ is set to 0.28.

3.4.2 Mutation operator

Let us assume the nonuniform mutation operator is applied in a generation r , and g_{max} is the maximum number of generations, new offspring c_i' can obtain as

$$c_i' = \begin{cases} c_i + \Delta(r, b_i - c_i) & \text{if } \tau = 0, \\ c_i + \Delta(r, c_i - a_i) & \text{if } \tau = 1, \end{cases}$$

$$\Delta(r, y) = y (1 - \text{rand}^{(1 - \frac{r}{g_{max}})^b})$$

where τ is a random number either 0 or 1, b is a parameter that determines the degree of dependence on the number of iterations, in our experiments, b is set to 0.5. The random value rand lies in a range $[0, 1]$.

3.5 Proposed algorithm for MLP

- STEP 1.** initialize the RGA parameters
- STEP 2.** initialize the population with real values in the domain for each neuron's connection weights and bias to its correspondent gene segments
- STEP 3.** while new gen. is less than equal to MaxGen. Do {
- STEP 4.** the fitness of a chromosome is determined by MSE
- STEP 5.** sort minimum fitness values
- STEP 6.** if first fitness value is less than equal to min. error then select best solution for MLP then goto step 9
- STEP 7.** select parents for reproduction based on their fitness
- STEP 8.** new population by crossover and mutation
- STEP 9.** goto step 1 for new generation }
- STEP 10.** initialize parameters of back-propagation learning
- STEP 11.** initialize weights of the MLP using best solution of RGA

- STEP 12.** while new epoch is less than equal to MaxEpoch or error converges to Min Error do
- STEP 13.** update weights to minimize error using back-propagation with training data
- STEP 14.** end while
- STEP 15.** evaluate performance of classification with test data
- STEP 16.** end while

4. EXPERIMENTAL STUDY

4.1 Experimental real world datasets

In this section numbers of experiments were conducted with standard datasets. Eleven classification problems were verified in the experiment. In Table 1 lists a summary of the used datasets along with following attributes: problems and the number of instances, the number of binary (b), continuous (c) features in the dataset, number of classes. The classification problems were obtained from the UCI repository [20]. In pattern classification, the total set of patterns in the dataset divided into three different set of partitions forming training, validation and test sets prechelt [17]. A popular and very useful form to use validation set in neural network is early stopping. In this paper the validation set was used for testing the performance of the network in the training phase, it is necessary to avoid the overtraining phenomenon. Here initially the datasets were divided into two segments like sixty and forty percent of data, former was used for training and later for testing sets. Again the training segment divided into two parts like twenty and forty percent of data. The later segment was

used for training and former segment for validation sets. Before partition of the dataset, we were normalized the dataset using z-score or max-min normalization techniques.

The proposed algorithm is compared with back-propagation and real-coded GA based training multilayer perceptron. BP, Real-coded GA based training and proposed one was implemented and analyzed using matlab.

Table 1: Summary of used classification problems

Dataset	Instances	Problem attributes			Class
		b	c	t	
Cancer	683	0	9	9	2
Bupa live	345	0	6	6	2
Diabetes	768	0	8	8	2
Heart	270	0	13	13	2
Hepatitis	155	0	19	19	2
Iris	150	0	4	4	3
Thyroid	215	0	5	5	3
Wine	178	0	13	13	3
Vehicle	846	0	18	18	4
Glass	214	0	9	9	6
Zoo	101	15	2	17	7

4.2 EXPERIMENTAL PREPARATION

1. Patterns were normalized to the range [-1, 1]
2. The real-coded genetic algorithms used real encoding to represent chromosomes
3. Each chromosome in the population represents the neural network architecture
4. The length of the chromosome is the total number of connection of the network
5. Synaptic weights of the neural network are represented by real values in a domain [-1, 1]
6. Population size: 10
7. Linear fitness scaling were used to compress the range of fitness to two
8. Roulette wheel selection or Rank based roulette selection were used in the mating pool
9. Crossover rate: 0.9
10. Arithmetic crossover operator was used
11. Mutation rate: 0.7
12. Non-uniform mutation operator was used
13. Elitism the best chromosomes are preserved for the next generation was used
14. Number of generation for each experiment: 50 to 100
15. The multilayer perceptron had only one hidden layer, number of neurons in this layer was optimized by trial and error method as mentioned in table 2.
16. The transfer function of the hidden layer and output layer are bipolar sigmoid functions
17. The learning rate and momentum parameter of the BP is 0.01 and 0.9
18. Each classifier repeatedly executed ten times for one over all datasets and average accuracy mentioned in Table 2

4.3 EXPERIMENTAL RESULT ANALYSIS

Each training algorithm runs ten times over all datasets mentioned in Table 1 and the average accuracy of the classifier (the percentage of samples that it correctly classified) is computed. The results were obtained for each training technique by the optimization of the connection weights of the multilayer perceptron. The fitness function values (errors)

were normalized and obtained average over total number of training samples. Finally in batch learning mean square error (mse) was obtained that updated the connection weights of the MLP. Moreover the classification rate of the test set obtained in the training of the MLP using different training algorithms, presented in Table 2. Figure 1 to Figure 11 show the graphs comparing the mean square error (mse) and classification rates of the investigated training algorithms over all datasets. The proposed algorithm obtained the best results in the most dataset where RGA based training fails. By taking advantage of global optimization, early stopping, and weight decay proposed algorithm takes less computational time than RGA based training algorithm. Similarly, the problem of local minimum of BP algorithm observed many times in running the training algorithm number of times over all datasets. It leads worst performance in the experiments that could be avoided by proposed algorithm.

From the experiments, it has revealed that by a large crossover rate and a higher mutation rate the proposed algorithm needs small number of generations. Here we used 50 to 100 number of generation with 0.9 crossover and 0.07 mutation rates to train the MLP at initial stage. Then BP algorithm takes small number of epochs to optimize the connection weights of MLP with less mean square error. In RGA based training, maximum generation number was chosen 10000.

It is analyzed from Table 2 that for almost all datasets the classification rate of the proposed training algorithm outperforms classical back-propagation and real-coded GA. But datasets like thyroid, vehicle, glass and zoo the RGA based training obtained poor classification rates even worse than back-propagation algorithm. Thus it is clearly observed from the table that where RGA based training not performed well there proposed training algorithm obtained best results. Moreover in hepatitis dataset RGA based training produced best result than proposed training algorithm. Figure 4 shows the graphs comparing the performances of the investigated training algorithms of multilayer perceptron. The proposed training algorithm obtained best results regarding classification accuracy in percentage except hepatitis dataset. From the results we realized that in the proposed algorithm, initially RGA evolved a better search space globally in few generations then BP locally optimized the connection weights of the neural network.

Table 2: Training results of the multilayer perceptron

Dataset	Input Nodes	Hidden Nodes	Classification Rates (%)			MSE		
			BP	RGA	GA BP	BP	RGA	GA BP
Breast cancer	9	10	97.27	98.21	98.44	0.021	0.024	0.021
Bupa live	6	7	69.69	70.61	70.79	0.054	0.111	0.061
Pima diabetes	8	10	75.25	79.22	79.22	0.067	0.024	0.066
Heart	13	10	82.03	87.40	87.95	0.022	0.024	0.019
Hepatitis	19	5	72.81	88.15	80.29	0.073	0.024	0.019
Iris	4	5	96.99	95.43	97.77	0.028	0.012	0.010
Thyroid	5	8	93.02	78.82	95.34	0.040	0.011	0.037
Wine	13	10	95.39	97.22	98.63	0.077	0.017	0.017
Vehicle	18	6	77.94	55.53	79.70	0.045	0.014	0.046
Glass	9	12	75.51	50.77	77.00	0.037	0.008	0.035
Zoo	17	10	95.14	66.21	95.57	0.027	0.006	0.020

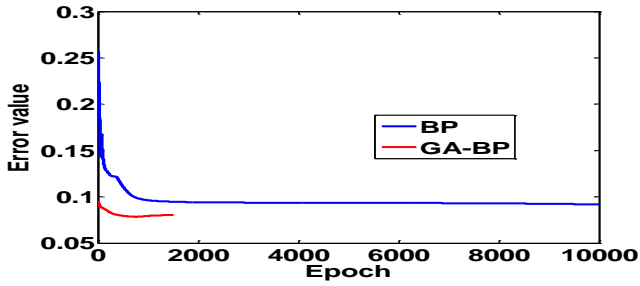


Fig 5: Bupa dataset training performance using BP and GA-BP

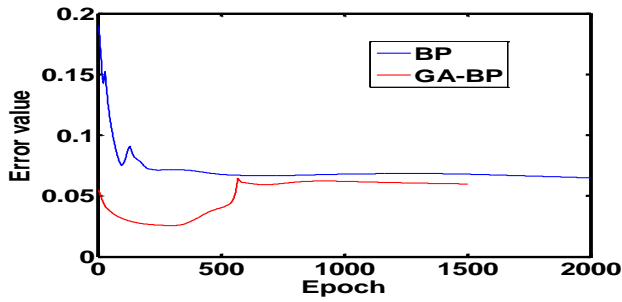
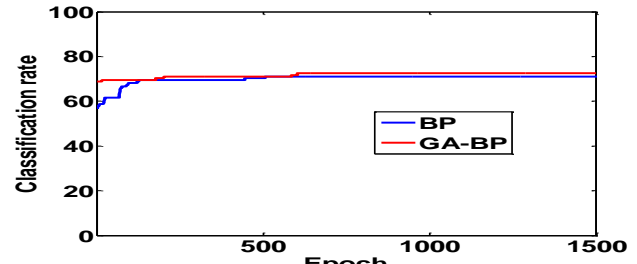


Fig 6: Pima diabetes dataset training performance using BP and GA-BP

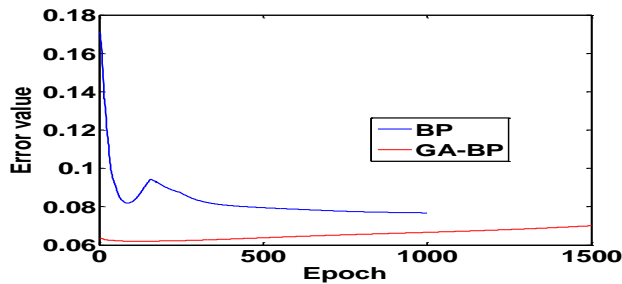
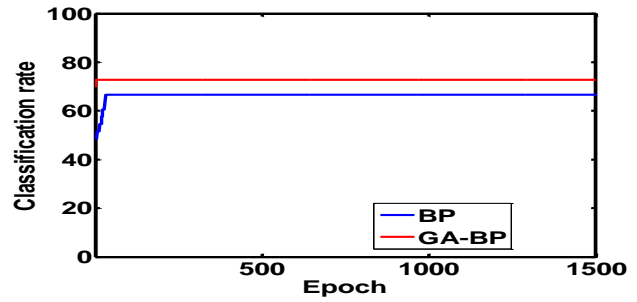


Fig 7: Hepatitis dataset training performance using BP and GA-BP

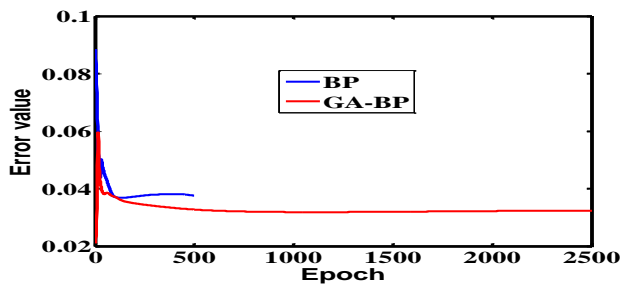
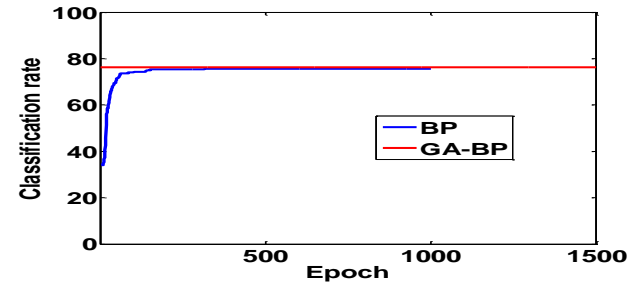


Fig 8: Thyroid dataset training performance using BP and GA-BP

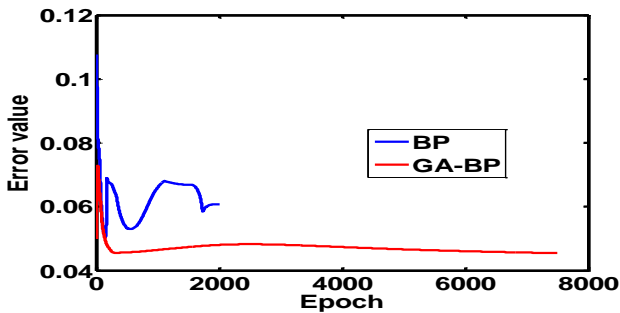
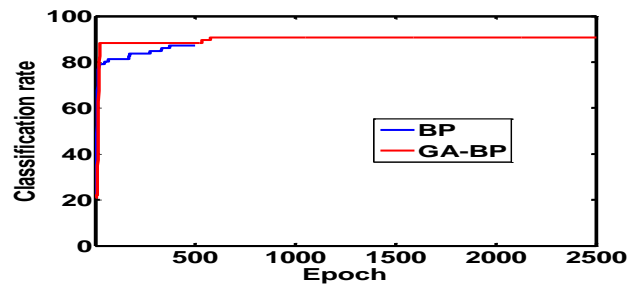
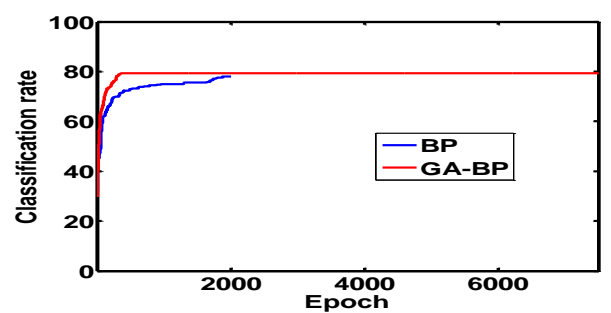


Fig 9: Vehicle dataset training performance using BP and GA-BP



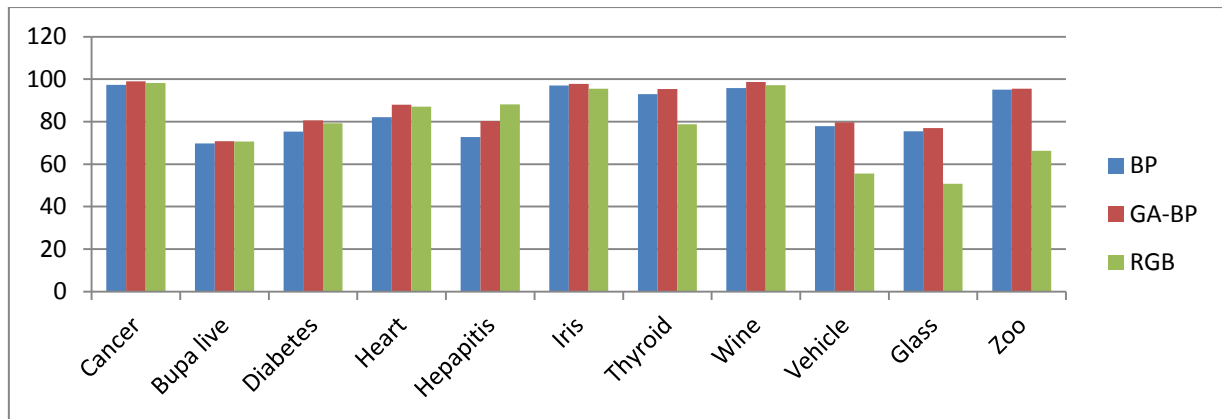


Fig 10: Performances of the investigated training algorithms of MLP

5. CONCLUSION

Feed forward neural networks training using back-propagation, real-coded GA, and proposed hybridization of a real-coded GA and back-propagation algorithms have been discussed in this paper. In the experiment, proposed hybrid training algorithm has been compared with back-propagation and real-coded GA using several real world standard datasets. From experimental results it is cleared that real-coded GA based training algorithm not provides the highest accuracy and generalization results for all datasets. Although RGA produce global optimal solutions, it has shown RGA suffers from premature error convergence in complex problems that can lead to the training failure. Similarly, the back-propagation algorithm has better local searching ability but its performance depends on the input sequence to reach at global optimum solution. Because of that back-propagation algorithm not always performs better and traps in local minima. Again when problems are more complex, back-propagation most often fails because of its inherent gradient decent technique. In case of complex problems, large connection weight parameters of the neural networks increase the size of chromosome. The longer the size of chromosome needs more generations to globally optimize the weights parameters. Hence genetic algorithms are slower in the cost of better performance than where back-propagation fails. To alleviate the problems of premature convergence and more training time of genetic algorithms and getting stuck in local minimum of back-propagation the hybrid algorithms has been adopted in this paper. The simulation of hybrid algorithm starts training with real-coded GA for several generations then uses that global information of RGA solution as initial weights of the neural network to commence the back-propagation algorithm for local convergence of error. The experimental results of the proposed hybrid algorithm improves the training error convergence rate where real-coded GA and back-propagation fail, that leads to better accuracy and generalization. It also revealed that the proposed algorithm outperforms back-propagation and real-coded GA training algorithm without trapping in local minimum. Moreover proposed algorithm takes less training time than real-coded GA based training algorithm. In future this work

will be extended in solving real world problems in image processing, bioinformatics, robotics and business.

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