

# Mining Multiple Level Association Rules to Mining Multiple Level Correlations to Discover Complex Patterns

Mamta  
Shobhit University  
Modipuram, Meerut

Shwetank Arya  
Gurukul Kangri University  
Hardwar

R.P.Agarwal  
Shobhit University  
Modipuram, Meerut

## ABSTRACT

Recently, frequent pattern mining (FPM) has become one of the most popular data mining approaches for various applications such as education, medical, farming, analysis of sale and purchase patterns etc. Apriori algorithm [11] and FP growth algorithm are working efficiently in data mining. These algorithms are typically restricted to a single concept level of hierarchy and uniform support threshold. Sometimes domain database support concept hierarchies that represent the relationships among many different concept levels. In this paper efforts are made to discover items at multiple levels of concept hierarchy. Up till now, a very few concern has been shown to this area. In this study mining multiple levels is explored and extended to mining cross levels in large database on the basis of user specified reduced support threshold constraint.

## General Terms

Identification of complex frequent patterns: from multiple level association rules to cross level association rules.

## Keywords

Complex patterns, multiple level association rules, cross level association rules, IDIV.

## 1. INTRODUCTION

The evolution of Data Mining (DM) technology is related to directly Moore's law. The law states that computer processing power would double in eighteen month intervals. This is precisely what has happened since the 1960s, and the prediction correctly shows where DM technology should be today [14]. Then around in 1980s Gregory Piatetsky Shapiro gave the term Knowledge Discovery in Data (KDD), but the most press liked the term "Data Mining" better [13-14]. Historically, the idea of discovering valuable patterns in data has been given a variety of names, including knowledge discovery, information harvesting, data archeology, data mining and pattern discovery. The phrase knowledge discovery in database was first given at KDD Workshop in 1989 [13] to emphasize that knowledge is the end product of data driven discovery. Data mining is the process of identifying potentially useful, understandable and hidden patterns in large data repository. There are various methods to find frequent complex hidden patterns in large repositories using association rules. Apriori algorithm [11] and FP growth algorithm are working efficiently in data mining. These algorithms typically work for single concept level of hierarchy and uniform support threshold. Since, sometimes business transaction database support concept hierarchies that represent the relationships among many different concept levels. In this study mining multiple levels is explored and extended to mining multiple levels to mining cross levels association rules. Multi level association rules can be mined using concept hierarchies under the support confidence framework.

There are number of variations for using support and confidence framework [1].

- Using predefined uniform minimum support and minimum confidence threshold for all levels.
- Using predefined reduced minimum support and minimum confidence threshold at lower levels.
- Using predefined item or group-based minimum support and minimum confidence threshold.
- Using user specified minimum support and confidence threshold framework.

Top down or bottom up any strategy can be used to mine the association rules. Generally, top down strategy is used, where counts are accumulated for the calculation of frequent item sets, at each concept level, starting at the concept level 1 and working downward in the concept hierarchy toward the more specific concept levels, up till no more frequent item sets can be found. At each level any algorithm can be used such as apriori algorithm using uniform minimum support or reduced minimum support. Uniform minimum support strategy generates many uninteresting patterns. If high minimum support is used at upper level and lower levels also, it generates many uninteresting rules at low levels. If low minimum support is applied at upper levels it avoids generating many interesting rules at higher levels. Therefore, for optimization it is required to use high minimum support at higher level and reduced minimum support at lower levels. This paper focuses on the mining multiple level to cross level mining among item sets.

## 2. REVIEW LITRATURE

The necessity of mining multiple level association rules and using taxonomy information for mining multiple association rules has also been used by many researchers, e.g. [1]. Researchers developed a group of algorithms and conclude that different algorithm may have the best performance for different distribution of data. A major difference between this study and theirs is that in this study correlation coefficient at multiple levels is also calculated and rule interestingness is validated through the correlation coefficient. Another difference is that at the time of making the filtered encoded table user specified support threshold is used. Researchers developed algorithm for mining constrained frequent patterns from uncertain correlated data [6]. In another study a two phases algorithm is developed that discover high utility item sets from large database [7]. In a study multi level hierarchical information encoded technique and frequent pattern mining method is used to provide users with experienced learning suggestions [8]. In a study apriory algorithm is used to find multi level association rules to increase the sale and profit [9]. In another study the problem of mining multiple level frequent item set is introduced and algorithm are proposed,

compared, validated through experiments and assessed on some parameters such as database and support [10]. Another study is done towards the combination of data mining and various statistical techniques such as chi square, regression analysis and hypothesis testing to provide some control to minimize the risk of discovering uninteresting rules and patterns [12].

In all existed studies multiple level association rules are discovered but in this present paper multiple level association rules are explored and extended to multiple level correlation rules to affirm the results discovered from multiple level association rules. Identification of multiple levels and cross level relationships among items plays an important role in discovering the answer of complex queries and making right decisions. Present study uses the example related to the stationary items. In this paper a method, based on association rules, is developed and discussed to identify multilevel and cross level relationship. Besides the investigation of several optimization methods, some interesting techniques for filtering uninteresting rules are also studied.

1. User is asked to input the support threshold at initial step to build the filtered encoded table.
2. User specified support threshold is used at level 1 and level+1 to discover the rules.

### 3. PROPOSED WORK

Concept hierarchy of items is used and numbered from level 0 to level + 1. Transaction T contains the items belonging to the terminal level. Level 0 is root/parent node and level + 1 is child node. Coding technique was proposed in [1] is used. For instance, in fig 1 the item pen is assigned code 1\*\*, since it belongs to level 1, the ball pen is assigned code 11\* and the Reynolds is assigned code 111, which provide the exact identification about the location of Reynolds ball pen in the concept hierarchy.

The problem of mining multiple level association rules, to discover the association rules consisting items belonging to the different levels of abstraction, meeting the minimum user specified support and confidence threshold, is extended to discover multi level correlation rules to affirm the mined results with statistical techniques. In this study user specified strategy is used in mining each level of abstraction. At initial level filtered encoded tables [Table 2, 3, 4] are made according to user specified support factor. The codes shown in strikethrough style are codes having the less support threshold from the user specified support threshold. At each level user specified support threshold is used to avoid the uninteresting rules. In this study user is asked to provide following inputs to enforce the constraint on the mining process:

Enter choice of strategy:

- Minimum support and confidence threshold to filter items from encoded transaction table
- Minimum support and confidence threshold at each level.

To explain the task an abstract example is taken, discussed and analyzed, which is the simulation of real life example.

**Example:** Find multiple levels and cross level association rules and correlation in the transaction repository table 1 for purchase patterns related to stationary items.

### 3.1 Mining multiple level association rules

Table 1 contain transaction\_id and item purchased. Three days example data is used to discover valuable patterns. Each tuple in the table is a unique item set purchased in a day. Taxonomical information is provided in fig 1 representing items at each level from root node to terminal node. Associations are discovered using the algorithm [Fig 2].

### 3.2 Algorithm to discover association rules

Input information:

- (i) A hierarchical-information encoded table task related data in the form of Transaction-id (TID) and Item sets (Items). (Each item in the item sets contains encoded concept hierarchical information).
- (ii) User specified minimum support for each concept level.

Begin

```

{
  Find unique item set and corresponding support factor and store them in a table2, table3 and table4.
  do(frequent one item sets)
  {
    for level 1 use code level 1 and wildcard (1**), with support and store in table 5.
    for level2 use code of level 1&code of level 2 with wildcard(11*)with support store in table8.
    for level 3 use complete code such as 111. store in table 11.
  }
  while table is not empty
  do(frequent 2 item sets for level 2)
  {
    Find two items from table 8 ,itemi,itemi+1,itemi+2 and corresponding support. If support >= user specified support store in table 9.
  }
  do(frequent 3 items from table 9)
  {
    Find three items and corresponding support store in table 10
  }
  do(frequent 2 item sets for level 3)
  {
    Find two items from table 11 and corresponding support, store in table 12
  }
  do(frequent 3 items sets for level3)
  {
    Find three items from table12 and corresponding support, store in table 13
  }
}
    
```

**Fig 2. Algorithm to discover association rules at multiple levels.**

Table 1 indicates the items purchased in three consecutive days. Item are encoded by using the technique [1]. Filtered encoded table is built by removing the items having less support threshold from the user specified support threshold. In this example it is assumed that the user specified support threshold is 1 % ( 3 transaction out of 30 transaction). The items having the less than 1 support per day are removed from the filtered table. Strikethrough style is used to represent the removed items [table 2, 3 and 4]. Table 5 is built which indicates the level 1 frequent one item sets using the support threshold 20%. Total transactions used are 30 and items having the minimum 6 support threshold are considered for the frequent one item sets at level 1. Table 6 indicates the level 1 frequent two item sets with support threshold 20%. Similarly table 7 indicates the level 1 frequent three item sets with support threshold 20%. For level 2 minimum support thresholds is assumed as 10%. Table 8 indicate the level 2 frequent one item sets and table 9 and table 10 indicate the frequent two and frequent three item sets at level 2. Table 11, 12 and 13 indicate the frequent one, two and three item sets at level 3 with minimum support threshold.

### 3.2 Mining Multilevel Correlation Coefficient

Data mining technique is data driven technique, it would beneficial to affirm the mined rules with statistical methodology to obtain more reliable results. Coefficient of correlation is one of the most widely used statistical measures to measure the strength of linear relationships in two or more variables. Of the several mathematical methods of measuring correlation, the Karl Pearson’s method is most widely used in practice. The coefficient of correlation is denoted by  $r$ . The value of the coefficient of correlation as obtained by its formula shall always lie between  $\pm 1$ . When  $r=+1$  it means there is perfect positive correlation between variables and  $r= -1$  it means there is perfect negative correlation between variables. When  $r = 0$  it means there is no correlation between variables. However, in practice  $r = +1, -1$  and  $0$  are rare. Values normally lie between  $+1$  and  $-1$ . The coefficient of correlation describes not only the magnitude of correlation but also the direction of correlation.

Table 14 indicates the correlation between items at level 1, table 15 shows the correlation between items at level 2 and table 16 indicates the correlation between items at level 3. Table 17 shows the correlation between cross level items. At level 1 item code 2\*\* and item code 4\*\* has .50 correlation which indicate positive correlation. The percentage of support is 43, means 43% times 2\*\* and 4\*\* items are purchased together. Item code 3\*\* and item code 4\*\* has .36 correlation which indicate positive correlation and magnitude is .36, if the sale of one item is increased the sale of other item will also be increased. Support percentage of 3\*\* and 4\*\* codes is 36, indicates that the sale of 3\*\* and 4\*\* both are purchased together 36 times out of 100 transactions. Item code 1\*\* and item code 4\*\* has .53 correlation which is also positive and indicate if the sale of 2\*\* item is rise consequently the sale of 3\*\* item also be rise.

### 3.3 Mining Cross level Association Rules and Correlation Coefficient

Cross level association rules refers association of one item to another item belongs to different category and level such as item coded as 1\*\* (pen) and item coded as 43\*(notebook) [Figure 1]. Table 17 shows the cross level correlation coefficient of code 1\*\* and code 43\* that Is -0.44 and support threshold of code item 1\*\* and 43\* is 43.33%. The validity of association rule is also affirmed by the correlation coefficient. Correlation coefficient also indicates that there is negative correlation in these two cross level rules.

**Table 1. Sales of Stationary items**

DAY	TID	Item Purchased
1	T1	Ball Pen, Simple Notebook, calculator
2	.....	.....
3	.....	.....

**Table 2. Filtered Encoded Transaction (Day1)Minimum support 1%**

TID	Items Purchased
T1	111, 431,321,131,432
T2	111,431,321,131,432
T3	111,431,321
T4	111,431,321
T5	111,431,321,221
T6	221,412,222
T7	221,412, <del>311</del>
T8	221,412, <del>231</del>
T9	221,412
T10	221,412, <del>421</del> ,321

**Table 3. Filtered Encoded Transaction (Day2) Minimum support 1%**

TID	Items Purchased
T1	111,131
T2	111,131
T3	111,431,321
T4	131,432, <del>312</del>
T5	131,432,221
T6	221,412
T7	221,412
T8	131,432,321
T9	221,412, <del>112</del>
T10	221,412

**Table 4. Filtered Encoded Transaction (Day3)Minimum support 1%**

TID	Items Purchased
T1	111,131,432
T2	111,321,431
T3	111,431,321
T4	131,432, <del>311</del>
T5	131,432
T6	221,412
T7	221,412
T8	131,432,321
T9	221,412, <del>212</del>
T10	221,412,111

**Table 5. Level 1 Frequent 1 Item set (Minimum Support 20%)**

Items	Support (%)
1**	60
2**	50
3**	36
4**	93

**Table 6. Level 1 Frequent 2 Item sets (Minimum Support 20%)**

Items sets	Support (%)
1**, 3**	33
1**, 4**	53
2**, 4**	50
3**, 4**	36

**Table 7. Level 1 Frequent 3 Item sets (Minimum Support 20%)**

Item sets	Support (%)
1**,3**,4**	36

**Table 8. Level 2 Frequent 1 Item sets (Minimum Support 10%)**

Item sets	Support (%)
11*	40
13*	36
22*	50
32*	33
41*	43
43*	50

**Table 9. Level 2 Frequent 2 Item sets (Minimum Support 10%)**

Item sets	Support (%)
11*, 43*	30
11*,32*	23
22*,41	43
32*,43*	30
13*,43*	20
11*,13*	16

**Table 10. Level 2 Frequent 3 Item sets (Minimum Support 10%)**

Item sets	Support (%)
11*, 43*,32*	26

**Table 11. Level 3 Frequent 1 Item sets (Minimum Support 6%)**

Item sets	Support (%)
111	40
431	26
321	36
221	50
131	36
412	43

**Table 12. Level 3 Frequent 2 Item sets (Minimum Support 6%)**

Item sets	Support (%)
111,431	26
111,321	26
321,431	26
221,412	43

**Table 13. Level 3 Frequent 3 Item sets (Minimum Support 6%)**

Item sets	Support (%)
111,431,321	23

**Table 14. Level 1, frequent two items sets Correlation Coefficient**

Item set	Item set	Correlation
1**	2**	-0.70
1**	3**	-.89
1**	4**	-0.70
2**	3**	0.63

2**	4**	0.5
3**	4**	.94

**Table 15. Level 2, frequent two items sets Correlation Coefficient)**

Item set	Item set	Correlation
11*	43*	.94
11*	32*	.89
22*	41*	0

**Table 16. Level 3, frequent two items sets Correlation Coefficient**

Item set	Item set	Correlation
111	431	.89
131	432	.63
221	412	.70

**Table 17. Cross Level Correlation Coefficient**

Item set	Item set	Correlation
1**	43*	-.44

#### 4. CONCLUSION

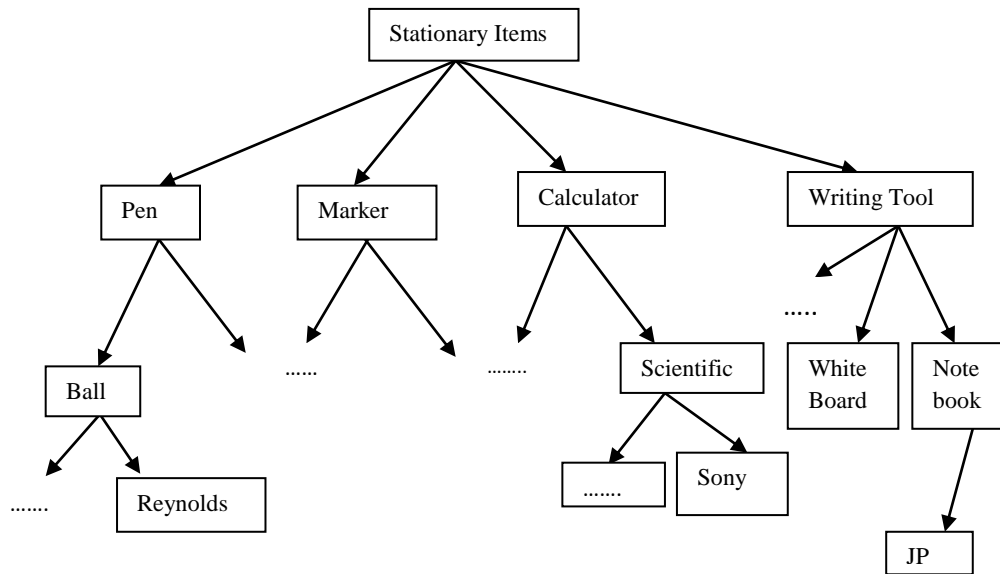
This study extended the scope of the study of mining association rules from single level to multiple level association rules, from uniform support framework to reduced support framework and also from mining multiple level association rules to mining multiple level correlation coefficients from large transaction database. Methods of mining cross level association rules and cross level correlation coefficient are also studied to validate the results. Study shows that mining multiple level correlations validate the results discovered from mining multiple level association rules and mining cross level association rules. Mining multiple level association allow to mine interesting patterns when data is available at multiple level of abstraction, which has been a common practice nowadays and discovering correlation rules at multiple levels not only affirm the resulting patterns but also indicate the positive or negative relationships in two variables. In this paper for the purpose of simplicity an abstract example similar to real life example is used. More concrete and generalized results can be obtained through the sample of real data which will be studied in our future work.

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**Fig 1. Concept hierarchy of stationary items.**