

Development and Performance Evaluation of Mismatched Filter using Differential Evolution

J. B. Seventline¹, G. V. K. Sharma², K. Sridevi³, D. Elizabeth Rani⁴, K. Raja Rajeswari⁵

^{1,2&3} Dept. of ECE, GITAM Institute of Technology, GITAM University, Visakhapatnam, A.P., INDIA.

⁴Dept. of EIE, GITAM Institute of Technology, GITAM University, Visakhapatnam, A.P., INDIA.

⁵ Dept. of ECE, College of Engineering, Andhra University, Visakhapatnam, A.P., INDIA

ABSTRACT

Pulse compression is a technique that plays an important role in various fields like radar, sonar and spread spectrum communication to achieve the high transmit energy of a long pulse while preserving the range resolution of a short pulse. In this paper a new method of design of mismatched filter to minimize the Peak sidelobe ratio (PSLR) in the pulse compressed waveform is discussed. The method used here is the differential evolution optimization technique. The performance of the filter is studied with different codes like binary barker and chaotic codes. Results show that significant reduction in Peak sidelobe ratio is obtained at the output of the mismatched filter.

Keywords

Pulse Compression, Autocorrelation, Peak sidelobe ratio, Differential evolution, Mismatched filter.

1. INTRODUCTION

In radar pulse compression technique when a target echo signal passes a matched filter, the filter output consists of a main lobe and several sidelobes [1,2]. These sidelobes can cause false alarms or mask the main lobe of weak target echo signals at neighboring range cells. The peak sidelobe is simply the largest sidelobe in the output of the matched filter. Thus the ratio of the peak sidelobe to main peak in dB (PSLR) should be as low as possible so that unwanted clutter gets suppressed. The design of radar filters to suppress the range sidelobes has been a subject of considerable interest in which lot of research work has been reported.

The least squares inverse filter design of mismatched filter was first proposed by Ackroyd and Ghani. Here, the sum of squared magnitude of the difference between the inverse filter outputs and ideal one is minimized [3]. Zoraster has developed a mismatched filter using linear programming techniques [4]. Here, the filter weights are designed in an optimized manner so that the main lobe amplitude is maximized and sidelobe amplitude is minimized. For mismatched filter design, Baden and Cohen used iteratively reweighted least squares to minimize PSLR. When mismatched filtering is used, the main peak will not be as large as it would have been with matched filtering. This loss is referred to as the *loss in processing gain*, or *LPG*. LPG is expressed in decibels as the ratio of the mismatched peak to the matched peak [5]. Neural networks using back propagation algorithm developed have also been used for side lobe reduction [6].

Recently Nunn [7] has suggested that the signal/filter optimization should start from a signal whose own autocorrelation function already exhibits low peak or integrated sidelobes. Based on his work, Levanon has developed longer mismatched filters using optimization

techniques for minimum integrated or peak sidelobes [8]. In his work, the design of a mismatched filter using least squares method to optimize Integrated Side lobe ratio (ISLR) and design of filter using the matlab function *fmincon* to optimize the Peak sidelobe ratio has been explained. The performance of the filter is studied by cross correlating different binary codes like barker codes and long binary codes like MSL codes and binary chaotic codes with the optimized filter coefficients.

In this paper a new method of the design of mismatched filter using differential evolution is discussed and its performance study by cross correlating different codes like binary barker code and chaotic codes has been presented. The generation of binary and ternary chaotic codes is done using chaotic maps and has been reported in the previous literature [9, 10].

2. CLASSICAL DIFFERENTIAL EVOLUTION

The differential evolution algorithm (DE) algorithm is a stochastic parallel direct search optimization method that is fast and reasonably robust and it was first proposed by Price and Storn in 1995 [11, 12]. The algorithm became quite popular because of easy methods of implementation and negligible parameter tuning [18]. It is used to solve problems in various fields such as control and synchronization of chaotic systems [13], parameter identification [14] and others because of its consistent and reliable performance in nonlinear optimization applications. The differential evolution combined with chaotic sequences has also been used to solve the image enhancement problem [15]. The algorithm was named DE due to a special kind of differential operator, which was used to create new offspring from parent chromosomes instead of classical crossover or mutation. Based on the individual being perturbed, the number of individuals used in the mutation process and the type of crossover used, 10 different strategies for DE was proposed by Price and Storn. In each strategy trial vectors are generated by adding the weighted difference between other randomly selected members of the population. DE/a/b/c is the general convention used above. DE represents differential evolution, a stands for a string denoting the vector to be perturbed, b is the number of difference vectors considered for perturbation of a, and c represents the type of crossover being used (exp: exponential, bin: binomial). The scheme implemented in this work is the DE/rand/1/bin, meaning that the target vector is randomly selected, and only one difference vector is used. The recombination is controlled by a binomial decision rule which is indicated by the bin acronym. The optimization procedure of DE/rand/1/bin is given by the following steps and procedures [15], [18].

DE also starts with a population of L , d dimensional search variable vectors or parameters like any other evolutionary

algorithm. The successive generations in DE is represented by discrete time steps like $n = 0, 1, 2, \dots, n, n + 1$, etc. The following notation for representing the i_{th} vector or individual of the population at the current generation (i.e., at time $n=n$) is used since the vectors are likely to be changed over different generations

$$x_i(n) = [x_{i,1}(n), x_{i,2}(n), \dots, x_{i,d}(n)] \quad (1.1)$$

These vectors are also often called as genes or chromosomes.

Step 1: Initialization of the variable vectors

Initially consider $n = 0$. The problem parameters or independent variables are initialized somewhere in their feasible numerical range because there may be a certain range within which value of parameter should lie for better search results for each search variable. Therefore the j_{th} component of the i_{th} population members may be initialized as

$$x_{i,j}(0) = x_j^M + (rand(0,1))(x_j^V - x_j^M) \quad (1.2)$$

where the lower and upper bound of the j_{th} parameter of the given problem is represented as x_j^M and x_j^V respectively and $rand(0,1)$ generally exists between 0 and 1 which is a uniformly distributed random number. Then the fitness value or objective function of each individual is evaluated.

Step 2: The mutation operation

An operation that adds a uniform random variable to one or more vector parameters is generally referred as mutation. The DE relies upon the population itself to supply increments of the appropriate magnitude and orientation. In every iteration of the algorithm or each generation a donor vector $v_i(n)$ is created, to change each population member $x_i(n)$. The method of creating this donor vector, varies between the various DE schemes. In this work a specific mutation strategy is used which is explained here. Three other parameter vectors (say the k_1, k_2 and k_3 th vectors ($k_1 \neq k_2 \neq k_3$)) are chosen in a random fashion from the current population. After that a scalar number f_d scales the difference of any two of the three vectors and the scaled difference is added to the third one to obtain the donor vector $v_i(n)$. Thus the evaluation for the j th component of each vector is expressed as

$$v_{i,j}(n+1) = x_{k_1,j}(n) + f_d(x_{k_2,j}(n) - x_{k_3,j}(n)) \quad (1.3)$$

Step 3: The crossover operation

Crossover is applied in the population following the mutation operation. There are two types of crossover called binomial crossover and exponential crossover. In binomial crossover which is used in this work, for each mutant vector, $v_i(n+1)$

trial vector is generated with

$$z_i(n+1) = [z_{i,1}(n+1), z_{i,2}(n+1), \dots, z_{i,d}(n+1)]$$

$$z_{i,j}(n+1) = v_{i,j}(n+1) \quad \text{if } randb(j) < CR \\ = x_{i,j}(n) \quad \text{otherwise} \quad (1.4)$$

where $z_{i,j}(n)$ stands for the j th component of the i_{th} individual or real-valued vector after crossover operation, $randb(j)$ is the j_{th} evaluation of a uniform random number generation in the range $[0, 1]$, CR is the crossover rate in the range $[0, 1]$.

Step 4: Selection operation

To determine which one of the target vector $x_i(n)$ and the trial vector $z_i(n+1)$ will survive in the next generation, DE actually involves the Darwinian principle of ‘‘Survival of the fittest’’ in its selection process. So the next step of the algorithm is ‘‘selection’’ and this step ensures that the population size is constant over subsequent generations. Thus, to decide whether or not the vector $z_i(n+1)$ should be a member of the population comprising the next generation, it is compared to the corresponding vector $x_i(n)$. Thus, if $F()$ denotes the objective function, then

$$x_i(n+1) = z_i(n+1) \quad \text{if } F(z_i(n+1)) \geq F(x_i(n)) \\ = x_i(n) \quad \text{otherwise} \quad (1.5)$$

Step 5: The stopping criterion

The generation number is increased to $n = n + 1$ and then we need to proceed to step 3 until a stopping criterion is met, usually a maximum number of iterations or generations, n_{max} .

3. PROBLEM FORMULATION

The design of mismatched filter using particle swarm optimization technique has been reported earlier [17]. The same procedure is adopted here, to find the optimum weights of a mismatched filter using the differential evolution algorithm so that the sidelobe levels in the filter output are reduced.

Phase coded pulse compression, is often used to increase range resolution and accuracy when energy requirements dictate a pulse length substantially in excess of the desired resolution in pulsed radar system. Codes or sequences refer to the phase of the carrier in phase coded pulse compression. Consider a binary or ternary sequence given by

$$S = \{s_0, s_1, \dots, s_{N-1}\} \quad (1.6)$$

where N is the number of samples of the sequence. The binary sequence has alphabets ± 1 where as the ternary sequence has alphabets $\pm 1, 0$. The output of the matched filter without Doppler shift which is nothing but the aperiodic autocorrelation function for positive delays is defined in equation (1.7)

$$r(k) = \sum_{i=0}^{N-1-k} s_i s_{i+k} \quad \text{for } k = 0, 1, \dots, N-1 \quad (1.7)$$

The filter elements or weights of the mismatched filter are considered as

$$H = \{h_0, h_1, \dots, h_{M-1}\} \quad (1.8)$$

where the weights are real and $M (\geq N)$ indicates the filter length. For mathematical convenience M will be assumed to be even if N is even and odd if N is odd. The filter output is not necessarily symmetric. The output of the mismatched filter [17] is given as

$$G_k = \sum_{i=0}^{M-1} h_i s_{i-k} \quad \text{for } -(N-1) \leq k \leq (M-1) \quad (1.9)$$

Here we assume $s_i = 0$ if $i < 0$ or $i > N - 1$. The constraint function is defined as

$$\begin{aligned} \text{Maximise } F &= G_{k=\frac{M-N}{2}} = \sum_{i=0}^{M-1} h_i s_{i-M-N/2} \\ \text{Subject to } \left| G_{k \neq \frac{M-N}{2}} \right| &= \left| \sum_{i=0}^{M-1} h_i s_{i-k} \right| \leq 1 \\ &\text{for } -(N-1) \leq k \leq (M-1), k \neq M-N/2. \end{aligned} \quad (1.10)$$

The main lobe level which has to be maximized is referred to as F. The inequality condition restricts all side-lobes to be less than and equal to one in absolute value which is given by 1.10. The Peak sidelobe ratio which is generally referred as PSLR of the mismatched filter output is defined in equation (1.11). In this equation the maximum value of the filter output or main lobe level which occurs at $k=M-N/2$ is compared with maximum of the absolute value of the filter outputs at $k \neq M-N/2$ which are considered as the peak sidelobe levels. By considering this constraint function the PSLR optimized filter or filter with reduced sidelobe levels is obtained

$$PSLR = 20 \log \frac{\max |G_{k \neq M-N/2}|}{G_{k=\frac{M-N}{2}}} \quad (1.11)$$

Here the individuals or variable vectors are chosen as mismatched filter impulse response coefficients or elements. The mutation factor f_d is chosen as 0.5 and the crossover rate (CR) is chosen as 0.3. The initial population of search variable vectors is chosen according to step 2. It is well known that the matched filter weights are the sequence itself which may be +1,-1 or zero. The mismatched filter weights are chosen to have a slight deviation from the zero padded matched filter's response which is of the form $H_0=[Z S Z]$ where Z is a all zero sequence of length $z=M-N/2$. So if the length of the sequence (N) is 13, and the filter length(M) is 39, z is 13. When the filter is designed in this fashion, the peak of the filter output occurs at $k=M-N/2$. For convenience, the filter length is considered as three times the length of the sequence. The population size and the number of iterations are varied with the length of the code.

4. SIMULATION RESULTS

The simulation is done using Matlab and the performance of the PSLR optimized mismatched filter is studied for different codes like barker code, chaotic binary code and chaotic

ternary codes of varying lengths. The PSLR obtained using equation(1.11) is shown in Table 1.1 and 1.2.

The well known matched filter response of Barker 13 has an PSLR of -22.289 dB but with the PSLR optimized filter lower PSLR is observed. The mismatched filter output from $k=-12$ to $k=38$ is plotted in Fig.1.1. As observed from the figure the peak of the filter output occurs at $k=13$. The matched filter output is not symmetric about $k=M-N/2$. The filter exhibits a LPG loss of -0.033dB and the PSLR obtained is -35.35 dB. The deviation of the mismatched filter weights from the matched filter weights are plotted in Fig.1.2. The population size chosen is 20 and the number of iterations is 200. Fig.1.3 indicates the mismatched filter output with a ternary chaotic code of length 21. The PSLR with matched filter was -22.3 dB. With mismatched filter PSLR as low as -26.17 dB is obtained as observed from the plot. But the LPG is -0.0361dB. The population size is 50 and the number of iterations is 200.

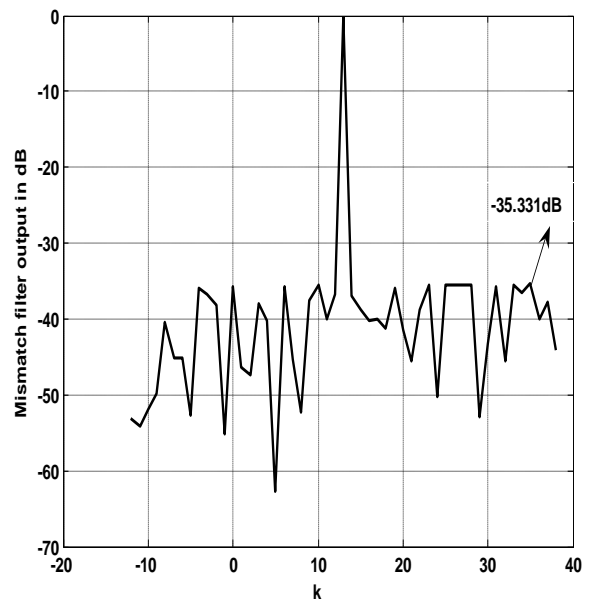


Fig 1.1 Mismatched filter output for Barker code

Table 1.1
PSLR of Barker code and chaotic binary code

Code	Length of the code	PSLR in dB (From matched filter output)	PSLR in dB (From mismatched filter output)	LPG in dB
Barker13	13	-22.9	-35.3551	-0.0333
Chaotic binary code	25	-18.4164	-20.4688	-0.0838

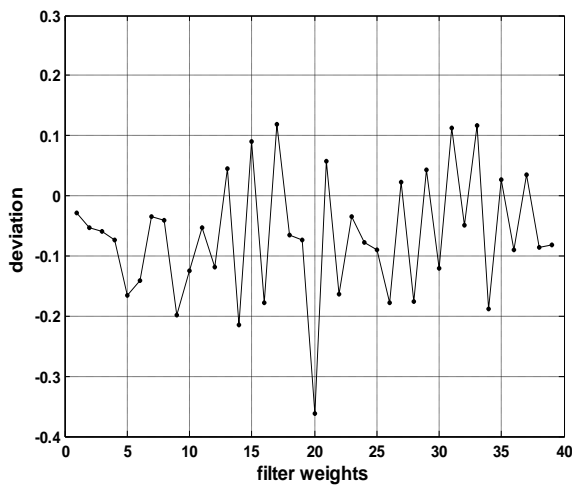


Fig.1.2 The mismatched filter elements deviation from Barker 13 signal values

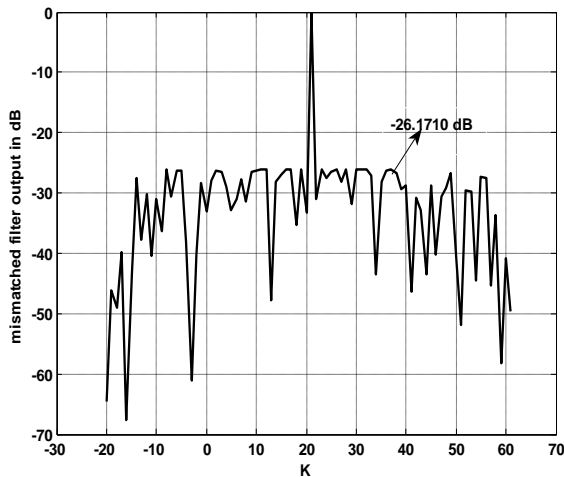


Fig 1.3. Mismatched filter output for ternary chaotic code of length 21

filter. The significant improvement in PSLR is observed from the table. To understand the reduction in PSLR very clearly, a plot of PSLR obtained with matched filter and with mismatched filter for ternary chaotic codes is also plotted in Fig 1.4

Table 1.2
PSLR of ternary chaotic codes from matched filter and mismatched filter

Length of sequence	PSLR in dB (From matched filter o/p)	PSLR in dB (From mismatched filter o/p)	LPG in dB
13	-20	-23.8495	-0.323
15	-20.8279	-24.7694	-0.082
17	-20.8279	-24.0853	-0.064
21	-22.9	-26.1710	-0.036
25	-20	-25.0926	-0.140
27	-20.4238	-26.7177	-0.998
29	-20.4238	-25.5605	-0.067
33	-18.7570	-24.2012	-0.117
35	-19.4007	-26.6595	-0.393
40	-20.2848	-24.3631	-0.398
50	-19.5545	-22.0725	-0.169

Table 1.2 shows the comparison of PSLR of the ternary chaotic codes obtained from the autocorrelation function output of matched filter reported earlier [10] and mismatched

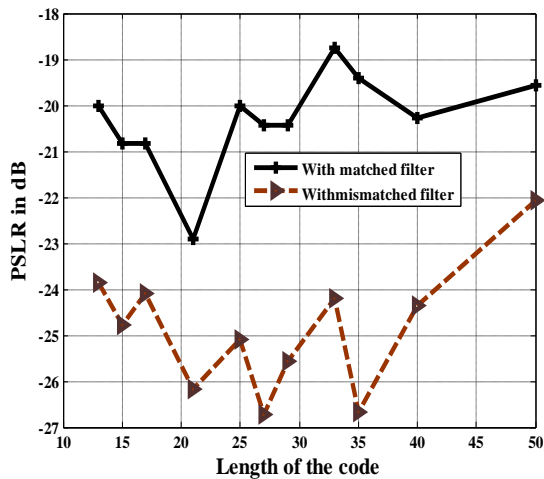


Fig.1.4. Comparison plot of PSLR with matched filter and with mismatched filter for ternary chaotic codes

5. CONCLUSION

In this paper a new method of design of mismatched filter to optimize PSLR of binary and ternary codes is proposed. For the ternary chaotic codes, good improvement in PSLR is observed at lower lengths. The filter can be used for larger length sequences but the length of the filter also proportionally increases with the length of the sequence which may make the practical implementation of the filter difficult. The most significant reduction in PSLR obtained with ternary chaotic code is -26.1740 dB at length 27. Reduction in PSLR of the mismatched filter output of Barker code is also observed which is -35.3551 dB. In previous literature design of mismatched filters using evolutionary algorithms like particle swarm optimization has been reported. But, the advantage of DE algorithm over the other methods is that it presents simple structure, convergence speed, versatility and robustness. The performance of the classical DE is sensitive to the choice of control parameters including the design of mutation factor. So this work can be extended to obtain better results by using the other schemes of DE to sequences of any length.

6. REFERENCES

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