

# HMM based Offline Handwritten Writer Independent English Character Recognition using Global and Local Feature Extraction

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## ABSTRACT

Recognition rate of handwritten character is still limited around 90 percent due to the presence of large variation of shape, scale and format in hand written characters. A sophisticated hand written character recognition system demands a better feature extraction technique that would take care of such variation of hand writing. In this paper, we propose a recognition model based on multiple Hidden Markov Models (HMMs) followed by few novel feature extraction techniques for a single character to tackle its different writing formats. We also propose a post-processing block at the final stage to enhance the recognition rate further. We have created a data-base of 13000 samples collected from 100 writers written five times for each character. 2600 samples have been used to train HMM and the rest are used to test recognition model. Using our proposed recognition system we have achieved a good average recognition rate of 98.26 percent.

## General Terms

Handwritten character recognition, Viterbi algorithm, Baum-Welch algorithm.

## Keywords

Hidden Markov Model, Sobel masks, gradient features, curvature features and projected histogram.

## 1. INTRODUCTION

The off-line handwriting recognition (OHR) still remains an active area for research towards exploring the newer techniques that would help improving recognition accuracy. It is because of the fact that several applications including mail sorting, bank processing, document reading and postal address recognition require offline handwriting recognition systems. Character recognition is nothing but Machine simulation of human reading [1], [2]. It is also known as Optical Character Recognition. It contributes immensely to the advancement of an automation process and can improve the interface between man and machine in numerous applications. Several research works have been focussing on new techniques and methods that would reduce the processing time while providing higher recognition accuracy.

Study reveals that the methods of Character Recognition have grown up sequentially [3], [4]. The recognition of isolated handwritten character was first investigated [5], but later whole words [6] were addressed. Most of the systems reported in literature until today consider constrained recognition

problems based on vocabularies from specific domain e.g., the recognition of handwritten check amounts [7] or postal address [8]. Free handwritten recognition, without domain specific constraints and large vocabularies was addressed only recently in a few papers [9], [10]. The recognition rate of such system is still low and there is a need of improvement [11].

It is now a well established fact that the direction of character strokes contains vast important information for character recognition. If the strokes in certain directions that occur at certain positions could be precisely described in the character image, the character will be easily categorized. Many statistical features used in character recognition are designed according to this idea [12]. Previous researchers [13][14] demonstrated that among direction features the gradient features [15] outperform various other directional features.

That's why we have given due stress on Gradient features by finding it both globally and locally for a character image. Gradient features are further supported by Projection features and curvature features. Projection features consist of mean, variance and entropy of the projected histograms on both X- and Y-axes.

The tool to train the system with the obtained feature vectors is taken to be HMM because OHR systems based on HMM have been shown to outperform segmentation based approaches [16]-[19]. With the usage of HMM models for the pattern recognition or character recognition, a HMM model keeps information for a character when the model is trained properly and the trained model can be used to recognize an unknown character. The advantage with HMM based systems is that they are segmentation free that is no pre- segmentation of word/line images into small units such as sub-words or characters is required [20]. On the other hand, HMM based approaches have been found to possess some limitations also. These limitations are due to two reasons-(a) the assumptions of conditional independence of the observations given the state sequence and (b) the restriction on feature extraction imposed by frame based observations [21].

However, the rest of the paper has been arranged as follows- Section 2 shows the proposed model, section 3 details out pre-processing, section 4 deals with feature extraction methods; section 5 describes the classifier whereas in section 6, post-processings are described. Section 7 is about the experiments and results. Conclusions have been drawn in section 8 and finally, in section 9, a single set of collected data has been shown.

## 2. PROPOSED MODEL

Features are extracted in both global and local processing. Generally for each character, a single HMM model is considered and trained by feature vectors. But we observe that some handwritten characters (e.g. A, W) show two completely different formats as shown in Fig.2. We use multiple HMM models for these characters whereas for other characters, we have taken single HMM model as shown in fig.3. Models are trained by the sequence of the symbols of the features extracted from some of the samples. To test a handwritten character image, we extract the similar features using same procedure as earlier and the corresponding sequence (observation) is compared with each HMM model  $P(O/\lambda)$ , probability of the observation sequence (O) by the models ( $\lambda$ ) is compared and the highest probability concludes the highest matching of the features with the corresponding model.

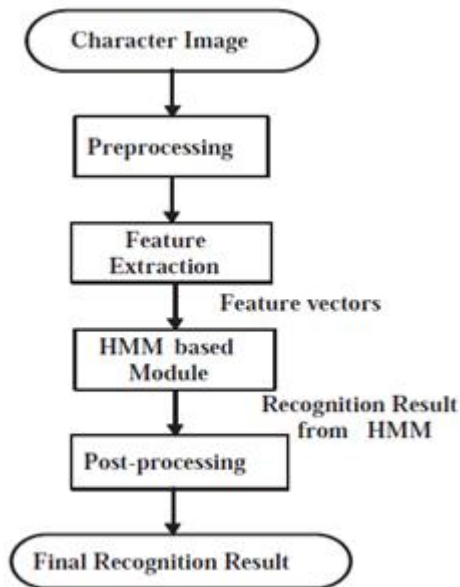


Fig. 1. System Overview

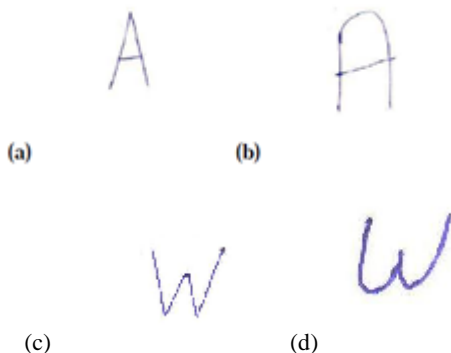


Fig.2. Two completely different formats for handwritten character A (a) A1 (b) A2 and for character W (c) W1 (d) W2

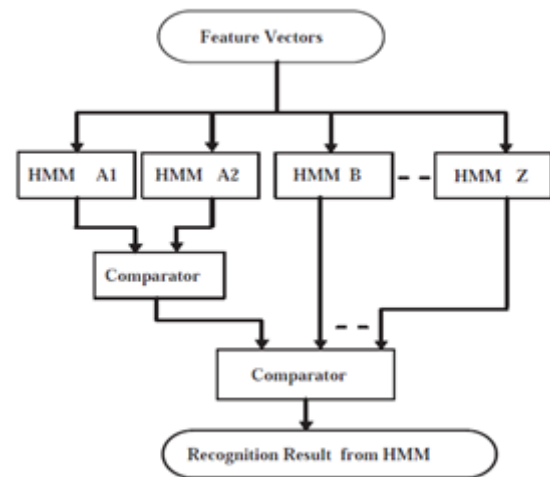


Fig.3. Proposed HMM Module for Character Recognition

## 3. PRE-PROCESSING

Any image processing application suffers from noise like isolated pixels. This noise gives rise to ambiguous features which results in poor recognition rate or accuracy. Therefore a preprocessing mechanism has been executed before we could start with feature extraction methods. Here a sequence of operations is carried out in succession as shown in flow diagram. We have used median filter for its better performance to get rid of unwanted marks or isolated pixels. Thinning is performed to get the skeleton of character image so that strokes could be conspicuous.

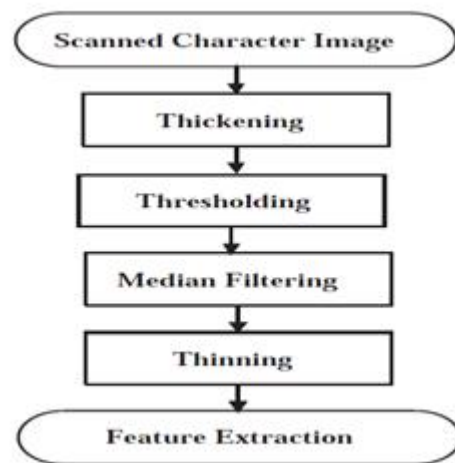


Fig. 4. Block Diagram for Pre-processing

## 4. FEATURE EXTRACTION METHODS

Feature extraction is an important part of any type of pattern recognition. A better feature extraction method may yield better recognition rate by a given classifier. Therefore, much attention is paid to extract the suitable features from the preprocessed images. Our feature extraction process consists of -

## 4.1 Global Feature Extraction Methods

Global features of an image sample describe its overall structure. We extract three global features as described below:

### 4.1.1 Gradient Features

To compute the density of line segments in the quantized direction we use only two masks - Horizontal sobel mask and Vertical sobel mask. Magnitude and phase of the gradient obtained by Sobel masks are calculated as below

$$\text{Magnitude: } M(x,y) = \sqrt{[S_H^2(x,y) + S_V^2(x,y)]} \quad (1)$$

$$\text{Phase: } \phi(x,y) = \tan^{-1} \frac{S_H(x,y)}{S_V(x,y)} \quad (2)$$

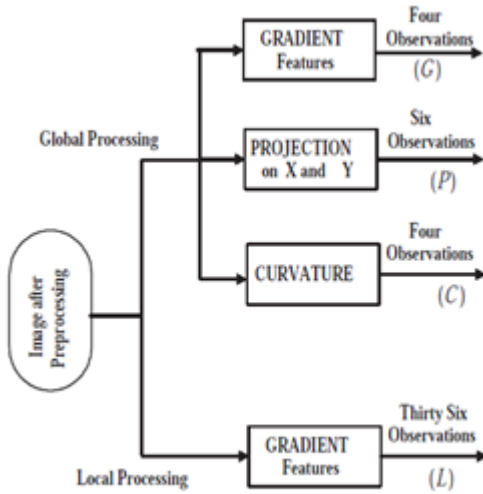


Fig. 5. Feature Extraction Process

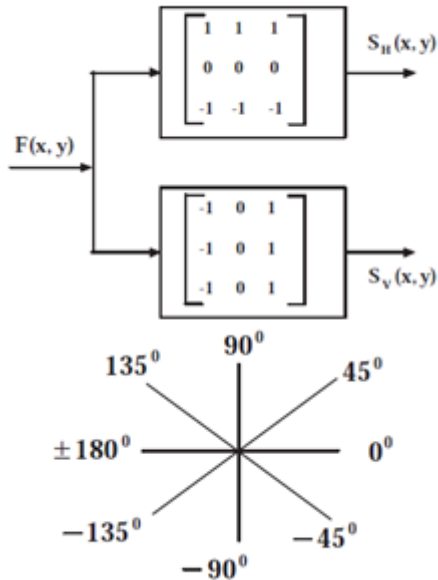


Fig. 6. Gradient Feature Extraction using Sobel Masks

Phase is quantized in eight directions as shown in Fig. 6. For each quantized phase value, corresponding magnitudes are added to get the total strength in that direction. To get the feature within finite number of symbols (here eleven symbols are used), magnitudes are normalized and quantized. Finally,

we consider four global gradient (G) features combining following pairs-(0°, ±180°), (45°, -135°), (90°, -90°) and (135°, -45°).

### 4.1.2 Projection Features

After preprocessing the two dimensional binary handwritten character image  $f(x, y)$  is projected to X and Y axis respectively and we get following two histograms.

Projection on X-axis:

$$U(i) = \sum_{k=1}^N f(i, k), \quad 1 \leq i \leq N \quad (3)$$

Projection on Y-axis:

$$V(j) = \sum_{k=1}^N f(k, j), \quad 1 \leq j \leq N \quad (4)$$

From each histogram we find three features, namely, mean, variance and entropy as given below

$$\mu_x = \frac{1}{N} \sum_{i=1}^N X(i) \quad (5)$$

$$\sigma_x^2 = \frac{1}{N} \sum_{i=1}^N (X(i) - \mu_x)^2 \quad (6)$$

and

$$E_x = - \sum_{i=1}^N e_{xi} \log(e_{xi}) \quad (7)$$

Where

$$e_{xi} = \frac{X(i)}{\sum_{i=1}^N X(i)}; \quad X = U \text{ and } V \quad (8)$$

Therefore, from projection method we find total six features as below

$$P = [\mu_U \sigma_U^2 E_U \mu_V \sigma_V^2 E_V]$$

### 4.1.3 Curvature Features

We have taken four curvatures measured from top (CT), bottom (CB), right side (CR) and left side (CL). Thus the curvature feature (C) consists of four observations as below

$$C = [C_T \ C_B \ C_R \ C_L]$$

## 4.2 Local Feature Extraction Methods

To extract the local information contained in the preprocessed character image, we divide the image by nine equal blocks and then, from each block four gradient features (as discussed earlier) are extracted. Thus, the local feature (L) contains 36 observations.

Therefore, our final observation sequence contains 50 observations obtained by global and local feature extraction methods, as shown below

$$O = [G(4) P(6) C(4) L(36)] \quad (9)$$

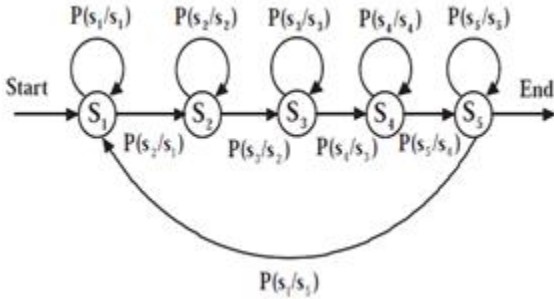
## 5. HIDDEN MARKOV MODEL

Hidden Markov Model (HMM) is a finite state machine in which a sequence of observations (O) is produced by this model but the corresponding sequence of states remains hidden within this model[16]. This HMM model can be defined as

$$\lambda = (\pi, A, B) \quad (10)$$

where  $\pi$  is initial state probability vector, A is final state transition probability matrix and B is final observation probability matrix. The HMM model was initially used for speech recognition purpose, but later it has been proved that

the HMM model can be efficiently utilized for other recognition process like character recognition, pattern recognition etc. In this paper we use a closed left to right chain HMM model for handwritten English characters recognition. A sketch of 5 states HMM model is shown in Fig.7.



**Fig. 7. Left to Right Chain HMM Model with 5 States.**

### 5.1 Training Of HMM Model

For the HMM model shown in Fig.7,  $\pi$  is taken as

$$\pi = [1 \ 0 \ 0 \ 0 \ 0] \quad (11)$$

Initial value of A and B are taken as below:

$$A = \begin{pmatrix} 0.8 & 0.2 & 0 & 0 & 0 \\ 0 & 0.8 & 0.2 & 0 & 0 \\ 0 & 0 & 0.8 & 0.2 & 0 \\ 0 & 0 & 0 & 0.8 & 0.2 \\ 0.2 & 0 & 0 & 0 & 0.8 \end{pmatrix}$$

and

$$B = \begin{pmatrix} 0.2 & 0.2 & 0.2 & 0.2 & 0.2 \\ 0.2 & 0.2 & 0.2 & 0.2 & 0.2 \\ 0.2 & 0.2 & 0.2 & 0.2 & 0.2 \\ 0.2 & 0.2 & 0.2 & 0.2 & 0.2 \\ 0.2 & 0.2 & 0.2 & 0.2 & 0.2 \end{pmatrix}$$

We have used Baum-Welch algorithm to train the HMM using observation sequence obtained from the feature vectors. At the end of training process we obtain the final value of A and B which is used for recognition purpose.

### 5.2. Recognition By HMM Model

Consider an observation vector (O) of length L as below

$$O = [O_1 \ O_2 \ O_3 \ \dots \ O_L] \quad (12)$$

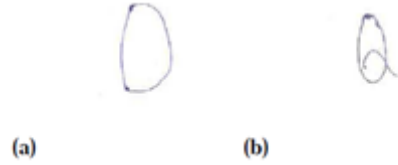
We use Viterbi decoding algorithm to decode the sequence of states of the HMM model  $\lambda$  for the sequence of observation O and it returns  $P(O/\lambda)$ , the probability of generating the given sequence O by the HMM model  $\lambda$ .

## 6. POST-PROCESSING

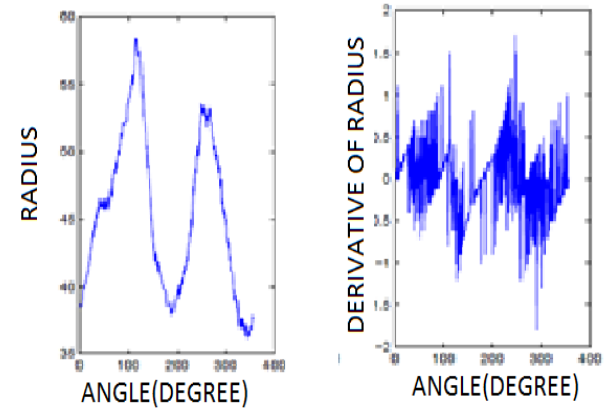
A post-processing block is included at the final stage of recognition process in order to provide special care to the highly confused group of characters due to their high structural correlation factor (similarity). Few examples of such groups are mentioned below-

- (1) O and Q,
- (2) M and N,
- (3) V and Y,
- (4) C and O,
- (5) B, K, R and P etc.

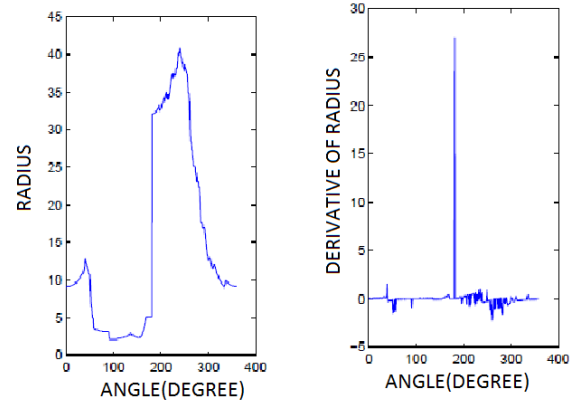
For each group we extract one or more new features that can discriminate these characters with almost 100 percent accuracy. For example, O and Q can be easily differentiated using signature features [18], as shown in Fig.8-10.



**Fig. 8. Samples of Character Image for Post-processing (a) Character O and (b) Character Q**



**Fig. 9. Signature and Derivative of Signature Plot for Character O Shown in Fig.8 (a).**



**Fig. 10. Signature and Derivative of Signature Plot for Character Q Shown in Fig.8 (b).**

These show that the differentiation of signature plot of Q contains very large spike that can be utilised to distinguish this (Q) from the character O using a threshold criteria. It should be noted that, this signature feature is not used to train the HMM models of all characters. The effect of this post-processing block is presented in the next section providing some experimental studies.

## 7. EXPERIMENTS AND RESULTS

A total of 13000 samples are collected from 100 persons. Each writer wrote 5 set of A-Z characters. Each character image is converted to a fixed size of 150x150 pixels. We have applied our feature extraction method on these samples and then these feature values are quantized and encoded to the eleven symbols in order to create sequences of observation symbols. First 100 samples of each character are used to train the corresponding character HMM. Rest 400 samples are used

to test our HMM classifier. For our experiment we have started with only 5 state model but we observed that as the no. of states of HMM model is increased, the corresponding recognition rate is also improved. Finally, we have got our expected result with 36 states HMM model as shown in tables. Table 1, shows the effectiveness of our proposed model of taking multiple HMM for a single character A.

**TABLE 1**  
**Improvement of Recognition Rate for Character A Using Proposed Model**

Character	Single HMM Model Recognition Rate (%)	Multiple HMM Model Recognition Rate (%)
A	85.25	98.5
W	89.5	98.0

In Table 2, we have shown final recognition rate of our character recognition system using post-processing and it is compared with result obtained without post processing technique. This produces an average recognition rate of 98.26%.

**TABLE 2**  
**Recognition Rate With Or Without Post-Processing (PP) Using Proposed Multiple HMM Model**

Character	Recognition Rate(%)		Character	Recognition Rate(%)	
	Without pp	With pp		Without pp	With pp
A	98.50	98.50	N	97.75	98.25
B	96.00	98.25	O	95.50	99.25
C	97.75	99.25	P	96.25	97.75
D	98.25	98.25	Q	96.25	99.00
E	98.75	98.75	R	92.75	97.25
F	99.00	99.00	S	95.50	95.50
G	94.50	94.50	T	98.25	98.25
H	97.75	97.75	U	98.50	98.50
I	99.25	99.25	V	96.75	98.75
J	98.50	98.50	W	98.00	98.00
K	97.50	98.75	X	98.25	98.25
L	98.75	98.75	Y	94.25	98.75
M	97.25	98.50	Z	99.50	99.50

## 8. CONCLUSION

In this paper, an approach has been made to increase the rate of recognition of handwritten character by finding both local and global features. Multiple level HMM model is designed for some specific letters having wide range of variations from writer to writer. In the last section, a trial has been made to put a line of demarcation between similar looking characters. All these specialties of this paper has made us obtain an average accuracy of 98.26%. For a significant number of letters, the accuracy rate is even close to 100%.

## 9. DATA-SET

One set of collected data has been shown for reference



## 10. ACKNOWLEDGMENTS

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