

# Performance Analysis of Turbo Code using EXIT Chart in Cooperative Communication

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## ABSTRACT

Whenever size, power or other constraints precluded the use of multiple transmit antennas, wireless systems cannot benefit from the well-known advantages of space time coding methods. Cooperation between wireless users has been proposed as a means to provide transmit diversity in the face of this limitation. This paper firstly analyse an ad-hoc network with a sender, a destination and a third station acting as relay is analyzed. Secondly in this paper Cooperative communication is performed with various well-known codes like convolution code and Turbo code. Using convolution code with cooperative communication provides full diversity and excellent coding gain. Turbo code offer better performance than Convolutional coding, Punctured Convolutional coding, Alamouti Scheme. [3] The turbo like decoding algorithm generally does not converge to a maximum-likelihood solution, although it is able to it is able to provide a good performance in practice. In this paer mostly extrinsic information transfer charts is used as tool to analyze the convergence behavior. We first design a PCCC-ID scheme for the sake of achieving decoding convergence at low SNR, using EXIT charts. Then invoke this PCC-ID scheme for cooperative communication, where the source employ PCCC-ID encoder and the relay encoding, interleaving and re-encoding which is then combined at destination using MRC.[5]

## 1. INTRODUCTION

Cooperative communications is a new communication technique which allows single antenna mobiles to share their antennas and to produce virtual multiple antenna system. Each mobile has one antenna and cannot individually generate spatial diversity. However, it may be possible for one mobile to receive the other, in which it can forward some version of “overheard” information along with its own data. Because the fading paths from two mobiles are statistically independent, this generates transmit diversity. [17] Cooperation leads to interesting tradeoffs in code rates and transmit power. Cooperative communication with turbo code gives the best performance. Turbo code achieve near Shannon limit error correction performance with relatively simple component codes. Turbo coding is a forward error correction (FEC) schmem.Iterative decoding is the key feature of turbo codes. Turbo code consists of concatenation of two convolution code. [9] Turbo codes give better performance at low SNR.

## 2. TURBO CODE

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### 2.1 Turbo code encoder

Generally, as a basic encoder RECURSIVE CONVOLUTIONAL ENCODER9RSC0 is used. If the component encoder is not recursive, the unit weight input sequence (0 0 0 1 1 1.....) will always generate a low weight codeword at the input of the second encoder for any interleaver design. In other words, interleaver would not influence the output codeword weight distribution if the component encoders were not recursive. However, if the component encoders are recursive, a weight-1 input sequence does not yield the minimum weight codeword out of encoder. The encoder output weight is kept finite only by trellies termination, a process that forces the coded sequence to terminate in such away that the encoder returns to zero state. [9]

Using figure the parallel configuration for the turbo encoder is shown figure. Good turbo codes have been constructed form component codes having short constraint lengths ( $k=3$  to 5).

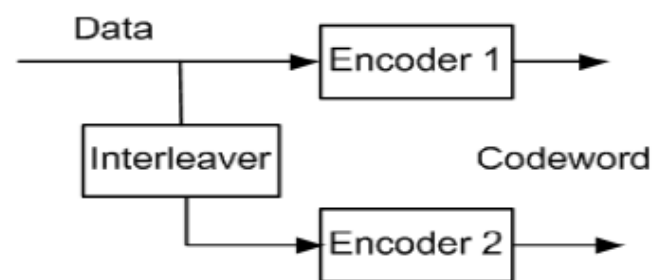
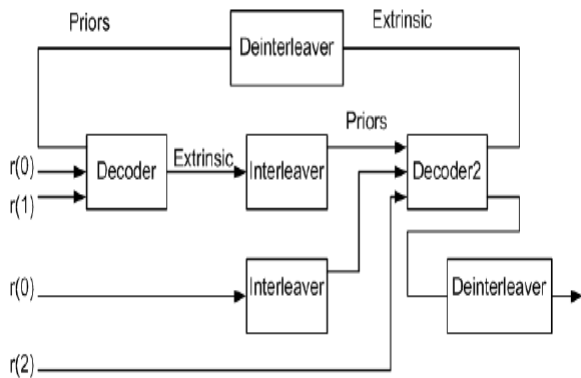


Fig 3: Turbo Encoder

### 2.2 Turbo Decoder

In typical communication receiver, a demodulator is often designed to produce soft decisions which are then transferred to a decoder. With Turbo codes, where two or more component codes are used and decoding involves feeding outputs from one decoder to the input of the other decoders in an iterative fashion Soft input soft output (SISO) decoder is used.

As shown in figure the output LLR of a systematic decoder can be represented as having three LLR elements. [19]

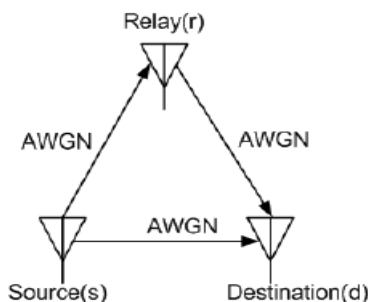


**Fig 4: Block Diagram of Turbo decoder**

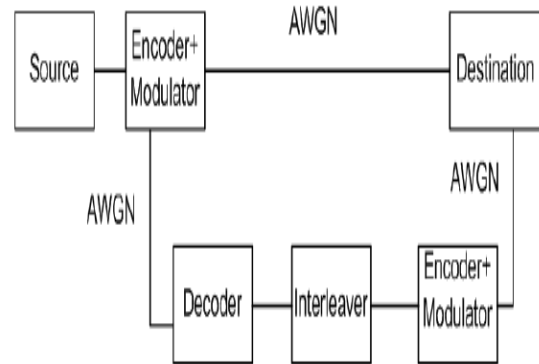
The following is the Block diagram of the turbo decoder. The received systematic bit and parity bit ( $r(0), r(1)$ ) associated with the first encoder are fed to decoder 1. This decoder initially uses uniform priors on the transmitted bits and produces probabilities called the extrinsic probabilities of the bits conditioned on the observed data. The output probabilities of decoder 1 are interleaved and passed to decoder 2, where they are used as "prior" probabilities in the decoder, along with the data associated with the second encoder, which are received systematic bits  $r(0)$  and parity bits  $r(2)$ . [14] The extrinsic output probabilities of decoder 2 are deinterleaved and passed back to become prior probabilities to decoder 1. The process of passing probability information back and forth continues until the decoder determines that the process has converged, or until some maximum number of iterations is reached. [11]

### 2.3 Cooperative Diversity using turbo codes

Here, consider a single relay system, consisting of one source, one relay, and one destination. Following figure-5(a) gives a block diagram of the two-hop relay system with a direct link from the source to the destination. A block diagram of a parallel concatenated DTC system is shown in figure-5(b).



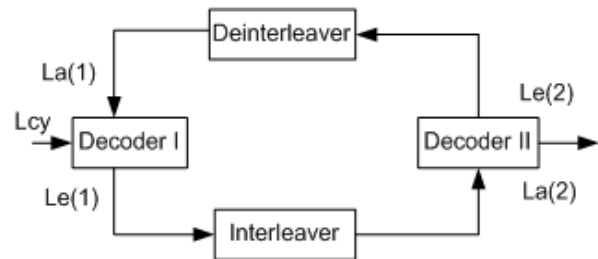
**Fig 5- a: Cooperative diversity system**



**Fig 5 b: Block Diagram of a cooperative Communication with turbo code**

### 3 TURBO CODE USING EXIT CHART

With wide application of turbo principle originally intended for decoding concatenated codes, the EXIT chart has been a powerful tool to visualize the convergence behavior of iterative decoding process based on mutual information. The Extrinsic Information Transfer EXIT chart was first introduced by Stephan ten Brink in [12]. The EXIT chart was mainly introduced due to the problem that occurs with BER chart when iteratively decoding is that it gives bad performance at low SNR. [7]



**Figure 6 Iterative decoder for parallel concatenated codes**

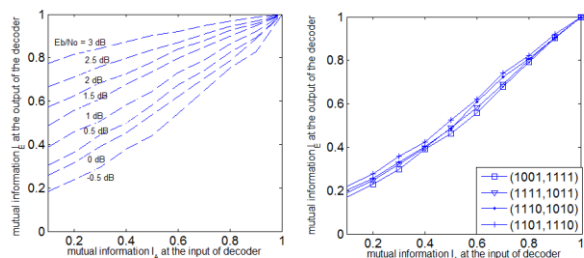
The iterative decoder for PCC is shown in Fig.4.2. For each iteration, the two decoder soft-in/soft-out decoders that accept and deliver probabilities or soft values and extrinsic part of the soft-output of one decoder is passed on to the other decoder to be used as a priori input. Thus it constitutes an iterative process with an information transfer between the two decoders which is analyzed using EXIT chart. For EXIT chart, we require the following parameters:

- Mutual Information
- Mutual information Transfer characteristics of iterative decoders
- Combination of Transfer characteristics [13]

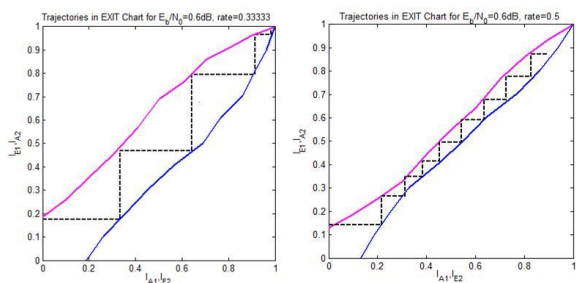
### 4. SIMULATION RESULT

The simulation results show the EXIT chart for the system model described in this chapter, in which the relay plays the most important role, i.e., relay decoding, interleaving, and re-encoding is done.  $E_b/N_0$ . The  $E_b/N_0$  value serves as a parameter for the curves. The BCJR algorithm is applied to a rate 1/2 recursive systematic convolution code of memory 4; the parity bits are punctured to obtain a rate 2/3 constituent code. The code polynomials (1010, 1110) are used. The

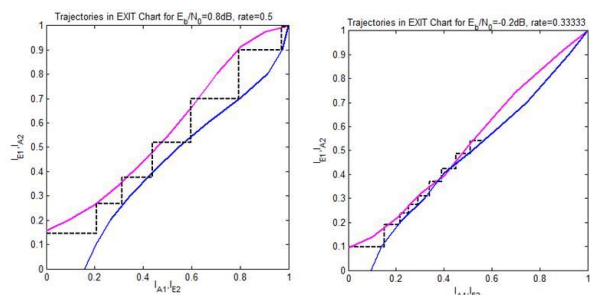
influence of different code polynomials is for the prominent case of a memory 4 code. The (1001, 1111)-code provides good extrinsic output at the beginning, but returns diminishing output for higher a priori input. For the (1101, 1110)-code it is the other way round. The constituent code of the classic rate 1/2 PCC with polynomials (1110, 1010) has good extrinsic output for low to medium a priori input.[15]



**Fig7 Influence of Eb/No and code polynomial on transfer characteristics**



**Figure 8: Exit chart for Eb/N0 = -0.2dB, rate = 0.33333 and Exit chart for Eb/N0 = 0.6 dB, rate = 0.33333**



**Figure 9: Exit chart for Eb/N0 = 0.6dB, rate = 0.5 and Exit chart for Eb/N0 = 0.8dB, rate = 0.5**

Fig.8 and Fig.9 shows the influence of code rate on transfer characteristics. To account for the iterative nature of the suboptimal decoding algorithm, both decoder characteristics are plotted into a single diagram. However, for the transfer characteristics of the second decoder the axes are swapped. Thus from the results it shows that the rate=1/2 gives better performance as there is more convergence.[16]

## 6 CONCLUSIONS

We can use turbo code with EXIT chart in cooperative communication. It gives better performance in terms of BER and SNR. The EXIT chart can be used to obtain an estimate on the BER after an arbitrary number of iterations. We can analyze the performance of mutual information at the input and output of decoder of Turbo code with help of EXIT chart.

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