

On Intuitionistic Fuzzy M-Precontinuous Mappings

Mahima Thakur

Department of Applied Mathematics
 Jabalpur Engineering College,
 Jabalpur, (M.P.) 482011 India.

S. S. Thakur

Department of Applied Mathematics
 Jabalpur Engineering College,
 Jabalpur, (M.P.) 482011 India.

ABSTRACT

The aim of this paper is to extend the concept of fuzzy M-pre continuous mappings due to Thakur and Singh [9] in intuitionistic fuzzy topological spaces and obtain some of their characterizations and properties.

Keywords

Intuitionistic fuzzy topology, Intuitionistic fuzzy M- pre continuous mappings.

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1. INTRODUCTION

After the introduction of fuzzy sets by Zadeh [11] in 1965 and fuzzy topology by Chang [4] in 1968, several researches were conducted on the generalizations of the notions of fuzzy sets and fuzzy topology. The concept of intuitionistic fuzzy sets was introduced by Atanassov [1, 2, 3] as a generalization of fuzzy sets. In the last 28 years various concepts of fuzzy mathematics have been extended for intuitionistic fuzzy sets. In 1997 Coker [5] introduced the concept of intuitionistic fuzzy topological spaces as a generalization of fuzzy topological spaces. In the same year Guecay Coker and Hayder [7] extended the concepts of fuzzy preopen sets and fuzzy precontinuity due to Bin Sahana [4] in intuitionistic fuzzy topology. In the present paper we introduce and study the concept of fuzzy M-pre continuous mappings in intuitionistic fuzzy topological spaces.

2. PRELIMANIRIES

Definition 2.1 [1]: Let X is a nonempty fixed set. An intuitionistic fuzzy set A in X is an object having the form

$$A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$$

Where the functions $\mu_A: X \rightarrow I$ and $\gamma_A: X \rightarrow I$ denote the degree of membership (namely $\mu_A(x)$) and the degree of non membership (namely $\gamma_A(x)$) of each element $x \in X$ to the set A , respectively, and $0 \leq \mu_A(x) + \gamma_A(x) \leq 1$ for each $x \in X$.

Definition 2.2 [1]: Let X be a nonempty set and the intuitionistic fuzzy sets A and B be in the form $A = \{ \langle x, \mu_A(x), \gamma_A(x) \rangle : x \in X \}$, $B = \{ \langle x, \mu_B(x), \gamma_B(x) \rangle : x \in X \}$

and let $\{A_i; i \in J\}$ be an arbitrary family of intuitionistic fuzzy sets in X . Then:

- (a) $A \subseteq B$ if $\forall x \in X [\mu_A(x) \leq \mu_B(x) \text{ and } \gamma_A(x) \geq \gamma_B(x)]$;
- (b) $A = B$ if $A \subseteq B$ and $B \subseteq A$;
- (c) $A^c = \{ \langle x, \gamma_A(x), \mu_A(x) \rangle : x \in X \}$;
- (d) $\bigcap A_i = \{ \langle x, \wedge \mu_{A_i}(x), \vee \gamma_{A_i}(x) \rangle : x \in X \}$;
- (e) $\bigcup A_i = \{ \langle x, \vee \mu_{A_i}(x), \wedge \gamma_{A_i}(x) \rangle : x \in X \}$;
- (f) $\tilde{0} = \{ \langle x, 0, 1 \rangle : x \in X \}$ and $\tilde{1} = \{ \langle x, 1, 0 \rangle : x \in X \}$.

Definition 2.3 [5]: Let X and Y be two nonempty sets and $f: X \rightarrow Y$ be a function. Then

(a) If $B = \{ \langle y, \mu_B(y), \gamma_B(y) \rangle : y \in Y \}$ is an intuitionistic fuzzy set in Y , then the pre image of B under f denoted by $f^{-1}(B)$, is the IFS in X defined by

$$f^{-1}(B) = \{ \langle x, f^{-1}(\mu_B)(x), f^{-1}(\gamma_B)(x) \rangle : x \in X \}$$

(b) If $A = \{ \langle x, \lambda_A(x), \nu_A(x) \rangle : x \in X \}$ is an intuitionistic fuzzy set in X , then the image of A under f denoted by $f(A)$ is the intuitionistic fuzzy set in Y defined by

$$f(A) = \{ \langle y, f(\lambda_A)(y), f(\nu_A)(y) \rangle : y \in Y \}$$

where, $f(\nu_A) = 1 - f(1 - \nu_A)$.

Definition 2.4 [5]: Two intuitionistic fuzzy sets A and B of X said to be q -coincident (AqB for short) if and only if there exists an element $x \in X$ such that $\mu_A(x) > \gamma_B(x)$ or $\gamma_A(x) < \mu_B(x)$.

Lemma 2.1 [5]: For any two intuitionistic fuzzy sets A and B of X , $\lceil (AqB) \Leftrightarrow A \subseteq B^c$ [5].

Definition 2.5[5]: An intuitionistic fuzzy topology on a nonempty set X is a family \mathfrak{T} of intuitionistic fuzzy sets in X satisfying the following axioms:

- (T₁) $\tilde{0}, \tilde{1} \in \mathfrak{T}$.
- (T₂) $G_1 \cap G_2 \in \mathfrak{T}$ for any $G_1, G_2 \in \mathfrak{T}$.
- (T₃) $\bigcup G_i \in \mathfrak{T}$ for any arbitrary family $\{G_i; i \in J\} \subseteq \mathfrak{T}$.

In this case the pair (X, \mathfrak{S}) is called an intuitionistic fuzzy topological space and each intuitionistic fuzzy set in \mathfrak{S} is known as an intuitionistic fuzzy open set in X . The complement A^c of an intuitionistic fuzzy open set is called an intuitionistic fuzzy closed set in X .

Definition 2.6 [5]: Let (X, \mathfrak{S}) be an intuitionistic fuzzy topological space and A be an intuitionistic fuzzy set in X . Then the fuzzy interior and fuzzy closure of A are defined by:

$$\text{cl}(A) = \bigcap \{K : K \text{ is an intuitionistic fuzzy closed set in } X \text{ and } A \subseteq K\},$$

$$\text{int}(A) = \bigcup \{G : G \text{ is an intuitionistic fuzzy open set in } X \text{ and } G \subseteq A\}$$

Lemma 2.2 [5] : For any intuitionistic fuzzy set A in (X, \mathfrak{S}) we have

- (a) A is an intuitionistic fuzzy closed set in $X \Leftrightarrow \text{cl}(A) = A$,
- (b) A is an intuitionistic fuzzy open set in $X \Leftrightarrow \text{int}(A) = A$;
- (c) $\text{cl}(A^c) = (\text{int}(A))^c$;
- (d) $\text{int}(A^c) = (\text{cl}(A))^c$.

Definition 2.7[7]: An intuitionistic fuzzy set A in an intuitionistic fuzzy topological space X is called :

- (a) Intuitionistic fuzzy pre open if $A \subseteq \text{int}(\text{cl}(A))$;
- (b) Intuitionistic fuzzy pre closed if its complement is intuitionistic fuzzy pre open.

Definition 2.8 [7]: Let (X, \mathfrak{S}) be an intuitionistic fuzzy topological space and A be an intuitionistic fuzzy set in X . Then the interior and closure of A are defined by:

$$\text{pcl}(A) = \bigcap \{K : K \text{ is an intuitionistic fuzzy pre closed set in } X \text{ and } A \subseteq K\},$$

$$\text{pint}(A) = \bigcup \{G : G \text{ is an intuitionistic fuzzy pre open set in } X \text{ and } G \subseteq A\}.$$

Definition 2.9[7]: A mapping $f : (X, \mathfrak{S}) \rightarrow (Y, \mathfrak{T})$ is said to be:

- (a) Intuitionistic fuzzy continuous if the inverse image of every Intuitionistic fuzzy open set of Y is Intuitionistic fuzzy open in X .
- (b) Intuitionistic fuzzy pre continuous if the inverse image of every Intuitionistic fuzzy open set of Y is intuitionistic fuzzy pre open set in X .

Definition 2.10: Let X be a non empty set and $p \in X$ a fixed element in X . If $\alpha \in (0,1]$ and $\beta \in [0,1)$ are two real numbers such that $\alpha + \beta \leq 1$ then, Intuitionistic fuzzy set $p(\alpha, \beta) = \{ \langle x, p_{\alpha}, 1-p_{1-\beta} \rangle : x \in X \}$ (where p_{α} is the fuzzy point in X with support p and value α) is called an Intuitionistic fuzzy point in X (IFP in short) where α denotes the degree of membership of $p(\alpha, \beta)$ and β denotes the degree of non membership of $p(\alpha, \beta)$.

3. INTUITIONISTIC FUZZY M-PRE CONTINUOUS MAPPINGS

Definition 3.1: A mapping f from an intuitionistic fuzzy topological space (X, \mathfrak{S}) to an intuitionistic fuzzy topological space (Y, \mathfrak{T}) is called intuitionistic fuzzy M-precontinuous if $f^{-1}(U)$ is intuitionistic fuzzy pre open set in X for every intuitionistic fuzzy pre open set U in Y .

Remark 3.1: Every intuitionistic fuzzy M-Precontinuous mapping is intuitionistic fuzzy precontinuous but the converse may not be true.

Example 3.1: Let $X = \{a, b\}$, $Y = \{x, y\}$ and U, V are the intuitionistic fuzzy sets respectively on X and Y defined as follows:

$$U = \{ \langle a, 0.4, 0.6 \rangle, \langle b, 0.5, 0.5 \rangle \},$$

$$V = \{ \langle a, 0.5, 0.5 \rangle, \langle b, 0.7, 0.3 \rangle \},$$

Let $\mathfrak{S} = \{ \tilde{0}, U, V, \tilde{1} \}$ and $\mathfrak{T} = \{ \tilde{0}, \tilde{1} \}$ be the intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $f: (X, \mathfrak{S}) \rightarrow (Y, \mathfrak{T})$ defined by $f(a) = x$ and $f(b) = y$ is intuitionistic fuzzy pre continuous (in fact intuitionistic fuzzy continuous) but not intuitionistic fuzzy M- pre continuous.

Consider the following example:

Example (3.2): Let $X = \{a, b\}$, $Y = \{x, y\}$ and V be an intuitionistic fuzzy set on Y defined as follows:

$$V = \{ \langle x, 0.5, 0.5 \rangle, \langle y, 0.6, 0.4 \rangle \},$$

Let $\mathfrak{S} = \{ \tilde{0}, \tilde{1} \}$ and $\mathfrak{T} = \{ \tilde{0}, V, \tilde{1} \}$ be intuitionistic fuzzy topologies on X and Y respectively. Then the mapping $g: (X, \mathfrak{S}) \rightarrow (Y, \mathfrak{T})$ defined by $g(a) = x$ and $g(b) = y$ is intuitionistic fuzzy M-precontinuous but not intuitionistic fuzzy continuous

Remark 3.2. Example 3.1 and Example 3.2 shows that the concepts of Intuitionistic fuzzy M-precontinuous and intuitionistic fuzzy continuous mappings are independent.

Theorem (3.1): The following statements are equivalent for a mapping $f: (X, \mathfrak{I}) \rightarrow (Y, \mathfrak{J})$:

- (a) f is intuitionistic fuzzy M -precontinuous.
- (b) $f^{-1}(V)$ is intuitionistic fuzzy pre closed set in X for every intuitionistic fuzzy pre closed set V in Y .
- (c) for every intuitionistic fuzzy point $P(\alpha, \beta)$ in X and every intuitionistic fuzzy preopen set V in Y such that $f(P(\alpha, \beta)) \in V$ there is an intuitionistic fuzzy pre open set U in X , such that $P(\alpha, \beta) \in U$ and $f(U) \subseteq V$.
- (d) for every intuitionistic fuzzy point $P(\alpha, \beta)$ in X and every pre neighbourhood V of $f(P(\alpha, \beta))$, $f^{-1}(V)$ is a pre neighbourhood of $P(\alpha, \beta)$.
- (e) for every intuitionistic fuzzy point $P(\alpha, \beta)$ in X and every pre neighbourhood V of $f(P(\alpha, \beta))$ there is a preneighbourhood U of $P(\alpha, \beta)$ such that $f(U) \subseteq V$.
- (f) $f(\text{pcl}(U)) \subseteq \text{pcl}(f(U))$ for every intuitionistic fuzzy set U of X .
- (g) $\text{pcl}(f^{-1}(V)) \subseteq f^{-1}(\text{pcl}(V))$ for every intuitionistic fuzzy set V of Y .
- (h) $f^{-1}(\text{pint}(V)) \subseteq \text{pint}(f^{-1}(V))$ for every intuitionistic fuzzy set V of Y .

PROOF :(a) \Leftrightarrow (b) Obvious.

(a) \Rightarrow (c). Let $P(\alpha, \beta)$ be an intuitionistic fuzzy point of X and V is an intuitionistic fuzzy pre open set in Y such that $f(P(\alpha, \beta)) \in V$. Put $U = f^{-1}(V)$. Then by (a), U is an intuitionistic fuzzy pre open set in X such that $P(\alpha, \beta) \in U$ and $f(U) \subseteq V$.

(c) \Rightarrow (a). Let V is intuitionistic fuzzy pre open set in Y and $P(\alpha, \beta) \in f^{-1}(V)$. Then $f(P(\alpha, \beta)) \in V$. Now by (c) there is an intuitionistic fuzzy preopen set U in X such that $P(\alpha, \beta) \in U$ and $f(U) \subseteq V$. Then $P(\alpha, \beta) \in U \subseteq f^{-1}(V)$. Hence $f^{-1}(V)$ is intuitionistic fuzzy pre open set in X .

(a) \Rightarrow (d). Let $P(\alpha, \beta)$ be an intuitionistic fuzzy point in X and V be a pre neighbourhood of $f(P(\alpha, \beta))$. Then there is a intuitionistic fuzzy pre open set W of Y such that $f(P(\alpha, \beta)) \in W \subseteq V$. Now $f^{-1}(W)$ is an intuitionistic fuzzy pre open set in X and $P(\alpha, \beta) \in f^{-1}(W) \subseteq f^{-1}(V)$. Thus $f^{-1}(V)$ is a pre neighbourhood of $P(\alpha, \beta)$ in X .

(d) \Rightarrow (e). Let $P(\alpha, \beta)$ be a intuitionistic fuzzy point of X and V be a pre neighbourhood of $f(P(\alpha, \beta))$. Then $U = f^{-1}(V)$ is a pre neighbourhood of $P(\alpha, \beta)$ and $f(U) = f(f^{-1}(V)) \subseteq V$.

(e) \Rightarrow (c). Let $P(\alpha, \beta)$ be an intuitionistic fuzzy point of X and V is an intuitionistic fuzzy pre open set in Y such that $f(P(\alpha, \beta)) \in V$. So there is pre neighbourhood W of $P(\alpha, \beta)$ in X such that $P(\alpha, \beta) \in W$ and $f(W) \subseteq V$. Hence there is an intuitionistic fuzzy pre open set U in X such that $P(\alpha, \beta) \in U \subseteq W$ and $f(U) \subseteq f(W) \subseteq V$.

(b) \Rightarrow (f). Let U be an intuitionistic fuzzy set of X . Since $U = f^{-1}(f(U))$, we have $U \subseteq f^{-1}(\text{pcl}(f(U)))$. Now $\text{pcl}(f(U))$ is an intuitionistic fuzzy pre closed set of Y and hence $f^{-1}(\text{pcl}(f(U)))$ is an intuitionistic fuzzy pre closed of X . Therefore $\text{pcl}(U) \subseteq f^{-1}(\text{pcl}(f(U)))$ and $f(\text{pcl}(U)) \subseteq f^{-1}(\text{pcl}(f(U))) \subseteq \text{pcl}(f(U))$.

(f) \Rightarrow (b). Let V is an intuitionistic fuzzy pre closed set of Y . then $f(\text{pcl}(f^{-1}(V))) \subseteq \text{pcl}(f(f^{-1}(V))) \subseteq \text{pcl}(V) = V$. Hence $\text{pcl}(f^{-1}(V)) \subseteq f^{-1}(V)$ and so $f^{-1}(V)$ is an intuitionistic fuzzy pre closed set of X .

(f) \Rightarrow (g). Let V be an intuitionistic fuzzy set of Y then $f^{-1}(V)$ is an intuitionistic fuzzy set of X . Therefore by hypothesis $f(\text{pcl}(f^{-1}(V))) \subseteq \text{pcl}(f^{-1}(V)) \subseteq \text{pcl}(V)$. Hence $\text{pcl}(f^{-1}(V)) \subseteq f^{-1}(\text{pcl}(V))$.

(g) \Rightarrow (f). Let U be a intuitionistic fuzzy set of X . Then $f(U)$ is an intuitionistic fuzzy set of Y and by (g), $\text{pcl}(f^{-1}(f(U))) \subseteq f^{-1}(\text{pcl}(f(U)))$. Hence $f(\text{pcl}(U)) \subseteq \text{pcl}(f(U))$.

(a) \Rightarrow (h). Let V be an intuitionistic fuzzy set of Y . Then $\text{pint}(V)$ is an intuitionistic fuzzy pre open set of Y and so by (a) $f^{-1}(\text{pint}(V))$ is an intuitionistic fuzzy pre open set of X . Since $f^{-1}(\text{pint}(V)) \subseteq f^{-1}(V)$, then $f^{-1}(\text{pint}(V)) \subseteq \text{pint}(f^{-1}(V))$.

(h) \Rightarrow (a). Let V be an intuitionistic fuzzy pre open set of Y . Then $\text{pint}(V) = V$ and $f^{-1}(V) \subseteq \text{pint}(f^{-1}(V))$. Thus $f^{-1}(V) = \text{pint}(f^{-1}(V))$ and $f^{-1}(V)$ is an intuitionistic fuzzy pre open set in X . Hence f is intuitionistic fuzzy M -precontinuous. ■

Lemma (3.1): A intuitionistic fuzzy set V is intuitionistic fuzzy pre open set of X if and only if there exists a intuitionistic fuzzy open set U such that $V \subseteq U \subseteq \text{cl}(V)$

Proof: Necessity if V is intuitionistic fuzzy pre open set of X Then $V \subseteq \text{int}(\text{cl}(V))$. Put $U = \text{int}(\text{cl}(V))$. Then U is intuitionistic fuzzy open and $V \subseteq U \subseteq \text{cl}(V)$.

Sufficiency: Let U be an intuitionistic fuzzy open set such that $V \subseteq U \subseteq \text{cl}(V)$. Then $V \subseteq \text{int}(U) \subseteq \text{int}(\text{cl}(V))$. Hence V is intuitionistic fuzzy pre open set of X .

Theorem (3.2): Let $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ be intuitionistic fuzzy precontinuous and intuitionistic fuzzy open mapping then f is intuitionistic fuzzy M -precontinuous.

Proof: Let V is intuitionistic fuzzy pre open set of Y then by Lemma (3.2) there exists a intuitionistic fuzzy open set U such that $V \subseteq U \subseteq \text{cl}(V)$. Therefore $f^{-1}(V) \subseteq f^{-1}(U) \subseteq f^{-1}(\text{cl}(V)) \subseteq \text{cl}(f^{-1}(V))$ because f is intuitionistic fuzzy open. Since f is intuitionistic fuzzy precontinuous, $f^{-1}(U)$ is intuitionistic fuzzy pre open set of X . Hence $f^{-1}(V) \subseteq f^{-1}(U) \subseteq \text{int}(\text{cl}(f^{-1}(U))) \subseteq \text{int}(\text{cl}(f^{-1}(V)))$ and $f^{-1}(V)$ is intuitionistic fuzzy pre open set of X . ■

Theorem (3.3): Let $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \omega)$ be two mappings. If f and g are intuitionistic fuzzy M -precontinuous then $g \circ f$ is intuitionistic fuzzy M -precontinuous.

Proof: Let V is an intuitionistic fuzzy pre open set in Z , since g is intuitionistic fuzzy M -precontinuous. $g^{-1}(V)$ is intuitionistic fuzzy pre open in Y . Therefore $(g \circ f)^{-1}(V) = f^{-1}(g^{-1}(V))$ is intuitionistic fuzzy pre open in X . because f is intuitionistic fuzzy M -precontinuous. Hence $g \circ f$ is intuitionistic fuzzy M -precontinuous. ■

Theorem (3.4): Let $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \omega)$ be two mappings. If f is intuitionistic fuzzy M -precontinuous and g is intuitionistic fuzzy precontinuous then $g \circ f$ is intuitionistic fuzzy M -precontinuous.

Proof: Let U be a intuitionistic fuzzy open set of Z . Since g is intuitionistic fuzzy precontinuous so $g^{-1}(U)$ is intuitionistic fuzzy pre open set of Y . Therefore $(g \circ f)^{-1}(U) = f^{-1}(g^{-1}(U))$ is intuitionistic fuzzy pre open set of X because f is intuitionistic fuzzy M -precontinuous. Hence $g \circ f$ is intuitionistic fuzzy precontinuous. ■

Definition (3.2): A mapping f from an intuitionistic fuzzy topological space (X, \mathfrak{I}) to an intuitionistic fuzzy topological space (Y, σ) is called intuitionistic fuzzy M -preopen if $f^{-1}(V)$ is intuitionistic fuzzy pre open set of Y for every intuitionistic fuzzy set V is intuitionistic fuzzy pre open set of X .

Remark (3.1): Every intuitionistic fuzzy M -preopen mapping is intuitionistic fuzzy pre open but the converse may not be true for,

Example (3.4): Let $X = \{a, b\}$, $Y = \{x, y\}$ and V be a intuitionistic fuzzy set of Y defined as follows:

$$V = \{ \langle a, 0.4, 0.6 \rangle, \langle b, 0.5, 0.5 \rangle \},$$

Let $\mathfrak{I} = \{ \tilde{0}, \tilde{1} \}$ and $\sigma = \{ \tilde{0}, V, \tilde{1} \}$. Then the mapping $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ defined by $f(a) = x, f(b) = y$ is intuitionistic fuzzy open and hence intuitionistic fuzzy preopen but not intuitionistic fuzzy M -preopen.

Consider the following example.

Example (3.5): Let $X = \{a, b\}$, $Y = \{x, y\}$ and U be a intuitionistic fuzzy set of X defined as follows:

$$U = \{ \langle a, 0.3, 0.7 \rangle, \langle b, 0.4, 0.6 \rangle \},$$

Let $\mathfrak{I} = \{ \tilde{0}, U, \tilde{1} \}$ and $\sigma = \{ \tilde{0}, \tilde{1} \}$. Then the mapping $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ defined by $f(a) = x, f(b) = y$ is intuitionistic fuzzy M -preopen but not intuitionistic fuzzy open.

Remark (3.2): Example (3.4) and example (3.5) shows that the concepts of intuitionistic fuzzy open and intuitionistic fuzzy M -preopen mappings are independent.

Theorem (3.5): Let $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ be an intuitionistic fuzzy M -preopen mapping. If V is a intuitionistic fuzzy set of Y and U is intuitionistic fuzzy pre closed set of X containing $f^{-1}(V)$, Then there exist a intuitionistic fuzzy set W in intuitionistic fuzzy pre closed set of Y such that $V \subseteq W$ and $f^{-1}(W) \subseteq U$.

Proof: Let $W = f(U)^c$. Since $f^{-1}(V) \subseteq U$ we have $f(U^c) = V^c$. Since f is intuitionistic fuzzy M -preopen, W is intuitionistic fuzzy pre closed set of Y and $f^{-1}(W) = (f^{-1}(f(U^c)))^c \subseteq ((U^c)^c) = U$. ■

Theorem (3.6): A mapping $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy M -preopen if and only if $f(\text{pint}(V)) \subseteq \text{pint}(f(V))$ for every intuitionistic fuzzy set V of X .

Proof: Necessity: If $f: (X, \mathfrak{I}) \rightarrow (Y, \sigma)$ is intuitionistic fuzzy M -preopen then $f(\text{pint}(V))$ is intuitionistic fuzzy preopen set of Y . Hence $f(\text{pint}(V)) = \text{pint}(f(V)) \subseteq \text{pint}(f(V))$. ■

Sufficiency: Let V is intuitionistic fuzzy set in X . Then by hypothesis $f(V)=f(\text{int}(V)) \subseteq \text{int } f(V)$ Hence $f(V)$ is intuitionistic fuzzy preopen set of Y . ■

Theorem (3.7): Let $f: (X, \mathfrak{T}) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \omega)$ are intuitionistic fuzzy M -preopen then $\text{gof} : (X, \mathfrak{T}) \rightarrow (Z, \omega)$ is also intuitionistic fuzzy M -preopen.

Proof: Obvious. ■

Theorem (3.8): Let $f: (X, \mathfrak{T}) \rightarrow (Y, \sigma)$ and $g: (Y, \sigma) \rightarrow (Z, \omega)$ be two mappings such that $\text{gof} : (X, \mathfrak{T}) \rightarrow (Z, \omega)$ is intuitionistic fuzzy M -preopen and g is intuitionistic fuzzy M -pre continuous and injective then f is intuitionistic fuzzy M -preopen.

Proof: Let V is intuitionistic fuzzy pre open set in X . Then $(\text{gof})(V)$ is intuitionistic fuzzy preopen set in Z because gof is intuitionistic fuzzy M -preopen. Since g is injective, we have $g^{-1}((\text{gof})(V))= f(V)$. Therefore $f(V)$ is intuitionistic fuzzy pre open set in Y , because g is intuitionistic fuzzy M -precontinuous. Hence f is intuitionistic fuzzy M -preopen. ■

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