

# Cost Optimization of Distributed Computing System with Dynamic Re-Allocation

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## ABSTRACT

A Distributed Computing System (DCS) is a combination of application and system programs that exchanges data across a number of independent terminals connected by a communication network. Cost optimization in DCS can be achieved by optimizing the performance of DCS. In task allocation two types of approaches are available and these are dynamic and static. Dynamic approach of task allocation is much better as compared to static, since it makes the best use of available computational resources in DCS. Task allocation problem can be described as 'm' number of tasks are required to execute on 'n' number of processors where number of tasks (m) is always greater than number of processors (n) ( $m > n$ ). This research offers a cost optimization algorithm with dynamic re-allocation of tasks to allocate the 'm' number of tasks on 'n' number of processors in DCS and their execution completes in k number of phases. Proposed algorithm is tested in MATLAB environment and it is noticed that obtained results are better as compared to past algorithms. Cost optimization dynamic model present in this research is helpful in performance optimization of DCS and also reduce the cost of task allocation in DCS.

## Keywords

Distributed Network, Dynamic Allocation, Performance, Residing cost, Reallocation cost

## 1. INTRODUCTION

Distributed Computing System (DCS) utilizes a network of many terminals in which each accomplish a partial operation of a task. Terminals are connected through communication channel either wireless or wired. DCS provides the facility of utilizing remote computing resources or data not reside in local terminals and also useful to increase the performance by providing facilities for distributed processing. DCS provide a higher performance, better reliability and better results over centralized network systems. In a DCS, the tasks of an application program must be allocated to processors to utilize the computational power and resources of the system in optimize manner. However, every time it is not possible that task will execute to processors for which the total cost of execution is minimized.

Dynamic task allocation has several merits over to static allocation in DCS. Dynamic allocation is a best way to use maximum utilization of computing resources in DCS because re-allocation of task modules dynamically are recommended during program execution, so as to take advantage of changes in the local reference patterns of the program. Hence Dynamic approach of task allocation are more common because they are more efficient and flexible.

This research consider a problem of task allocation for allocating 'm' tasks of an application to 'n' processors ( $m > n$ ) in such a way that total cost of execution can be minimized in distributed computing system. A dynamic task allocation method is used here to solve task allocation problem and it allocates the tasks to optimize overall task allocation cost. Some of the other related task allocation methods have been reported in literature such as Task Assignment [1, 10, 19], task scheduling [2, 3], Distributed Processing Environment [4], Task Allocation [5, 7, 9, 11, 13], data communication in Mobile Computing [6], Dynamic Task Allocation [8], Dynamic Tasks Scheduling [12, 16, 20, 22], Dynamic Optimization Algorithm [14], dynamic programming [15], Dynamic Reassignment [17], Dynamic Load Balancing [18] and Dynamic Task Assignment [21]. This research solve here a task allocation problem dynamically in DCS by allocating available processors in such a way that overall load should be balanced so system overloading can be avoided by using the proper utilization of processors.

## 2. OBJECTIVE

The objective of this research is to find out the optimal cost for a task allocation problem in Distributed Computing System (DCS) or develop a task allocation model that can minimize the overall system cost with the dynamic re-allocation approach. This research offers a mathematical model that allocates the tasks dynamically as tasks executes in various phases. During the particular task execution rest of other task are residing in the particular phase. Execution cost for each phase [EC], inter task communication cost [ITCC], residence cost [RC] of each task on different processors and relocation cost [REC] for each task are considered to design a dynamic tasks allocation model. To achieve cost optimization in DCS allocation method finds an allocation with minimum allocation cost.

## 3. TECHNIQUE

This research considers a distributed computing system consisting of a set  $T = \{t_1, t_2, t_3, t_4, \dots, t_m\}$  of m tasks to be allocated on a set  $P = \{p_1, p_2, p_3, \dots, p_n\}$  of n processors divided into k phases with criteria tasks m are more than the number of processors n ( $m > n$ ). Execution cost for phase wise of each processor is given in the form of Execution Cost Matrix  $ECM(.,.)$  of order  $k \times m \times n$ . The Residing Cost for residing the unexecuted tasks on the processor is mentioned in Residing Cost Matrix  $RCM(.,.)$  of order  $k \times m \times n$ . The Inter Task Communication Cost between executing and non-executing tasks are also considered and is mentioned in the Inter Task Communication Cost Matrix  $ITCCM(.,.)$  of order  $m \times k$  and during the processing a task is re-allocate from one processor to another processor then it also obtained some cost i.e. reallocation cost and it is given in the Reallocation Cost

Matrix RECM(.) of order  $m \times k$ . To calculate ERCM(.) for each phase sum up the values of ECM(.,) and RCM(.,). Compute the average of each row of ERCM(.) and arrange the values in increasing order in  $AVG\_ROW_{asc}()$ . Now it selects first  $n$  number tasks from  $AVG\_ROW_{asc}()$  and store them in  $ERCM\_I(.)$  and remaining  $n$  number of tasks in  $ERCM\_II$  by partitioning ERCM(.) into two sub problems. Follow the same process for next  $n$  or less than  $n$  and solve them using assignment method. Evaluate the Execution Cost, Communication Cost and Reallocation Cost. Follow the same process for all phases and at the end calculate the value of Execution Cost, Communication Cost and Reallocation Cost to obtain the phase wise total execution cost. Calculate the sum of optimal cost of each phase to evaluate the overall optimal cost of distributed computing system.

#### 4. ALGORITHM

- Step 1: Start Algo  
 Step 2: Read the number of tasks in  $m$   
 Step 3: Read the number of processors in  $n$   
 Step 4: Read the number of phases in  $k$   
 Step 5: Read the Execution Cost Matrix ECM(.,) of order  $k \times m \times n$   
 Step 6: Read the Residing Cost Matrix RCM(.,) of order  $k \times m \times n$   
 Step 7: Read the Inter Task Communication Cost Matrix ITCCM(.) of order  $m \times k$   
 Step 8: Read the Reallocation Cost Matrix RECM(.,) of order  $m \times k$   
 Step 9: For  $I = 1$  to  $m$   
     i.  $K = I$ ;  
     ii. Add the values for ECM(.,) and RCM(.,) and store the results in ERCM(.,)  
     iii. Store the average of each row of ERCM(.,) and store it in  $AVG\_ROW()$   
     iv. sort  $AVG\_ROW()$  in ascending and store the results in  $AVG\_Row_{asc}()$   
     v. While (All tasks of  $AVG\_Row_{asc}()$  !=SELECTED)  
     {  
         a. Make partition of ERCM(.,) for  $n$  tasks, store it in  $ERCM\_I(.)$  and  $ERCM\_II(.)$   
         b. Apply assignment method on  $ERCM\_I(.)$  and  $ERCM\_II(.)$   
     }  
     v. Compute Execution Cost (EC), Inter Task Communication Cost (ITCC) and Reallocation Cost (RC)  
     vi. Total Cost = EC + ITCC + RC  
      $I = I + 1$   
     vii. Optimal Cost = (Total Cost)  
 Step 10: End for  
 Step 11: State Results  
 Step 11: End Algo

#### 5. IMPLEMENTATION

This research considers a distributed computing system which is made up of four tasks  $\{t_1, t_2, t_3, t_4\}$  to be allocated on two processors  $\{p_1, p_2\}$  in five phases. The phase wise execution cost of individual processor is known in the form of Execution Cost Matrix ECM(.,) of order  $k \times m \times n$  where  $k$  is the number of phases,  $m$  is the number of tasks and  $n$  is the number of processors. Residing costs for the remaining tasks, except for the executing task, on each processor is also known and mentioned in Residing Cost Matrix (.,) or order  $k \times m \times n$ . Inter Task Communication Cost between the executing task

and all other task if they are on different processors also taken into the consideration and mentioned in Inter Task Communication Cost Matrix ITCCM(.) or order  $m \times k$ . During the execution an allocated task is shifted from one processor to another processor during the next phase then some cost is incurred in reassignment process at the end of each phase and it is known as reallocation cost. Reallocation cost for the given example is also known and it is mentioned in Reallocation Cost Matrix RECM(.) of order  $m \times k$ .

Table 1: Phase wise Execution Cost Matrix (ECM)

	Phase	Task	Execution Cost	
			P1	P2
ECM (.,) =	1	t <sub>1</sub>	6	5
		t <sub>2</sub>	-	-
		t <sub>3</sub>	-	-
		t <sub>4</sub>	-	-
	2	t <sub>1</sub>	-	-
		t <sub>2</sub>	8	7
		t <sub>3</sub>	-	-
		t <sub>4</sub>	-	-
	3	t <sub>1</sub>	-	-
		t <sub>2</sub>	-	-
		t <sub>3</sub>	4	6
		t <sub>4</sub>	-	-
	4	t <sub>1</sub>	-	-
		t <sub>2</sub>	-	-
		t <sub>3</sub>	-	-
		t <sub>4</sub>	5	3
	5	t <sub>1</sub>	9	7
		t <sub>2</sub>	-	-
		t <sub>3</sub>	-	-
		t <sub>4</sub>	-	-

Table 2: Phase wise Residing Cost Matrix (RCM)

	Phase	Task	Residing Cost	
			P1	P2
RCM (.,) =	1	t <sub>1</sub>	-	-
		t <sub>2</sub>	4	3
		t <sub>3</sub>	3	4
		t <sub>4</sub>	4	5
	2	t <sub>1</sub>	2	3
		t <sub>2</sub>	-	-
		t <sub>3</sub>	4	5
		t <sub>4</sub>	2	3
	3	t <sub>1</sub>	4	2

		t <sub>2</sub>	3	4
		t <sub>3</sub>	-	-
		t <sub>4</sub>	3	5
	4	t <sub>1</sub>	5	3
		t <sub>2</sub>	3	2
		t <sub>3</sub>	2	3
		t <sub>4</sub>	-	-
	5	t <sub>1</sub>	-	-
		t <sub>2</sub>	5	3
		t <sub>3</sub>	2	3
		t <sub>4</sub>	3	4

Table 3: Inter Task Communication Cost Matrix (ITCCM)

ITCC(,)=	Tasks ↓	Phases				
		1	2	3	4	5
	t <sub>1</sub>	-	3	4	3	-
	t <sub>2</sub>	2	-	3	4	2
	t <sub>3</sub>	5	3	-	4	3
	t <sub>4</sub>	2	3	5	-	0

Table 4: Reallocation Cost Matrix (RECM)

RECM(,)=	Tasks ↓	Phases				
		1	2	3	4	5
	t <sub>1</sub>	2	4	3	3	-
	t <sub>2</sub>	3	3	2	4	-
	t <sub>3</sub>	2	3	5	3	-
	t <sub>4</sub>	2	3	4	2	-

Task t<sub>1</sub> will execute in phase 1 as mentioned in ECM (Table 1) while remaining tasks i.e. t<sub>2</sub>, t<sub>3</sub> and t<sub>4</sub> will be treat as a residing tasks. Allocation algorithm will compute the sum of ECM(,) and RCM(,) for phase 1 and will form another matrix named as ERCM:

ERCM(,)=		p <sub>1</sub>	p <sub>2</sub>
	t <sub>1</sub>	6	5
	t <sub>2</sub>	4	3
	t <sub>3</sub>	3	4
	t <sub>4</sub>	4	5

Average of each row of ERCM(,) is calculated and store in an linear array named as AVG\_ROW(). On arranging the values of AVG\_ROW in ascending order a new linear array AVG\_ROW<sub>asc</sub>() is formed.

$$\begin{aligned}
 \text{AVG\_ROW}() &= \left\{ \begin{array}{cccc} t_1 & t_2 & t_3 & t_4 \end{array} \right\} \\
 &= \left\{ \begin{array}{cccc} 5.5 & 3.5 & 3.5 & 4.5 \end{array} \right\} \\
 \text{AVG\_ROW}_{\text{asc}}() &= \left\{ \begin{array}{cccc} t_2 & t_3 & t_4 & t_1 \end{array} \right\} \\
 &= \left\{ \begin{array}{cccc} 3.5 & 3.5 & 4.5 & 5.5 \end{array} \right\}
 \end{aligned}$$

In order to find optimal allocation, allocation technique will split ERCM(,) by selecting first two tasks from AVG\_ROW<sub>asc</sub>() and store the values in ERCM\_I(,) and last two tasks into ERCM\_II respectively:

ERCM_I(,)=		p <sub>1</sub>	p <sub>2</sub>
	t <sub>2</sub>	4	3
	t <sub>3</sub>	3	4
ERCM_II(,)=		p <sub>1</sub>	p <sub>2</sub>
	t <sub>4</sub>	4	5
	t <sub>1</sub>	6	5

On applying assignment method on ERCM\_I and ERCM\_II to allocate the tasks, allocation and their costs is obtained and present in Table 5.

Table 5: Initial Dynamic Allocation Table

Phase	Executing Task	Processor	Assigned Task	Execution Cost (EC)	Communication Cost (CC)	Reallocation Cost (RC)	Phase-wise Total Cost (EC + CC + RC)
1	t <sub>1</sub>	p <sub>1</sub>	t <sub>3</sub> * t <sub>4</sub>	7	2	0	17
		p <sub>2</sub>	t <sub>2</sub> * t <sub>1</sub>	8			

By following the same algorithm on the remaining phases final allocation is obtained as present in Table 6 for given example.

Table 6: Phase wise Dynamic Allocation Table

Phase	Executing Task	Processor	Assigned Task	Execution Cost (EC)	Communication Cost (CC)	Reallocation Cost (RC)	Phase-wise Total Cost (EC + CC + RC)
1	t <sub>1</sub>	p <sub>1</sub>	t <sub>3</sub> * t <sub>4</sub>	7	2	0	17
		p <sub>2</sub>	t <sub>2</sub> * t <sub>1</sub>	8			
2	t <sub>2</sub>	p <sub>1</sub>	t <sub>3</sub> * t <sub>1</sub>	6	3	7	26

		p <sub>2</sub>	t <sub>2</sub> * t <sub>4</sub>	10			
3	t <sub>3</sub>	p <sub>1</sub>	t <sub>4</sub> * t <sub>2</sub>	6	5	5	23
		p <sub>2</sub>	t <sub>3</sub> * t <sub>1</sub>	8			
4	t <sub>4</sub>	p <sub>1</sub>	t <sub>4</sub> * t <sub>3</sub>	7	4	7	23
		p <sub>2</sub>	t <sub>1</sub> * t <sub>2</sub>	5			
5	t <sub>1</sub>	p <sub>1</sub>	t <sub>2</sub> * t <sub>3</sub>	7	2	0	20
		p <sub>2</sub>	t <sub>1</sub> * t <sub>4</sub>	11			
Total execution cost							109

## 6. CONCLUSION

This research designed a task allocation model with dynamic reallocation technique for execution of tasks in Distributed Computing System (DCS) and provides the optimal solution in order to get optimized costs for task allocation. This allocation model considered the several factors of dynamic environment i.e. execution cost, residing cost, reallocation cost, inter task communication cost and most important execution phases. In dynamic model a tasks completes its execution in various phase so presented dynamic allocation model provide optimal solution phase wise. The presented model is tested in MATLAB platform by creating distributed environment as mentioned in Fig. 1. Optimal cost is calculated for each phase and every task. Communication cost between executing and non-executing task, reallocation cost of task are also added to evaluate final optimal cost of each phase. Phase wise results are generated in MLATLAB for presented algorithm and algorithm [17], results are compared for both algorithms, on comparing phase wise execution cost and total execution cost, it is found presented model shows the better results as mentioned in Table 7.

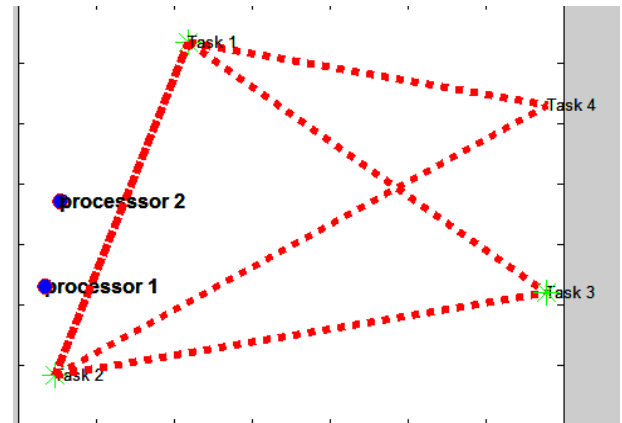


Fig.1: Distributed environment in MATLAB

Table 7: Algorithm results derived in MATLAB environment and compare with algorithm [17]

Phase	Executing Task	Processor	Assigned Task	Phase wise cost for presented algorithm	Phase wise cost for algorithm [17]
1	t <sub>1</sub>	p <sub>1</sub>	t <sub>3</sub> * t <sub>4</sub>	18	18
		p <sub>2</sub>	t <sub>2</sub> * t <sub>1</sub>		
2	t <sub>2</sub>	p <sub>1</sub>	t <sub>3</sub> * t <sub>1</sub>	24	24
		p <sub>2</sub>	t <sub>2</sub> * t <sub>4</sub>		
3	t <sub>3</sub>	p <sub>1</sub>	t <sub>4</sub> * t <sub>2</sub>	33	25
		p <sub>2</sub>	t <sub>3</sub> * t <sub>1</sub>		
4	t <sub>4</sub>	p <sub>1</sub>	t <sub>4</sub> * t <sub>3</sub>	28	30
		p <sub>2</sub>	t <sub>1</sub> * t <sub>2</sub>		
5	t <sub>1</sub>	p <sub>1</sub>	t <sub>2</sub> * t <sub>3</sub>	15	23
		p <sub>2</sub>	t <sub>1</sub> * t <sub>4</sub>		
Overall Optimal Cost				118	120

Graphical representation of comparison as mentioned in Table 7 is also drawn and it is mentioned in Fig. 2.

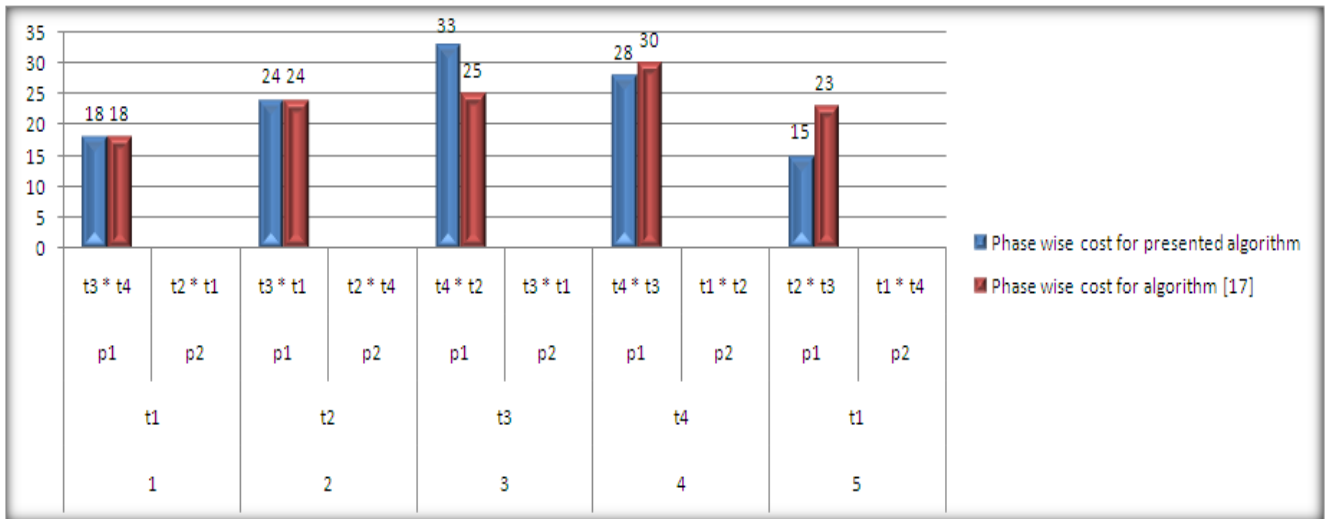


Fig. 2: Showing phase wise comparative results of presented algorithm with algorithm [17]

Overall results also evaluated and compared with algorithm [17] as mentioned in Fig. 3.

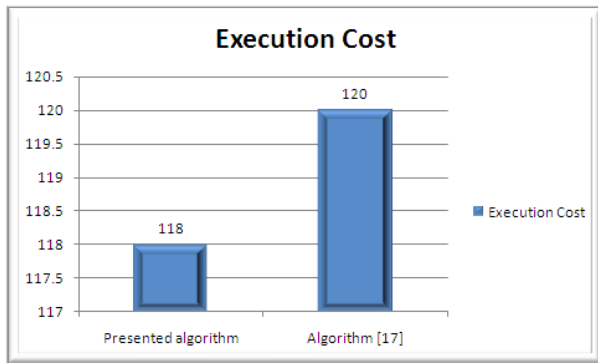


Fig.3: Execution cost for present algorithm and algorithm [17]

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