

Fig 2: Indoor power-line network for house 2

Numbers in vertical and horizontal branches represent branch length and branch ID. In determining the impulse response for each topology the power-line channel model by Anatory et al was used. The receiver terminals were located at the switch sockets for each topology.

3. IMPULSE RESPONSE OF AN INDOOR POWER-LINE NETWORK

To be able to design a communication system using typical Tanzania indoor power-line network based on multicarrier modulation, channel delay spread must be determined first. From the circuit diagram of each map the impulse response was estimated at the switch sockets using the recent power-line channel model by Anatory et al. The model is given in (1a) [5]. Equation (2.1) [5] gives the transfer function between any load point (receiver location) and the sending end (transmitter location).

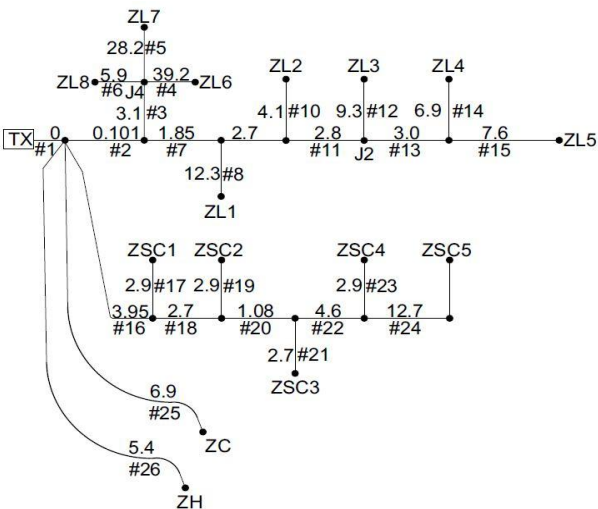


Fig 3: Indoor power-line network for house 3

During the impulse response determination; the transmitter was placed at the distribution function block that includes all the system (with all branches included) and the receiver side was placed at the switch sockets, the loads where either terminated at low or high impedances because in PLN it has been shown that the maximum delay spread occurs for cases when the channel is terminated either in low impedances or high impedances [6].

The most common insulation material of low voltage power cables for Tanzania indoor power-line network is PVC. However, it is not practical to define any general dielectric characteristics of the PVC. This is because the characteristics of the PVC depend heavily on the factors like temperature, frequency and the exact

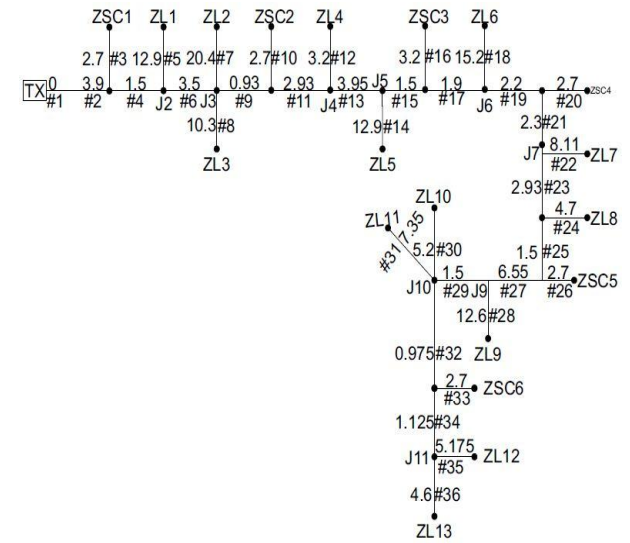


Fig 4: Indoor power-line network for house 4 composition of the insulation material [12].

Fig. 5 shows the relationship between dielectric constant, frequency, and temperature.

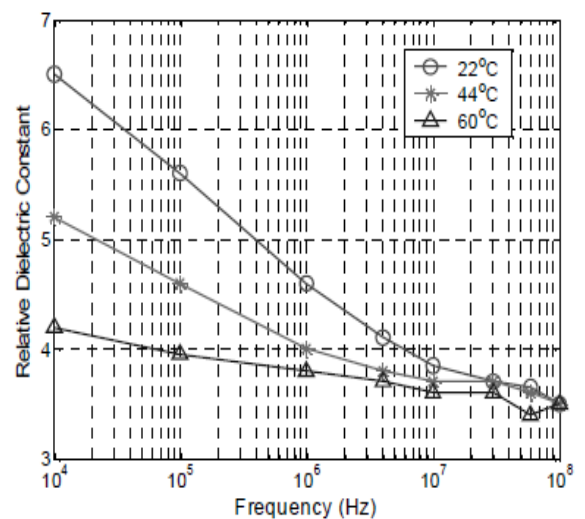


Fig 5: Relationship of the dielectric constant, frequency and temperature [12]

Due to the fact that it is not practical to define any general dielectric characteristics of the PVC for this study ϵ_r was taken to be 4.75 and μ_r was taken to be 1. Also because in a real transmission line attenuation caused by R and G is much less than by L and C, i.e. $R \ll \omega L$ and $G \ll \omega C$, then the lossless case was considered. The per unit length inductances, capacitances, characteristic impedances and propagation constants for a lossless case were found using;

$$L = (\mu/\pi) \cosh^{-1}(D/2a) [H] \quad (1)$$

$$C = \frac{\pi\epsilon}{\cosh^{-1}(D/2a)} [F/M] \quad (2)$$

$$Z = \sqrt{\frac{L}{C}} \quad (3)$$

$$\gamma = \alpha + j\beta = j\omega\sqrt{LC} \quad (4)$$

The parameter μ is permeability of the dielectric material, D is the cable diameter (or separation between live and neutral), a is radius of conductor and ϵ is permittivity of the dielectric medium.

During impulse response determination the transmitter was a 2V rectangular pulse, with 0.9 μ s pulse width and shifted by 0.1 μ s. This rectangular pulse was then applied to the Tanzania indoor power-line network with source impedance terminated in characteristic impedance. After finding the channel transfer function in frequency domain, the signal response in frequency domain was determined using (2) [5] at the switch sockets where the receiver is located.

Finally the impulse response was found by Inverse Fourier Transform. In all cases source impedance was 85 Ω .

4. TYPICAL IMPULSE RESPONSES FOR TANZANIA HOME POWER-LINES NETWORKS

The following Figures depict the impulse responses at various terminals for each house. For each house the impulse responses were determined at various terminals all terminated in 10 Ω and 100k Ω respectively. And for all analyses the source impedance was 85 Ω .

Consideration of all impulse responses displayed by Figures 6-9 showed that the maximum delay spread (time span of channel impulse response) T_m was about 2 μ s. This is because according to

Figures 6(a)-9(a) channel amplitudes at low impedances were very smaller hence contributing less to channel amplitude fluctuations.

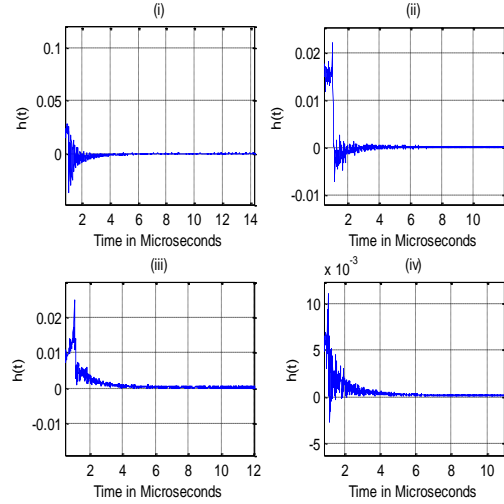


Fig 6(a) House 1 impulse response at various loads (all terminated in 10 Ω) (i) ZSC1, (ii) ZSC3, (iii) ZSC5 and (iv) ZSC7.

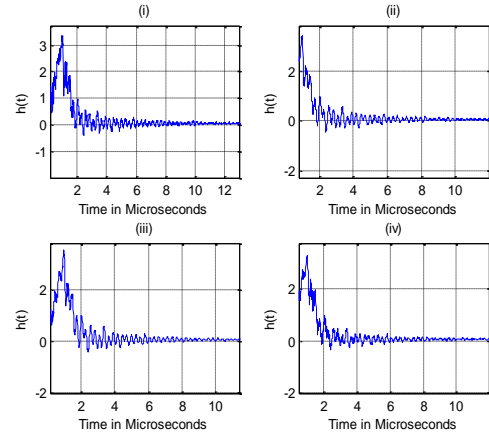


Fig 6(b): House 1 impulse response at various loads (all terminated in 100k Ω) (i) ZSC1, (ii) ZSC3, (iii) ZSC5 and (iv) ZSC7.

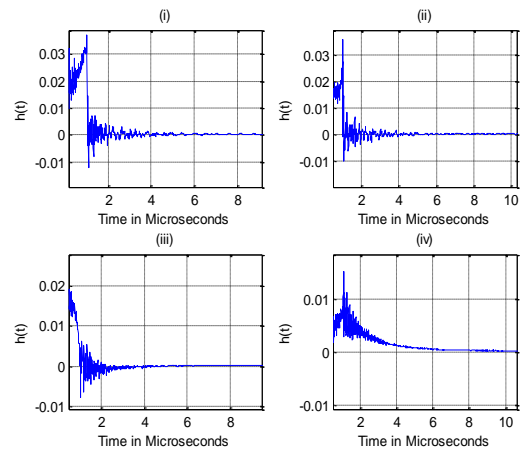


Fig 7(a): House 2 impulse response at various loads (all terminated in 10 Ω) (i) ZSC1, (ii) ZSC2, (iii) ZSC3 and (iv) ZSC5

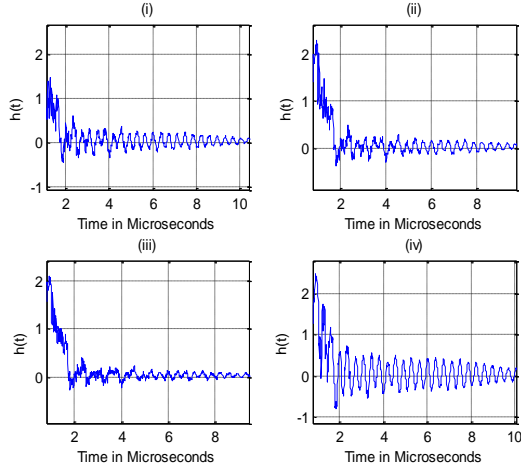


Fig 7(b): House 2 impulse response at various loads (all terminated in 100kΩ) (i) ZSC1, (ii) ZSC2, (iii) ZSC3 and (iv) ZSC6

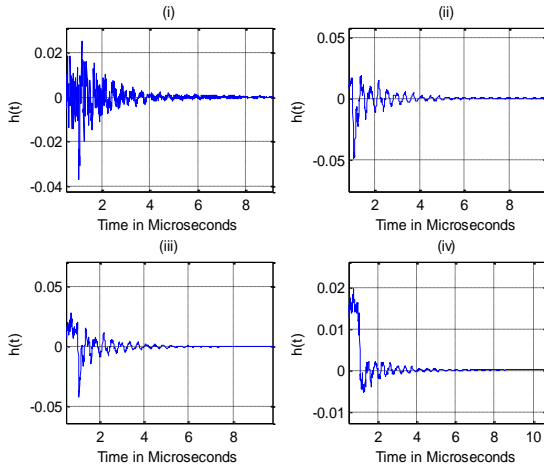


Fig 8(a): House 3 impulse response at various loads (all terminated in 10Ω) (i) ZSC1, (ii) ZSC3, (iii) ZSC4 and (iv) ZSC5

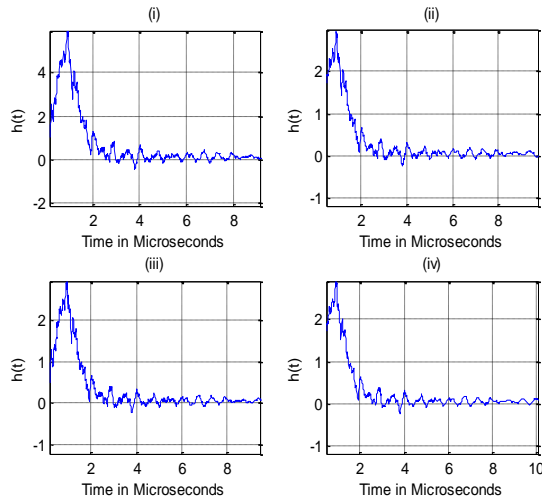


Fig 8(b): House 3 impulse response at various loads (all terminated in 100kΩ) (i) ZSC1, (ii) ZSC3, (iii) ZSC4 and (iv) ZSC5

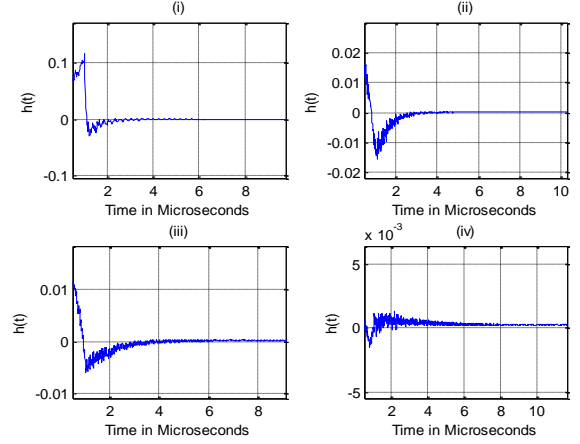


Fig 9(a): House 4 impulse response at various loads (all terminated in 10Ω) (i) ZSC1, (ii) ZSC3, (iii) ZSC5 and (iv) ZSC6

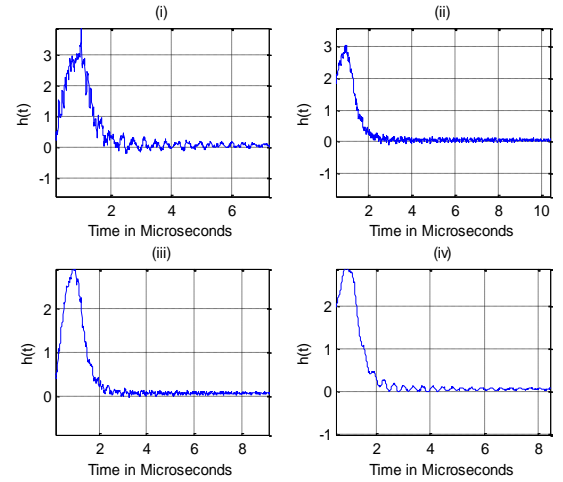


Fig 9(b): House 4 impulse response at various loads (all terminated in 100kΩ) (i) ZSC1, (ii) ZSC3, (iii) ZSC5 and (iv) ZSC6

5. OFDM SYSTEM DESIGN

An OFDM system with total frequency band $B=16.5\text{MHz}$ was considered. Since the number of sub-channels N has to be chosen in such a way that the symbol time in each sub-channel is greater than the delay spread of the channel so as to combat ISI (sub-channel bandwidth is less than the channel coherence bandwidth), then given the maximum delay spread of $2\mu\text{s}$, the channel coherence bandwidth B_c was $B_c = 1 / T_m = 1 / 2\mu\text{s} = 0.5\text{MHz}$. To insure flat-fading on each sub channel $BN = B / N = 0.1 * B_c$.

Where B is the total bandwidth and B_c is the coherence bandwidth. Thus, $N = B / 0.1 * B_c = 16.5\text{MHz} / (0.1 * 0.5\text{MHz}) = 330$ sub channels are needed to insure flat-fading on each sub channel.

In discrete implementations of multicarrier N must be a power of two for the DFT and IDFT operations, in which case $N = 512$ for this set of parameters [6]. So the OFDM symbol duration was $T_N = 1 / BN = N / B = 512 / 16.5\text{MHz} = 31.03\mu\text{s}$

which is more than the delay spread of the channel hence ISI between OFDM symbols is removed. But the orthogonality of sub channels in OFDM cannot be maintained. This is because individual sub channels cannot be completely separated by using an FFT circuit at the receiver due to adjacent inter-symbol interference (AIS) introduced by transmission channel distortions. To reduce the (AIS) distortion, a simple solution is to increase the symbol duration or the number of carriers. However, this method may be difficult to implement in terms of carrier stability against Doppler frequency and FFT size.

A practical way to eliminate AIS between adjacent OFDM symbols is to create a cyclically extended guard interval called a cyclic prefix. This way each OFDM symbol is preceded by a periodic extension of the signal itself. The total symbol duration becomes $T = T_N + T_G$.

Where T_G , is the guard interval (Cyclic prefix). With a cyclic prefix included each symbol is made of two parts. The whole signal is contained in the active symbol, the last part of which is also repeated at the start of the symbol and is called a guard interval or cyclic prefix. When the guard interval is longer than the channel impulse response, or the multipath delay, the effect of AIS can be eliminated. However, the intercarrier interference (ICI), or in-band fading, still exists [8].

The length of the cyclic prefix was set to $\mu = 64 \gg T_m / T_s = 2 * 16.5 = 33$ to insure no ISI between adjacent OFDM symbols.

All design parameters of the OFDM system are summarized in Table 1.

Table 1: OFDM system parameters

No.	Parameter	Value
1.	Total Bandwidth (B)	16.5MHz
2.	Coherence Bandwidth (B_c)	0.5MHz
3.	Number of Channels (N)	512
4.	Modulation	BPSK, OFDM
5.	Symbol Duration (T_N)	34.91 μ s
6.	Cyclic Prefix (μ)	64
7.	Guard Interval	3.88 μ s
8.	Sub-channel Bandwidth (BN)	32.22 KHz
9.	Data Rate (BPSK)	1.67 bps

6. BIT ERROR RATE EXPRESSIONS FOR UN-CODED OFDM

The performance indication of any modulation scheme in any communication channel is through bit error rate performance. The channel impulse response of the power-line is given as in (5) and it can be expanded to appear as in (6). The corresponding sub-channel response is given in (7).

$$h(t, \tau) = \sum_{i=0}^{L-1} h_i(t) \delta(t - \tau_i) \quad (5)$$

$$h(t, \tau) = h_0 + h_1 \delta(t - \tau_1) + h_2 \delta(t - \tau_2) + h_3 \delta(t - \tau_3) + \dots + h_{L-1} \delta(t - \tau_{L-1}) \quad (6)$$

$$H_k = h_0 + h_1 e^{-j\pi \frac{k}{N}} + h_2 e^{-j\pi \frac{2k}{N}} + h_3 e^{-j\pi \frac{3k}{N}} + \dots + e^{-j\pi \frac{4k}{N}} \quad (7)$$

For instance assuming the power-line channel with impulse response as in (3.12);

$$h(t, \tau) = 0.7\delta(t) + 0.25\delta(t - 0.5T_b) + 0.7\delta(t - 1.5T_b) + 0.5\delta(t - 3T_b) \quad (8)$$

Then the corresponding sub-channel response is as in (9);

$$H_k = 0.7 - 0.25e^{-j\pi \frac{k}{N}} + 0.7e^{-j\pi \frac{3k}{N}} + 0.5e^{-j\pi \frac{6k}{N}} \quad (9)$$

The OFDM system may be implemented by using BPSK or QPSK or M-QAM. The BER performance of a PLC-OFDM based system under BPSK, QPSK and M-QAM is given by (10-13) respectively. In (10-13) the parameters E_b , N_m , H_k and N represent the energy signal, noise power, sub-channel response and number of sub-channels respectively. The parameters T_N and T_{guard} are information time and guard time [1].

$$P_{bk} = \frac{1}{N} \sum_{k=0}^{N-1} Q \left[\sqrt{\frac{2|H_k|^2 a_g E_b}{N_m}} \right] \quad (10)$$

$$P_{bk} = \frac{1}{N} \sum_{k=0}^{N-1} 2Q \left[\sqrt{\frac{2|H_k|^2 a_g E_b}{N_m}} \right] - Q^2 \left[\sqrt{\frac{2|H_k|^2 a_g E_b}{N_m}} \right] \quad (11)$$

$$P_{bk} = \frac{1}{N} \sum_{k=0}^{N-1} 4 \left[1 - \frac{1}{\sqrt{M}} \right] * Q \left[\sqrt{\frac{3 \log_2 M |H_k|^2 a_g E_b}{(M-1)N_m}} \right] \quad (12)$$

$$a_g = \frac{T_N}{T_N + T_{guard}} \quad (13)$$

In this study equation 10 and 13 were used for evaluating the performance of the PLC-OFDM system with BPSK modulation using MATLAB simulations. During the simulations H_k was derived from the typical impulse responses of the four Tanzania home power-line networks as discussed above. N_m represented noise power as it's

explained in [5]. The remaining parameters were obtained from the OFDM parameters in Table 1.

7. OFDM SYSTEM PERFORMANCE ANALYSIS

The home power-line networks have different topologies which are governed by the location of loads within a room and number of rooms. Different numbers of rooms add branches to the power-line network. Types of equipments used in house influence load impedance which varies with frequency. The distance between junction boxes dictates the branch length and hence all these affect the performance of the channel. To determine the influence of branches, branch length and load impedance the power line configurations from four houses were selected. The transmitter was placed at the main switch while the receiver was located at the switch sockets. The transmitter was terminated in line characteristics impedance while the receiver was terminated at 50Ω and 10kΩ for low and high impedance analyses respectively.

7.1. Influence of Low Impedance, Number of Branches and Branch Length

First the home power-line network 1 was considered. The transmitter was at node 1 just after the main switch. Fig. 10-13 shows the performance of the four home power-line channels at different terminals, terminated at 50Ω for each house. It is observed that for all four home power-line channels the good performance is obtained at ZSC1 because it is close to the transmitter. The good performance of 10⁻¹⁰ is obtained at the load ZSC1 at SNR per bit of 42.5dB, 42dB, 32.5dB and 41dB for HPLN 1, HPLN 2, HPLN 3 and HPLN 4 respectively. The performance at the other nodes is degraded due to number of branches between transmitting and receiving ends.

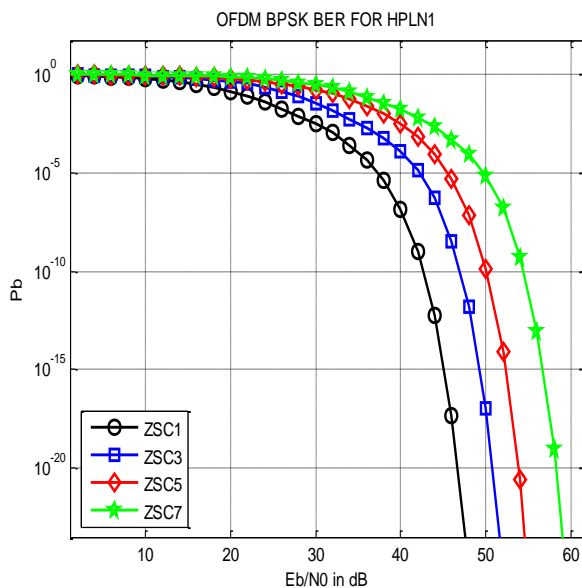


Fig 10: HPLN 1 simulation results at different loads (all terminated at 50Ω)

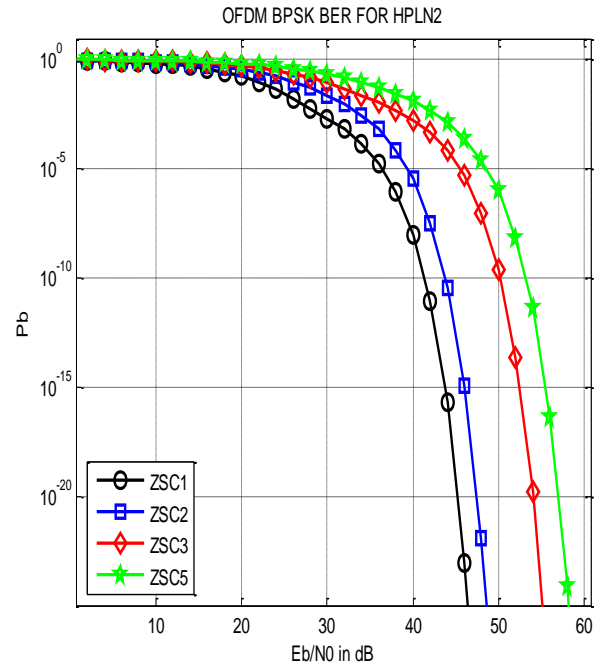


Fig 11: HPLN 2 simulation results at different loads (all terminated at 50Ω)

7.2. Influence of High Impedance, Number of Branches and Branch Length

Fig. 14-17 shows the performance of the four home power-line channels at different terminals, terminated at 10kΩ for each house. Again it is observed that for all four home power-line channels the good performance is obtained at ZSC1 because it is close to the transmitter.

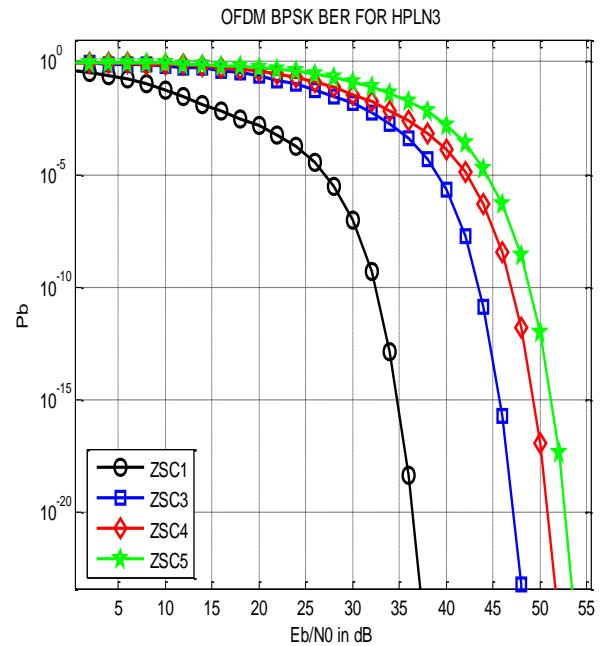


Fig 12: HPLN 3 simulation results at different loads (all terminated at 50Ω)

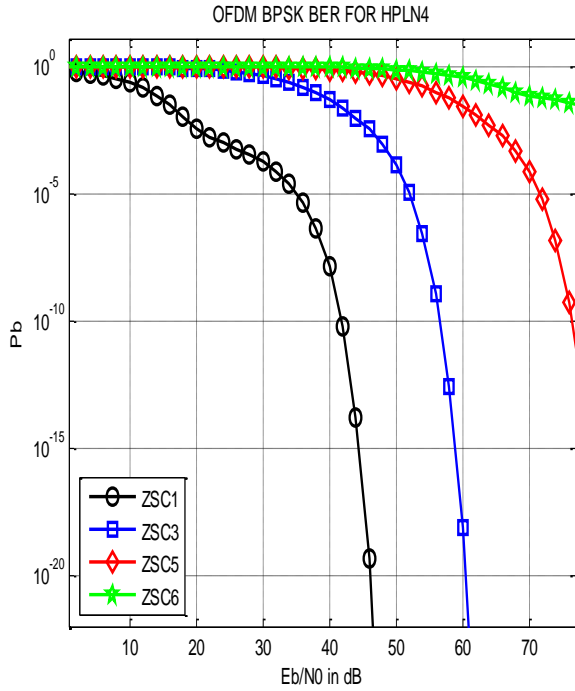


Fig 13: HPLN 4 simulation results at different loads (all terminated at 50Ω)

The good performance of 10-10 is obtained at the load ZSC1 at SNR per bit of 67dB and 76dB for HPLN 1 and HPLN 4 respectively. For HPLN2 and HPLN 3 to achieve the good performance of 10-10 at least SNR per bit of 80dB is required. The performance at the other nodes is degraded due to number of branches between transmitting and receiving ends.

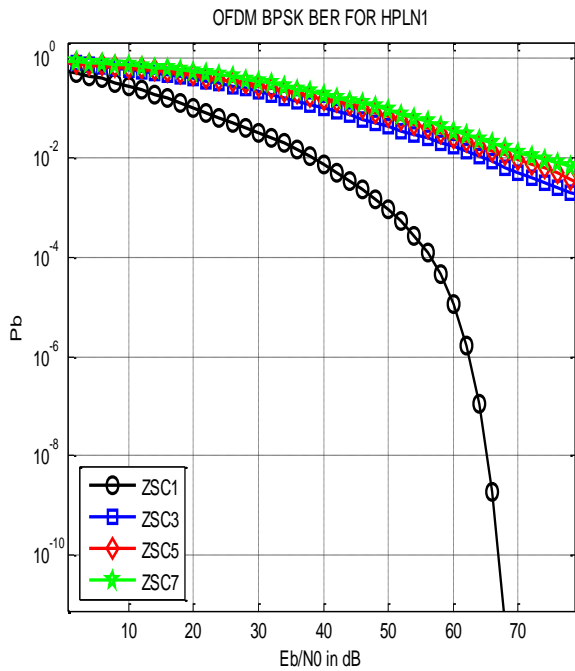


Fig 14: HPLN 1 simulation results at different loads (all terminated at 10kΩ)

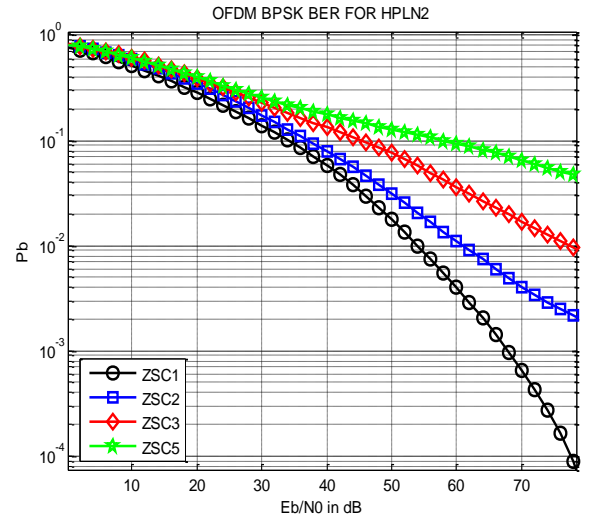


Fig 15: HPLN 2 simulation results at different loads (all terminated at 10kΩ)

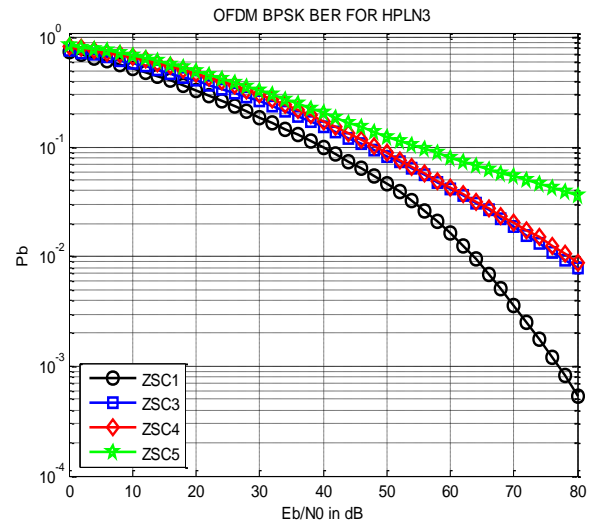


Fig 16: HPLN 3 simulation results at different loads (all terminated at 10kΩ)

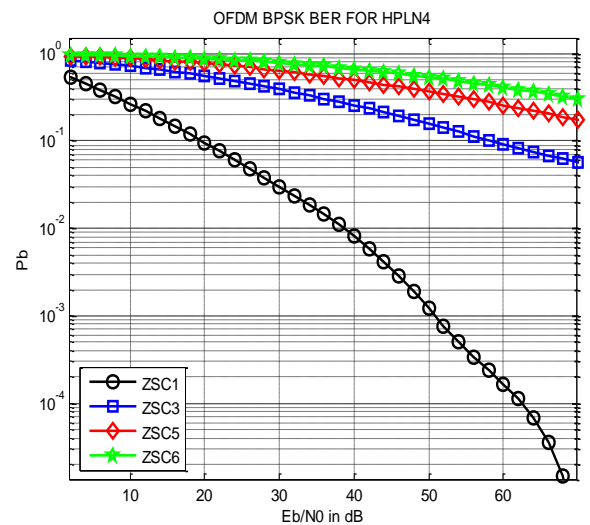


Fig 17: HPLN 4 simulation results at different loads (all terminated at 10kΩ)

7.3. Performance Comparison

By comparing simulations of the un-coded OFDM system it is observed that the performance of OFDM system with BPSK modulation for the considered networks is affected by number of branches and load impedances for each house. This is because when the channel was terminated either in low or high impedances the SNR per bit gain of 24.5dB, at least 38dB, at least 47.5dB and 35dB is required to maintain bit error rate performance of 10⁻¹⁰ at high impedances for HPLN 1, HPLN 2, HPLN 3 and HPLN 4 respectively. This indicates that an average SNR per bit gain of 47.5dB is needed so that sustained communication is still maintained in all four topologies.

8. CONCLUSION

In this study, the factors that influence the indoor BPLC system design were studied. The channel model by anatory et al has been used to simulate a realistic indoor power-line network of Tanzania. The delay spread of such networks is about 2 μ s and this has been used to calculate the number of sub-carriers and cyclic prefix required in the OFDM system based on BPSK. It was found that, when the channel was terminated either in low or high impedances the average SNR per bit gain of 47.5dB is needed so that sustained communication is still maintained in all the four home power-line networks.

8.1. Recommendations

The results of this work have shown that communication performance in Tanzania indoor power-line networks is different for each house. To maintain the same performance many houses need to be taken into account. This will help BPLC communication systems engineers to design robust and reliable communication systems. Also without coding the performance is poor because of high SNR required for better performance. To improve performance error control codes are required, to minimize SNR for a particular bit error rate.

8.2. Suggestions for further research

For future work it is recommended to perform Tanzania indoor power-line network modeling so that many houses can be investigated. The model will enable the discovery of transmission methods that can cope with different topologies of Tanzania indoor power-line networks. Also there is a need of coming up with a method of deriving the power delay profiles from the power-line channel models like that of Anatory et al.

9. REFERENCES

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