Wavelet-based Image Compression of Quasi Encrypted Grayscale Images

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ABSTRACT
As data is exchanged quickly in electronic way, information security plays a vital role in transmission and storage. Digital images are widely used in industrial purpose, so it is necessary to protect image from unauthorized access. Quasi group encryption is used to encrypt the grayscale image to provide security during transmission. Computer images are extremely data intensive and hence require large amounts of storage space. As a result, the transmission of an image from one machine to another can be very time consuming. By using image compression techniques, it is possible to remove some of the redundant information contained in images, requiring less storage space and less time to transmit. This paper is focused on selecting the most appropriate wavelet function for a given encrypted grayscale image compression. The Discrete Meyer wavelet function gives high compression ratio and the improved PSNR (peak signal to noise ratio) value for an encrypted grayscale image at decomposition level three.

Keywords
Quasi-group, PSNR (peak signal to noise ratio), wavelet function, compression ratio, data intensive.

1. INTRODUCTION
With the growth of multimedia technology over the past decades, the demand for digital information increases dramatically. The advances in technology have made the use of digital images prevalent to a large extent. Still images are widely used in applications like medical and satellite images. Digital images are comprised of an enormous amount of data. Reduction in the size of the image data for storing and transmission of digital images are becoming increasingly important as they find more applications. When the storage space or communication bandwidth is low, image is often compressed. It is necessary to reduce the size of the image with respect to bandwidth limited channel. In transmission and storage of images, security is an important issue, and one way to ensure security is the use of encryption. Consider an example, the plaintext X and the encryption function is a stream ciphertext represented by Y = X ⊕ K, where K is the secret key/hidden key and Y is the ciphertext. The operator (encryption) ⊕ is the exclusive bitwise operator [1].

Symmetric encryption is a form of cryptosystem in which encryption and decryption are performed using the same key. The most widely used symmetric cipher are DES (Data Encryption Standard) and AES (Advanced Encryption Standard). A symmetric encryption scheme has five components, a) Plain text-original data b) Encryption algorithm-performs various substitutions and transformations on plain text c) Secret key-value is independent of the plain text d) Ciphertext-scrambled data e) Decryption-reverse of the encryption algorithm to produce/reconstructed original data. The Data Encryption Standard has been the most widely used. Cipher uses 64-bit block and a 56-bit key. The Advanced Encryption Standard is a block cipher intended to replace DES for commercial applications. It uses 128-bit block size and key size of 128,192 or 256 bits. RC4 is a variable key size stream cipher with byte-oriented operations. RC4 algorithm is based on the use of a random permutation [2].

Secure encryption algorithm must withstand the attacks such as cipher text-only attack, known-plaintext attack, chosen-plaintext attack and exhaustive key attack[3]. This paper proposes a symmetric cryptographic technique called quasi-group. The quasi-group encryptor has a very good scrambling property. The purpose of the scrambler is to maximize the entropy at the output.

The basic goal of image compression is to represent an image with minimum number of bits of an acceptable image quality. All image compression algorithms strive to remove statistical redundancy and exploit perceptual irrelevancy while reducing the amount of data as much as possible. Image compression schemes can be broadly classified into two types: Lossless compression and Lossy compression. In lossless compression, the image after compression and decompression is identical to the original image and every bit of information is preserved during the decompression process. The reconstructed image after compression is an exact replica of the original one. Although lossless compression methods have the appeal that there is no deterioration in image quality, this scheme only achieves a modest compression rate. The lossless compression scheme is used in applications where no loss of image data can be compromised. Lossless compression scheme is preferred in the case of medical image compression. In lossy compression, the reconstructed image contains degradations with respect to the original image. Here perfect reconstruction of the image is sacrificed by the elimination of some amount of redundancies in the image to achieve a higher compression ratio. In lossy compression, a higher compression ratio can be achieved when compared to lossless compression [4].

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Wavelet transform has achieved 4. The mathematical equation for decryption is defined by
\[ D(a_1, a_2, a_3, \ldots, a_n) = e_1, e_2, e_3, \ldots, e_k \] (2)

where \( e_1 = a_1 \) and \( e_k = a_i / a_i \).

2.1 Encryption Algorithm

Input: Image, Encryption Key
Output: Encrypted Image
1. Get the size of the image and store it.
2. Convert image matrix into a vector.
3. Construct a new image matrix by filling the odd position values followed by even position values.
4. Convert a new image matrix into a vector.
5. Binary key data is embedded in the vector and the resulting vector is stored.
6. Convert the vector into image matrix.

2.2 Decryption Algorithm

Input: Encrypted Image, Decryption Key
Output: Decrypted Image
1. Convert the encrypted image matrix into a vector.
2. The binary key is initially used for decryption and stored as a vector.
3. Vector is converted to image matrix.
4. Image matrix is divided into two vectors and new image matrix is created by filling the odd and even positions.
5. The resulting image matrix is the decrypted image.

The encrypted images are compressed by either loss or lossless compression scheme before transmitting it in the bandwidth limited channel. Table 1 shows the duration for performing the encryption and decryption operation on various images.

### Table 1
#### Quasi-group Encryption and Decryption duration in seconds

<table>
<thead>
<tr>
<th>Image</th>
<th>Encryption(s)</th>
<th>Decryption(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cameraman</td>
<td>0.2563</td>
<td>0.3643</td>
</tr>
<tr>
<td>Lena</td>
<td>0.2560</td>
<td>0.3704</td>
</tr>
<tr>
<td>Barbara</td>
<td>0.2600</td>
<td>0.3699</td>
</tr>
</tbody>
</table>

The encryption and decryption durations of Quasi-group are compared with Mirror-like Image Encryption (MIE) algorithm and Visual Cryptography (VC) algorithm in Table 2. Mirror-like Image Encryption algorithm is based on a binary sequence and it includes 7 steps. Visual Cryptography method includes two steps. First it transforms grayscale image into four halftone images (Cyan, Magenta, Yellow and Black) and then in second step two transparencies of VC are generated. The secret image is obtained by stacking two transparencies [6].

### Table 2
#### Comparison of Encryption and Decryption algorithms duration in seconds

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Image</th>
<th>Encryption(s)</th>
<th>Decryption(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIE</td>
<td>Lena</td>
<td>0.27</td>
<td>0.22</td>
</tr>
<tr>
<td>MIE</td>
<td>Baboo</td>
<td>0.49</td>
<td>0.22</td>
</tr>
<tr>
<td>VC</td>
<td>Lena</td>
<td>1.98</td>
<td>-*</td>
</tr>
<tr>
<td>VC</td>
<td>Baboo</td>
<td>3.57</td>
<td>-*</td>
</tr>
<tr>
<td>QG</td>
<td>Lena</td>
<td>2.560</td>
<td>3.704</td>
</tr>
<tr>
<td>QG</td>
<td>Baboo</td>
<td>2.686</td>
<td>3.658</td>
</tr>
</tbody>
</table>

MIE-Mirror-like Image Encryption
VC-Visual Cryptography for Images
QG-Quasi-Group
It can be observed that quasi-group algorithm takes less time for performing encryption and decryption as compared to VC and takes less time for performing encryption as compared to MIE.

3. WAVELET TRANSFORM

Wavelet transform (WT) represents an image as a sum of wavelet functions (wavelets) with different locations and scales. Any decomposition of an image into wavelets involves a pair of waveforms: one to represent the high frequencies corresponding to the detailed parts of an image (wavelet function) and one for the low frequencies or smooth parts of an image (scaling function). Wavelet transform has achieved considerable attention in the field of image processing due to its flexibility in representing non-stationary image signals and its adapting to human visual characteristics. Their inherent capacity for multiresolution representation akin to the operation of the human visual system motivated a quick adoption and widespread use of wavelets in image processing applications. A wavelet transform divides a signal into a number of segments, each corresponding to a different frequency band [7].

A Fourier transform does not give information about the time at which particular frequency has occurred in the signal. Hence, a Fourier transform is not an effective tool to analyse a non-stationary signal. To overcome this problem, windowed Fourier transform, or short-time Fourier transform was introduced. Even though a short-time Fourier transform has the
ability to provide time information, multiresolution is not possible with the short-time Fourier transforms. Wavelet is the answer to the multiresolution problem. A wavelet has the important property of not having a fixed-width sampling window. The wavelet transform can be broadly classified into (i) Continuous wavelet transform and (ii) Discrete wavelet transform. For long signals, continuous wavelet transform can be time consuming since it needs to integrate over all times.

To overcome the time complexity, discrete wavelet transform was introduced. Discrete wavelet transform can be implemented through sub-band coding. The DWT is useful in image processing because it can simultaneously localise signals in time and scale, whereas the DFT or DCT can localise signals only in the frequency domain. The Discrete Wavelet Transform (DWT) is obtained by filtering the signal through a series of digital filters at different scales. The scaling operation is done by changing the resolution of the signal by the process of sub sampling [8].

3.1 Wavelet Families

There are many members in wavelet families, they are a) Haar b) Daubechies c) Symlets d) Coiflets e) Meyer f) Mexicanhat g) Morlet. The haar, daubechies, symlets, coiflets wavelets are supported by orthogonal wavelets. The meyer, mexicanhat, morlet wavelets are symmetric in shape. Based on their scaling function (or shape) and ability to analyze the signal, the wavelets are chosen for particular application [9].

(a) Haar: Any discussion of wavelets begins with Haar wavelet, the first and simplest. Haar wavelet is discontinuous, and resembles a step function. It represents the same wavelet as Daubechies db1. Figure 2 shows the wavelet function of Haar in which x-axis represents the time and y-axis represents the frequency.

(b) Daubechies: The daubechies wavelets are compactly supported orthonormal wavelets thus making discrete wavelet analysis possible. Daubechies family wavelets are written dbN, where N is the order, and db the "surname" of the wavelet. The db1 wavelet, as mentioned above, is the same as Haar wavelet. Figure 3 shows the wavelet function of daubechies in which x-axis represents the time and y-axis represents the frequency.

(c) Symlets: The symlets are nearly symmetrical wavelets proposed by Daubechies as modifications to the db family. The properties of the two wavelet families are similar. Figure 4 shows the wavelet function of symlet in which x-axis represents the time and y-axis represents the frequency.

(d) Coiflets: The wavelet function has 2N moments equal to 0 and the scaling function has 2N-1 moments equal to 0. The wavelet function and scaling function have a support of length 6N-1. Figure 5 shows the wavelet function of coiflet in which x-axis represents the time and y-axis represents the frequency.

(e) Meyer: The wavelet and scaling function are defined in the frequency domain. Figure 6 shows the wavelet function of meyer in which x-axis represents the time and y-axis represents the frequency.

4. COMPRESSION METRICS

The steps involved in compression and decompression are 1) Load the image 2) Generate the compressed image 3) Calculate compression ratio 4) Calculate MSE and PSNR for original and output image. 5) Obtain reconstructed image. Depending on the type of compression technique employed, the type of compression metrics used for digital image varies. The basic metric, compression ratio (3) is used to evaluate the performance of compression algorithm.

\[
\text{Compression ratio} = \frac{\text{Output file size (bytes)}}{\text{Input file size (bytes)}}\quad (3)
\]

The mean square error (MSE) is useful to measure an average value of energy lost in lossy compression of original image. A very small MSE (4) value can be taken to mean that the image is very close to original.

\[
\text{MSE} = \frac{1}{MN} \sum_{Y=1}^{M} \sum_{X=1}^{N} (I(X,Y) - I'(X,Y))^2 \quad (4)
\]
The peak signal-to-noise ratio (PSNR) is the ratio peak signal power to noise power. The common use of the PSNR is to measure the quality of reconstructed images that have been compressed. Each picture element (pixel) has a color value that can change when an image is compressed and then uncompressed. Signals can have a wide dynamic range, so PSNR is usually expressed in decibels, which is a logarithmic scale.

\[
\text{PSNR} = 20 \cdot \log_{10} \frac{255}{\sqrt{MSE}} \quad (5)
\]

5. EXPERIMENTAL RESULTS

The image processing software package (MATLAB) is used for the image processing experiments. For the above mentioned wavelets, image compression is performed and calculated the compression ratio with different wavelet families. Results of compression ratio for different wavelet families are shown in Table 3. We have taken the test images (lena, cameraman and Barbara) and have used the Haar wavelet (haar), Daubechies wavelet (db1,db2,db5,db10) Coiflet wavelet (coif1, coif3, coif5) Symlet wavelet (sym2,sym4,sym6, sym8) and Discrete Meyer wavelet (dme). From the results it is observed that Discrete Meyer wavelet has the higher compression ratio.

Table 3

<table>
<thead>
<tr>
<th>Wavelet Families</th>
<th>Cameraman</th>
<th>Lena</th>
<th>Barbara</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haar</td>
<td>97.9026</td>
<td>99.2093</td>
<td>98.6056</td>
</tr>
<tr>
<td>Db1</td>
<td>97.9026</td>
<td>99.2093</td>
<td>98.6056</td>
</tr>
<tr>
<td>Db2</td>
<td>98.0523</td>
<td>99.3008</td>
<td>98.8533</td>
</tr>
<tr>
<td>Db5</td>
<td>98.5288</td>
<td>99.4481</td>
<td>99.2458</td>
</tr>
<tr>
<td>Db10</td>
<td>98.9055</td>
<td>99.5835</td>
<td>99.4484</td>
</tr>
<tr>
<td>Coif1</td>
<td>98.3235</td>
<td>99.3292</td>
<td>99.0355</td>
</tr>
<tr>
<td>Coif3</td>
<td>98.7791</td>
<td>99.5563</td>
<td>99.4376</td>
</tr>
<tr>
<td>Coif5</td>
<td>99.1167</td>
<td>99.6627</td>
<td>99.5843</td>
</tr>
<tr>
<td>Sym2</td>
<td>98.0523</td>
<td>99.3008</td>
<td>98.8533</td>
</tr>
<tr>
<td>Sym4</td>
<td>98.4016</td>
<td>99.3867</td>
<td>99.1466</td>
</tr>
<tr>
<td>Sym6</td>
<td>98.5358</td>
<td>99.4851</td>
<td>99.2891</td>
</tr>
<tr>
<td>Sym8</td>
<td>99.6899</td>
<td>99.5245</td>
<td>99.4112</td>
</tr>
<tr>
<td>Dmey</td>
<td>99.7519</td>
<td>99.8539</td>
<td>99.7490</td>
</tr>
</tbody>
</table>

Quasi-group encryption is performed prior to protect the privacy. Figure 7 shows the original image. Figure 8 shows the quasi-group encrypted image. A good reconstructed image is one which has high PSNR and low MSE value. From the results, we concluded that Discrete Meyer wavelet is good for compressing the encrypted image. Figure 9 shows the first level decomposition of Discrete Meyer wavelet, figure 10 shows the second level decomposition of Discrete Meyer wavelet and figure 11 shows the third level decomposition of Discrete Meyer wavelet for encrypted image. It provides low MSE and high PSNR value at the decomposition level three. Figure 12 shows the reconstructed image and Figure 13 shows the decrypted image. Table 4 shows the MSE, PSNR and Bit rate for various images after applying Discrete Meyer wavelet function with decomposition level three.

Table 4

<table>
<thead>
<tr>
<th>Image</th>
<th>MSE</th>
<th>PSNR</th>
<th>Bit rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cameraman</td>
<td>2.3445</td>
<td>44.4303</td>
<td>2.4571</td>
</tr>
<tr>
<td>Lena</td>
<td>2.5530</td>
<td>44.0603</td>
<td>2.4764</td>
</tr>
<tr>
<td>Barbara</td>
<td>9.4575</td>
<td>38.3730</td>
<td>2.7319</td>
</tr>
</tbody>
</table>
In this paper we presented the compression of encrypted grayscale images. The quasi group has good scrambling, that constitutes an excellent method and generation of pseudo-random sequences. The encrypted image is compressed by using wavelet-based image compression scheme. We have applied different wavelet functions on encrypted images to get an improved PSNR value and compression ratio. We analyze the compression ratio obtained after each wavelet-based image compression and found that Discrete Meyer wavelet function provides maximum compression ratio for an encrypted image.

7. REFERENCES

8. AUTHORS PROFILE
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