Blind Equalization in OFDM Systems by Channel Shortening and Channel Diversity Exploitation

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ABSTRACT
We propose two alternative approaches for blind channel shortening to design time domain finite impulse response equalizer (TDE) in multicarrier single input, multiple output systems. The first approach we utilize the constant envelope of the transmitted signal called constant modulus (CM). Second approach is based on decision directed algorithm, where we update time domain equalizer using decision directed cost function. These cost function have been widely studied for single carrier systems, implementing them in multicarrier scenario is of great importance. Simulations shows they outperform classical multicarrier equalization by restoration of redundancy (MERRY) and Carrier nulling algorithm (CNA) that utilizes redundancies inherent in carriers in terms of bit error rate.

General Terms
Channel equalization algorithms in wireless communication.

Keywords
Blind equalization, Constant modulus algorithm, decision directed algorithm, SIMO, OFDM.

1. INTRODUCTION
Future communication systems aim to provide high data rate with reliability. The main challenge to achieve this goal is the dispersive effects of communication channels, which leads to inter-symbol interference (ISI). Multicarrier modulation techniques such as OFDM and DMT have been widely used in high speed digital communication systems to combat channel frequency selectivity, the technique work effectively when the delay spread of the channel does not exceed the cyclic prefix (CP) inserted at the transmitter [1]. Extending the CP length is bandwidth inefficient while insufficient CP length results in inter-carrier (ICI) and inter-symbol (ISI) interference due to subcarriers orthogonality destruction. In this case, equalization at the receiver to shorten the effective channel to appropriate channel becomes important. Channel shortening is done by means of a time domain equalizer (TDE), which is finite impulse response filter (FIR). Cascaded channel-equalizer arrangement produces the effective shortened channel impulse response. Most of channel shortening schemes utilizes training sequences which is bandwidth inefficient [2]. These methods have been studied in the context of wire line systems such as Digital subscriber line (xDSL) [2]. High complexity nature and being non-adaptive have made more quests for better method [3]. Blind adaptive algorithm improves bandwidth by exploiting signal properties such as presence of CP or autocorrelation characteristics in multicarrier signal [2], [3].

The design of time domain equalizer (TDE) extensively studied in the literature [2],[3],[4],[5],[7,18]. Most supervised methods originate from (Falconer and Magee) [5], they proposed a minimum mean-square (MMSE) method for channel shortening, aiming at reducing the complexity in maximum likelihood sequence estimation which has exponentially growth with respect to channel length. Melza, Younce and Rohrs [4], proposed the maximum shortening SNR, that attempt to minimize the energy of the outside window of interest while keeping the inside energy fixed. Aldhahil and Cioff [8] proposed maximum geometric SNR approach that incorporate the optimization of achievable bit rate into TDE design, in fact all these approaches utilizes some of constraints to insure performance. In contrast to these supervised approaches, Blind methods have been proposed by various scholars recently. Classical multicarrier equalization by restoration of redundancy (MERRY) have been studied in [9]. In [10], [11] fast converging recursive implementation and generalized MERRY have been proposed as improved versions. Sum squared autocorrelation minimization (SAM) proposed in [13], it exploit the second order statistics (SOS) by minimizing the sum of squared autocorrelation of the combined channel equalizer impulse response outside the desired length. In fact the whiteness of the signal and wide sense stationarity assumptions are taken into account, the cost function is defined and optimized using stochastic gradient descent algorithm. Several improvement versions of SAM algorithm that focuses to reduce complexity have been proposed, such as SLAM in [12], GLHSAM in [16]. Another famous approach for blind equalization is carrier nulling algorithm (CNA) initially proposed by De couville et al [19], then improved through lag hopping by Romano and Barbarossa in [17]. The approach utilizes the presence of null carrier in multicarrier transmitter structure, it is well known that null carriers contain zero energy; hence by minimizing the energy falling in these null carriers an adaptive procedure is developed with low complexity. In [20], an improved version termed “maximization of useful-to-null subcarrier energy ratio” was proposed, but the approach has high computation complexity using power iteration method. Considering all these approaches we can see that they rely on redundancies present on the multicarrier structure to find time domain equalizer without considering the effects of equalizer response on useful carriers. This in turn must give inefficient shortened channel which lead to higher bit error rate.
In this paper we propose the use of constant envelopes of the signal at the receiver and derive the Time domain approach for blind equalization. Also we utilize decision directed function to implement multicarrier blind equalization. These two approaches are being compared with the benchmark approaches.

The paper is organized as follows. Section 2 gives the MC-SIMO data model, section 3 and 4 present the proposed TDE update criterions and adaptive implementation, section 5 numerical data and simulation is provided and finally section 6 concludes while section 7 provides references.

2. MULTICARRIER DATA MODEL

In multicarrier modulation subcarriers are overlapped closely together while the orthogonality is maintained. The procedure is done by mapping the data bits onto complex valued symbols from a given constellation (QPSK, QAM etc.) and applying an inverse discrete Fourier transform using (IFFT) to transform them into time domain sequences. Baseband equivalent MC system model is depicted in figure 1 (next page). N parallel data sequences denoted by \( a_{k,n} \) are grouped into a block \( a_k \), where \( n \in \{1, 2, ..., N\} \) subcarriers number, \( k \) is a block index. The \( k^{th} \) block modulates the different subcarriers using IFFT operation, resulting to a vector of time domain sample denoted by

\[
X_k = \left[ x_{k,1}, x_{k,2}, ..., x_{k,N} \right]^T
\]

and expressed by

\[
X_k = F^H a_k
\]

Where \( F \) is the FFT matrix, \( \{F\}_{k,l} = (1/\sqrt{N}) e^{j(2\pi kl)/N} \) and \( k, l \in \{0, 1, ..., N - 1\} \). The last \( V \) samples called cyclic prefix (CP) are copied and prepended at the beginning of the block \( X_k \) to form the \( k^{th} \) block of length \( M = N + V \), given by

\[
\tilde{X}_k = \left[ x_{kM+1}, x_{kM+2}, ..., x_{kM+N} \right]^T = \left[ x_{kN-P+1}, x_{kN-P+2}, ..., x_{kN}, x_{kN+1}, x_{kN+2}, ..., x_{kN+V} \right]^T
\]

(1)

this will result to orthogonality of the subcarriers. Data are transmitted though several channels deployed (through oversampling or multiple antennas) after parallel to serial operation (P/S). Denoting the finite impulse response channel (FIR) of length \( L_k \) by \( h_1, h_2, ..., h_S \). Assuming transmitter and receiver are well synchronized, the received data at s branch \( (s \in \{1, 2, ..., S\}) \) is given by

\[
\tilde{r}_{S,kM+m} = \sum_{l=1}^{L_k} h_{S,l} \tilde{x}_{kM+m-l} + \tilde{b}_{S,kM+m}
\]

(2)

Where: \( \tilde{b}_{S,kM+m} \) is the noise sample, assumed to be white i.i.d and \( m \in [1, 2, ..., M] \) is the sample index within the block. When \( V \leq L_k \) then time domain equalizer (TDE) is needed before the FFT operation. For SIMO transceivers, channel shortening is performed by S TDE’s \( \left[ W_1, W_2, ..., W_S \right] \) of length \( L_n \), whose output is given by

\[
\tilde{y}_{S,kM+m} = \sum_{l=1}^{L_n} W_{S,l} \tilde{r}_{S,kM+m-l} = W_S^T \tilde{r}_{S,kM+m}
\]

(3)

Where

\[
W_S = [w_{S,1}, w_{S,2}, ..., w_{S,L_n}]^T, \tilde{r}_{S,kM+m} = [\tilde{r}_{S,kM+m-L_n}, ..., \tilde{r}_{S,kM+m}]^T
\]

After adding all S time domain equalizer (TDE), the outputs are obtained as:

\[
\tilde{y}_k = [\tilde{y}_k, \tilde{y}_k, \tilde{y}_k]^T, \text{the cyclic prefix is removed from the received block } \tilde{y} \text{ to obtain the } k^{th} \text{ received block vector:}
\]

\[
c_i = \sum_{s=1}^{S} \sum_{l=1}^{L_n} h_{s,l} w_{s,l-l}
\]

(5)

At the receiver, the effective equivalent channel output is S/P converted, M parallel sub-stream are formed, that is \( k^{th} \) block

\[
\tilde{y}_k = [\tilde{y}_k, \tilde{y}_k, ..., \tilde{y}_k]^T
\]

Figure 1. MC-SIMO baseband equivalent system model.

\[
\tilde{y}_{kM+m} = \sum_{s=1}^{S} \tilde{y}_{s,kM+m}
\]

\[
= \sum_{s=1}^{S} c_s \tilde{x}_{kM+m-l} + \sum_{s=1}^{S} \sum_{l=1}^{L_n} W_{s,l} \tilde{r}_{s,kM+m-l}
\]

(4)

Where the effective equivalent channel of length \( L_e + 1 \) is:
\[ y_k = [y_{k,1}, y_{k,2}, \ldots, y_{k,N}]^T = \left[ \tilde{y}_{LM=P+1}, \tilde{y}_{LM+P+2}, \ldots, \tilde{y}_{LM+P+N} \right]^T \]  \hspace{1cm} (6)

At this point serial streams are converted back to parallel. The very important parameter at this stage is synchronization delay \( \delta \) that determines where the receiver should break the inputs samples into blocks.

\[ y(k) = [y_{LM+1}, y_{LM+2}, \ldots, y_{LM+N}]^T \]  \hspace{1cm} (7)

Thereafter, each block is passed through Fast Fourier Transform (FFT) as:

\[ Y(k) = F[y(k)] \]  \hspace{1cm} (8)

The output of FFT for each tone is equalized by one tap frequency domain equalizer (FEQ) to scale and insure proper orientation of the symbol.

\[ a_{k,i} = Y(k).FEQ_i \]  \hspace{1cm} (9)

Where \( k \) and \( i \) denote the \( k^{th} \) block and \( i^{th} \) sample respectively. The effective channel is expressed as the sum of convolution of each channel with its respective time domain equalizer (TDE) that is:

\[ c = c_1 + c_2 \]  \hspace{1cm} (10)

Where \( c_1 = h_1 * W_1 \) and \( c_2 = h_2 * W_2 \)

3. CONSTANT MODULUS ALGORITHM FOR A TDE

Constant modulus approach has been used widely in single carrier systems; here we develop an adaptive criterion for multicarrier systems. Consider the cost function defined at the output of the FFT and frequency domain equalization FQE:

\[ J_{CM} = \sum_{i=1}^{N} E[(\bar{a}_{k,i}^2 - R_i)^2] \]  \hspace{1cm} (11)

Where \( a_{k,i}, R_i \) denotes the particular tone and statistics of the transmitted sequences. Using the instantaneous stochastic gradient descent optimization procedure, we have:

\[ \frac{\partial J_{CM}}{\partial W_j} = \sum_{i=1}^{N} \frac{\partial |e_i|^2}{\partial W_j} = \sum_{i=1}^{N} (\bar{v}_s e_i^* + e_i (\bar{v}_s e_i^*)) \]  \hspace{1cm} (12)

Where \( e_i = (\bar{a}_{k,i}^2 - R_i) \). Recalling that the gradient with respect to complex vector is given by:

\[ \frac{\partial a_{k,i}^2}{\partial W_j} = 0.5 \left( \frac{\partial a_{k,i}^2}{\partial W_{j,R}} + j \frac{\partial a_{k,i}^2}{\partial W_{j,I}} \right) \]  \hspace{1cm} (13)

Where \( R, I \) and * refers to real, imaginary and complex conjugate respectively. It can be shown that:

\[ \frac{\partial a_{k,i}}{\partial W_j} = 0 \]  \hspace{1cm} (14)

\[ \frac{\partial a_{k,i}^2}{\partial W_j} = 2FEQ_i \sum_{i=1}^{N} f_{i,j}^* \tilde{r}_{i}^*(Mk+1) \]  \hspace{1cm} (15)

After further manipulations of (12) we arrive at:

\[ \frac{\partial J_{MCDDA}}{\partial W_j} = 4\sum_{i=1}^{N} e_i \left( \bar{F}EQ_i \sum_{i=1}^{N} f_{i,j}^* \tilde{r}_{i}^*(Mk+1) \right) \]  \hspace{1cm} (16)

\[ \frac{\partial J_{MCDDA}}{\partial W_j} = 4\sum_{i=1}^{N} e_i \left( \bar{F}EQ_i \sum_{i=1}^{N} f_{i,j}^* \tilde{r}_{i}^*(Mk+1) \right) \]  \hspace{1cm} (17)

Where \( \tilde{r}_{i}^*(Mk+1) = r_{i}^*(Mk+l+1: -1: Mk+l - L_{m} + 1)^T \)

The two time domain equalizers (TDE) can be updated by the procedure below noting that \( \mu \) is the step size.

\[ W_{i,k+1} = W_{i,k} - \mu \bar{N}_w J_{MCDDA} \]  \hspace{1cm} (18)

\[ W_{2,k+1} = W_{2,k} - \mu \bar{N}_w J_{MCDDA} \]  \hspace{1cm} (19)

4. DECISION-DIRECTED ALGORITHM (DDA) FOR TDE

The Decision-directed algorithm selects the nearest symbol in the constellation relatively to the current received symbol estimate and the equalizer is adapted by minimizing the mean square error (MMSE) of the distance between them. For single carrier the cost function is defined as:

\[ J_{DDA} = E[(Q | a_k) - a_k^2] \]  \hspace{1cm} (20)

We define the multicarrier cost function as:

\[ J_{MDDA} = \sum_{i=1}^{N} J_{DDA} = \sum_{i=1}^{N} |e_i|^2 = \sum_{i=1}^{N} e_i e_i^* \]  \hspace{1cm} (21)

Where \( e = Q | a_k) - a_k \) and we have considered instantaneous cost function, thus expectation operator is removed. Taking the stochastic gradient descent of the cost function with respect to equalizer vectors as:

\[ \frac{\partial J_{MDDA}}{\partial W_j} = -2 \sum_{i=1}^{N} \bar{v}_s e_i e_i^* + e_i (\bar{v}_s e_i^*) \]  \hspace{1cm} (22)

The gradient of the output of quantizer is zero, since it is constant. After modest algebra and keeping in mind equations (14) and (15) we realize that:

\[ \frac{\partial J_{MDDA}}{\partial W_j} = -2 \sum_{i=1}^{N} e_i \left( \bar{F}EQ_i \sum_{i=1}^{N} f_{i,j}^* \tilde{r}_{i}^*(Mk+1) \right) \]  \hspace{1cm} (23)

\[ \frac{\partial J_{MDDA}}{\partial W_j} = -2 \sum_{i=1}^{N} e_i \left( \bar{F}EQ_i \sum_{i=1}^{N} f_{i,j}^* \tilde{r}_{i}^*(Mk+1) \right) \]  \hspace{1cm} (24)

The two time domain equalizers (TDE) can be updated by the procedure below noting that \( \mu \) is the step size.

\[ W_{i,k+1} = W_{i,k} - \mu \bar{N}_w J_{MDDA} \]  \hspace{1cm} (25)
\[ W_{2,k+1} = W_{2,k} - \mu \nabla J_{MCDDA} \]  

(26)

5. SIMULATIONS AND DISCUSSION

In this section we perform numerical simulation for the adaptive blind channel shortener derived. The simulation parameters used are typical to that of wireless LAN standard IEEE 802.11a: 4 QAM (QPSK) signaling was used, on which we generated 10,000 number of FFT blocks each block have a size of 64 (i.e. 64 FFTSIZE) and cyclic prefix of length 16.

The Rayleigh channel model with exponentially distribution profile was generated with 32 taps. Two equalizer (system with two antennas S=2) of length 48 was used. MERRY, CNA and multicarrier training algorithms (MCTA) were used for comparison purpose. Step size parameters used for the algorithms are shown in Table 1

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>FQE ((\mu))</th>
<th>TDE ((\mu))</th>
</tr>
</thead>
<tbody>
<tr>
<td>MCT</td>
<td>0.005</td>
<td>0.00002</td>
</tr>
<tr>
<td>MCDD</td>
<td>0.005</td>
<td>0.000003</td>
</tr>
<tr>
<td>MCCM</td>
<td>0.005</td>
<td>0.000005</td>
</tr>
<tr>
<td>MERRY</td>
<td>0.005</td>
<td>0.0003</td>
</tr>
<tr>
<td>CNA</td>
<td>0.005</td>
<td>0.000003</td>
</tr>
</tbody>
</table>

Table 1. Step size used in algorithms

Two simulations where performed. One is when the system has null carriers and the other when the system has no null carriers. Fig. 2 below shows channel response before equalization (shortening) and Fig. 3 show after equalization with MCTA (multicarrier trained algorithm), only taps energy left are within CP length.

In case we introduce some carriers with zero energy the BER against SNR is depicted on the Fig. 5 below. 12 null carriers were used on which 6 were inserted at the beginning of the FFT block and 6 where inserted at the end of the FFT block. The BER performance for these algorithms does not change much when more number of FFT block is used to adapt the equalizer, otherwise the performance of MCDDA and MCCMA would have to degrade seriously since they have no information on the presence of zero energy in some carriers as MCTA do. CNA (carrier null algorithm) is also compared with others blind algorithm as depicted in the figure 5.
6. CONCLUSION

In this article we have introduces the BER performance of two blind channel shortening algorithms for multicarrier systems. When the delay spread of the channel is greater than CP, time domain equalizer is important for shortening the channel impulse response. We have compared the performance of the derived algorithms relative to supervised and other unsupervised methods, it have been observed that algorithms that depends on redundancies requires more data for updating the equalizer so as to have better convergence, incorporating fractionally equalization structure has improved the performance of the constant modulus algorithm in multicarrier system (MCCMA). For this perspective we have seen that the proposed methods outperform other blind methods. More analysis in terms of computation complexity, presence of colored noise and other interferes is currently being investigated. Incorporating channel coding methods and MIMO system might further improves the proposed blind methods.

7. REFERENCES


